P-194

ENGR-90-006 TSF1-R-014

(MACA-CH-186,77) THE SEFTUTS OF FURCTION ON A SINGLE STELAW SHEAR LAYER AND ITS PARENT BOUNDARY LAYER (Michigan State Univ.) 184 MOU- . 1.

G3/34 U277520

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lateral coordinate
У
          lateral coordinate in wall units
          transverse coordinate
GREEK SYMBOLS
          angular acceleration
          angle in the XY plane between velocity vector and axis or X
γ
           array probe
          velocity fluctuation see (13)
δυ, δν
          boundary layer displacement thickness
          hot-wire voltage ratio
ζ
          offset hot-wire voltage ratio
          momentum deficit thickness or angular position
          momentum deficit thickness at separation
\theta_{\Omega}
          kinematic viscosity
           locally scaled perturbation level, see (14)
          phase angle
           angular acceleration
          width measure of the forced shear layer, see (17)
SPECIAL SYMBOLS
           time average of the quantity ( )
(\overline{\phantom{a}})
           rms of the fluctuating quantity ()
(~)
           phase average of the quantity ( )
(< >)
           the quantity ( ) for the forced condition
```

()_f

Nomenclature

A,B,n	coefficients for Collis and Williams equation
A _e	piston amplitude
$C_0 \dots C_n$	polynomial coefficients
c _f	local skin friction coefficient
f	frequency
E	hot wire voltage
Q	velocity at hot-wire
Q_3	velocity on wire 3
Q ₄	velocity on wire 4
$R_{oldsymbol{ heta}}$	Reynolds number based on θ
St	Strouhal number
u'	streamwise velocity fluctuation
u'(ø)	u' at phase angle ϕ
u ⁺	streamwise velocity in wall units
U _T	friction velocity
u _o	free Stream velocity
v'	lateral velocity fluctuation
v' (φ)	v' at phase angle ϕ
V _e	entrainment velocity
w _p	piston width
x	streamwise coordinate
x ₀	virtual shear layer origin

INTRODUCTION

1.1 Overview

Forcing and its effect on fluid flows has become an accepted tool in the study and control of flow systems. It has been used both as a diagnostic tool, to explore the development and interaction of coherent structures, and as a method of controlling the behavior of the flow. A number of forcing methods have been used in order to provide a perturbation to the flow; among these are the use of an oscillating trailing edge, acoustically driven slots, external acoustic forcing, and mechanical piston methods.

There have been numerous studies into the effects of forcing on free shear layers. Substantial information can be found in the review articles (e.g. Fiedler [1988] and Hussain [1986]) and in the original publications which they cite.

The investigation presented here documents the effect of a planar mechanical piston forcing on a single stream shear layer; it can be noted that this is one of the lesser studied free shear layers. The single stream shear layer can be characterized by its primary flow velocity scale \mathbf{U}_0 and the thickness of the separating boundary layer θ_0 . The velocity scale \mathbf{U}_0 is constant over the length of the flow field; $\theta(\mathbf{x})$ can be used as a width scale to characterize the unforced shear layer. In the case of the forced shear layer the velocity field is a function of phase time and definition of a width measure becomes somewhat problematic.

1.2 Similar prior work

The effects of sinusoidal forcing of the separating boundary layer in a single stream shear layer have been studied by Fiedler and Mensing [1985] and Disimile [1986]. An acoustic forcing mechanism was used in the Fiedler and Mensing study; the acoustic wave was applied to the separating boundary layer through a wave guide channel. Two separate trailing edge geometries were used in their study, see Figure The separating boundary layer for their study had an R $_{\boldsymbol{\theta}}$ value of 1. 830. Experimental observations of the resulting large scale motions measurements and smoke visualizations. included hot-wire Hot-wire measurements in the shear layer indicated maximum $\tilde{\mathbf{v}}$ levels at $S_{+}=(x-x_{0})f/U_{0}\simeq 1$. This result, combined with the flow visualization data, suggests that the large scale coherent motion has its maximum organization at this location. A comprehensive evaluation of the

effect of forcing frequency and amplitude effects on the shear layer is provided by the Fiedler and Mensing study.

The Disimile investigation, which was executed on the same apparatus as the current study, used a mechanically driven piston to provide a low amplitude forcing of the separating boundary layer. Expressing the forcing piston amplitude as $A(t) = A_0 \cos \omega t$, the Disimile investigation was performed using $A_0 = 0.76$ mm, or $A_0/\theta_0 \simeq 0.12$. The Disimile study revealed the formation of a large scale coherent motion and documented its translation properties in phase time. A negligible influence by the forcing input on the separating boundary layer was indicated.

1.3 The current experiment

The study documented here, which was designed to build upon the previous investigations, was to examine the effect of large amplitude forcing at separation on the separating boundary layer. The effects of forcing on the developing shear layer constituted the second phase of the present study. A third phase of the work was to examine the behavior of the entrainment field for the shear layer, and its response to the strongly forced shear layer.

The experimental approach taken was to provide a large amplitude forcing to a large separating boundary layer. In particular, a forcing amplitude of $A_0/\theta_0 = 0.58$ was used with a separating boundary layer characterized by $R_{\theta(0)} = 5500$. and $\theta_0 = 6.5$ mm. Phase averaged

measurements, using a single hot-wire anemometer, were performed throughout the development region of the shear layer and the upstream boundary layer. Planar velocity vector measurements in the entrainment region were provided through the use of a 4 wire probe. As a result of the large physical dimension of the separating boundary layer (θ_0 = 6.5 mm) a 4 wire probe was able to be used to examine the planar velocity field just downstream of the separation lip.

EXPERIMENTAL EQUIPMENT AND PROCEDURES

2.1 Experimental Facility

2.1.1 Tunnel

The tunnel used for the present study was a single stream shear layer suction tunnel, a plan view of which is presented in Figure 2. The test section for the tunnel was subatmospheric, with the open volume of the laboratory between the fan exit and the inlet to the tunnel serving as a settling chamber for the return flow. The test section for the tunnel is shown in Figure 3, with a $0.5 \text{m} \times 0.8 \text{m}$ core flow exiting into a $1.7 \text{ m} \times 0.8 \text{ m} \times 3.0 \text{ m}$ test section. (The height for the entire area shown in Figure 3 was a constant 0.8 m.) The tunnel was equipped with a glass wall over the entire length of the test section which enabled optical positioning methods to be used to locate the probe. The test section, downstream of the separation step (at x = 0.0) was equipped with a movable floor traversing mechanism, as shown schematically in Figure 4.

The prime mover for the tunnel was a Chicago 30.5 SQA airfoil fan powered by a 15 Hp variable speed DC motor. The motor was equipped with a tachometer feedback control system which maintained the motor speed to within \pm 0.5% of the set value.

Flow conditioning upstream of the test section was provided by three two-dimensional contractions with an overall contraction ratio of 22.6 to 1. Additional conditioning was provided by turbulence manipulators downstream of the first two contractions. These manipulators consisted of a 3.175 mm diameter honeycomb with an 1/d ratio of 8, and a set of 30 mesh screens spaced 12.7 mm apart. A final asymmetric contraction, to the boundary layer development section, was placed downstream of the manipulators.

The boundary layer development section, as shown in Figure 5, conditions the boundary layer upstream of the separation lip. This conditioning takes the form of removing the upstream boundary layer formed during the last contraction through use of a separate bleed fan. This low momentum fluid was extracted using a splitter plate as shown in Figure 5. The plenum downstream of the splitter plate exhausted into the receiver through a Buffalo Forge 37v fan. This fan was driven by a 3 Hp A/C constant speed motor through an adjustable speed belt drive allowing the adjustment of the bleed flow.

A distributed roughness trip mechanism, consisting of 609. mm of 16 grit sandpaper, was employed. This trip method was based on the

work by Klebanoff and Diehl [1951]. The distributed roughness was followed by 1290. mm of smooth wall. The final 655. mm of wall consisted of white formica covered particle board providing a surface with the following desirable characteristics;

- a) A low surface roughness; which minimized wall roughness effects on the developing boundary layer.
- b) A non-conducting surface; which provided desirable heat transfer properties. When operated near a conducting surface the heat loss from a hot-wire anemometer will give rise to significant errors in measurement. Usage of a non-conducting surface such as formica covered particle board minimizes this effect.
- c) A white smooth surface; which enabled an optical wire-shadow positioning method to be used to accurately determine the position of the hot-wire when near the wall.

In contrast with many single stream shear layer facilities, the facility used in this study had the attribute of being able to both condition and to have control over the fluid stream entrained by the shear layer. The entrained fluid was taken from the open laboratory volume through filter media and into a settling chamber. One wall of the settling chamber consisted of a series of throttle modules, which allowed for the control of the flow rate through the use of a sliding throttle plate as shown in Figure 6. The flow passed through the throttle modules, then through a coarse screen, a contraction to the

0.8 m test section height, and into a honeycomb and fine screen turbulence manipulators; see Figure 7.

2.1.2 Traverse system

The probes were positioned by means of a 3 axis traversing system, shown schematically in Figure 8. This traverse consisted of a rack and pinion drive in the X direction, a screw feed drive in the Y direction, and a worm gear drive in the θ direction. Each axis was driven through stepper motors under computer control. The resolution in the X, Y, and θ directions were .8 mm, .01 mm, and .02 degrees respectively.

2.1.3 Forcing System

Forcing of the separating shear layer was provided by a motor driven piston forcing mechanism. The basic mechanical system was employed in previous research of lower amplitude forcing effects; see Disimile [1984] and Figure 9. The piston was belt driven using a constant speed (1760 RPM) 1 Hp AC motor and variable pitch pulleys. The piston motion was obtained using an eccentric as shown in Figure 10. The time dependant position of the piston can be written as:

$$A - A_0 \times \cos(\phi) \tag{1}$$

Where ϕ is the angular position of the rotating shaft.

This study was performed using an amplitude $A_0 = 3.84$ mm and a frequency of 16.1 Hz. Phase information was obtained through use of an optical pickup on the forcing piston drive shaft as shown in Figure 11.

2.2 Measuring Equipment

2.2.1 Pressure measurements

Pressure measurements were made using an MKS baratron model 310 1 Torr pressure transducer and 170M 6-C amplifier. The overall uncertainty for all pressure measurements is $\pm .08\%$ of indicated plus $\pm .00001$ Torr.

2.2.2 Anemometry

All hot-wire measurements in this study used locally fabricated hot-wires and probes. A typical straight wire is shown in Figure 12. The wire itself is 5 micron tungsten with an overall length of 3 mm and an active length of 1 mm. The inactive portions of the wire are copper plated to a nominal diameter of 50 microns. The wires were mounted on the tips of jewelers broachs, the plating as well as the small diameter prongs lead to minimal interference effects. The measurements were all performed with the wires operated in the constant temperature mode at a nominal overheat of 0.7.

Two types of probes were used in this study, single wire probes and a compact vorticity probe. The single wire probes consisted of a

single wire as described above, operated with the wire parallel to the Z axis. A modified wire mounting was used for the wires involved in the boundary layer measurements. Specifically, the wire was mounted on the side of the tip of the broachs, rather than the end of the broachs; see Figure 13. This allowed the active portion of the wire to be brought closer to the wall.

The compact vorticity probe is a 4 wire probe allowing for the resolution of velocity components and gradients in a single plane. The probe is shown schematically in Figure 14 and consists of a single X array, with the addition of two straight wires. The individual wires are as described above.

As can be seen from Figure 14, the overall size of the measurement area is 1 mm² normal to the mean flow. Although no large scale model studies have been performed on this probe to determine possible prong interference effects, results up to the time of this writing indicate that such effects are minimal. Measurements at various orientations in the calibration stream return the correct values given the probe orientation. In addition measurements of the thermal interference between wires, obtained by running all possible on and off combinations of wires while the probe is in the calibration stream, show no thermal interference between wires.

Two types of anemometers were used in this work; these were the DISA model 55M01 and the TSI model 1755. In both instances the

nominal output was approximately 4.5 volts at the free stream speed of 13 mps. Electrical noise levels for both types of anemometers were approximately 1 millivolt rms. Frequency response for the anemometry was approximately 20 KHz at 13 mps.

2.3 Data Acquisition System

2.3.1 Computer system

The computer system used for both the data taking and all data processing was a DEC 11/73 microcomputer; this system is shown diagrammatically with the associated data acquisition and laboratory interface hardware in Figure 15. This computer consisted of the central processing unit, two RD-53 70 megabyte hard disk drives, a 90 megabyte Tk50 tape drive, an AXVIIC A/D, a KWVIIC programmable clock, a DRVIIJ digital interface, a DRVIIW DMA interface, and miscellaneous other serial and networking interconnects.

The AXVIIC A/D provided limited sampling capability which was used primarily for monitoring the tunnel speed and other experimental parameters prior to the actual data taking.

The DRV11J digital interface and KWV11C programmable clock, in conjunction with a custom built stepper motor translator and driver system provided computer control over the traversing system.

2.3.2 Primary A/D

The primary A/D used for the experimental work was a TSI IFA200 12 bit simultaneous sample 10 channel unit. This A/D was configured to provide an input signal range of 0 to +5 volts, giving a least significant bit level of 1.22 millivolts. The IFA200 is a self contained unit providing it's own internal clock and sampling circuitry. Interface to the 11/73 computer was through a DRV11W DMA interface, providing a maximum single channel sample rate of 50 KHz, and a total throughput of 250 thousand samples per second. The IFA200 used was a true simultaneous sample A/D, consisting of 10 independent A/Ds which were driven by a common sample signal. An analog delay adjust in the sample signal was provided, and for all data in this study the A/D was calibrated to provided a channel to channel sample uncertainty equivalent to a 0.0001 mm convection length at the typical free stream velocity of 13 mps.

2.3.3 Phase pickup

The phase trigger used to conditionally sample the forced data in this study was provided by means of a metal tab passing between the sensing elements of an optical pickup, see Figure 11. This arm was mounted at a radius of 100 mm giving a mechanical positional uncertainty of approximately 0.2 degrees.

An electrical schematic of the pickup and conditioning circuit is shown in Figure 16. The electrical output from the pickup is

amplified, fed into a one-shot multivibrator, buffered to standard TTL levels and fed to the IFA200 A/D. The one-shot multivibrator is used to provide a positive output duration of approximately 30% of the forcing period. The overall uncertainty caused by the electrical system is negligible for the forcing period used.

2.4 Data Processing

2.4.1 Single Wire

The hot wires were all calibrated in the low disturbance free stream flow of the tunnel. The physical location x = 150. mm and y = -250. mm was used for the calibrations. The calibration data were obtained as the mean of 2000 samples taken at 200 Hz. A single calibration data set consisted of measurements at 7 or more speeds ranging from 1.0 to 13.5 mps. A pitot static tube was used in conjunction with the MKS baratron pressure transducer to provide the reference velocity.

The calibration data were used to define the coefficients (A,B,n) in the modified Collis and Williams relation,

$$E^2 = A + B \times Q^n \tag{2}$$

where E is the measured wire voltage and Q is the tunnel speed. These A, B, and n were values determined by using an ordinary least squares method to determine A and B given n, and minimizing that relation as a

function of n.

All processing of the anemometry data was executed by first converting the measured voltages to velocities using the calibration constants on a data point by data point basis, and then performing statistical processing on the resulting velocities.

2.4.2 Compact Vorticity Probe

2.4.2.1 Calibration

The calibration of the compact vorticity probe was also executed in the low disturbance free stream flow of the tunnel at X=150. mm and Y=-250. mm using a pitot static tube and the Baratron pressure transducer as a velocity reference. Sampling details for a single calibration point were the same as those used for a straight wire; however, as a result of the processing algorithm used, the calibration data were required at a number of angles (θ) with respect to the flow. These data were taken at angles from -36° to +36° in 6° steps.

Since small differences in the velocities measured by the wires can translate into large gradients because of the compact size of the probe, improved calibrations were obtained by using one of the straight wires rather than the pressure transducer as a velocity reference. This was accomplished by first fitting A,B,n values to the two straight wires for all angles, then selecting the wire with the minimum standard deviation (based on velocity) and using the resulting

coefficients for that wire along with the calibration data to generate the calibration velocities for the other three wires of the probe. Calibration constants were then determined for all wire and angle combinations using the new velocities.

The variation in the hot wire response with respect to flow angle was modeled by defining a voltage ratio (as follows:

$$\zeta = E(\gamma) / E(0) \tag{3}$$

where $E(\gamma)$ is the hot-wire voltage at the probe angle γ and E(0) is the hot-wire voltage at the probe angle of 0. This function is non-linear and strongly speed dependant. At any given speed the function can be modeled as a polynomial. Since the function has an inflection around $\zeta=1.0$, it is advantageous to redefine the voltage ratio as an offset value:

$$\eta = E(\gamma) / E(0) - 1.0$$
 (4)

which allows γ to be accurately modeled as a rational polynomial of the form:

$$\gamma = c_5 \eta^5 + c_4 \eta^4 + c_3 \eta^3 + c_2 \eta^2 + c_1 \eta + c_0$$
 (5)

where $C_5, C_4, C_3, C_2, C_1, C_0$ are fitted coefficients. Typical rms values of this fit are 0.3°. Representative calibration data and fitted

curves are shown in Figure 17.

Since equation 5 is a strong function of velocity, see Figure 17, a separate set of coefficients were determined at 51 discrete speeds equally spaced over the range from the minimum to the maximum calibration speed. The η value at each speed and angle is computed from calculated voltages using the A,B,n values for the wire at that angle and the arbitrary speed.

2.4.2.2 Processing

2.4.2.2.1 Determination of the u,v components

The x and y velocity components of the flow (u and v) can be computed by knowing the velocity magnitude in the xy plane, and the indicated velocity from one of the slant wires. The velocity magnitude was taken as the average of the indicated velocities from the two straight wires, Q_3 and Q_4 . Once this velocity had been determined, the flow angle γ could be computed from either of the slant wires. In practice the angle was computed using both of the slant wires, and this angle was compared to the calibrated angle range. If the indicated angles were both within the calibrated range, $(-36^{\circ} < \gamma < +36^{\circ})$, the average is used. If only one computed angle was outside of the calibration range the value which lay within the calibration range was used. If both angles lay outside the calibration range the $\gamma = f(\eta)$ polynomial for the wire most normal to the flow was extrapolated to yield the angle, and the point was marked as suspect.

Since the response of the vertical wires does, to a slight degree, depend on the flow angle, two calculations were made for each wire at each point in the data set. For the second calculation the angle information from the first calculation was used to determine the calibration constants $A(\gamma)$, $B(\gamma)$, and $n(\gamma)$ to be used in the determination of Q_3 and Q_4 .

2.4.2.2.2 Accuracy

The accuracy of the processing algorithm was verified for each set of experimental data by processing time series data taken in the free stream during calibration. In all cases the computed flow angles were within 0.5° of the physical probe angle.

The validity of the extrapolations of the η = $f(\gamma)$ relation were verified by taking time series data in the calibration stream at probe angles with respect to the flow direction of $\pm 6^{\circ}$ beyond the normal calibration range. The extrapolated values, so computed, were accurate to within $\pm 1.0^{\circ}$.

2.4.3 Phase Averaging

Phase averaged data acquisition was performed by sampling both the analog input channels of interest and the conditioned phase signal from the forcing mechanism optical pickup at a high data rate. The resulting time series was then divided into intervals based on the pickup signal. Each of these intervals, representing one forcing

period, was then divided into 16 equally spaced intervals and the phase average sample extracted from the time series at these points. As an example consider a block of data where the leading edge of the pickup signal occurred at data points 1 and 384. Dividing the forcing period into 16 intervals, only points 1, 25, 49... would be saved; corresponding to phase locations of 0., 22.5, 45.0... degrees.

For this study, data were taken at 5000 samples per second, and the mean forcing period was 62 milliseconds. This gives an uncertainty of ± 0.6 degrees in any specific phase value due to the sampling rate. Since the subdivision of the intervals over which the phase averaging was performed was based on one revolution of the arm, uncertainties due to long term, (time scales greater than one forcing period) variations in motor speed were eliminated. In addition this method allowed for accurate monitoring of the actual motor speed, since the length of each period sampled is also saved. For all of the data presented in this thesis, the variation in the periods was on the order of the sampling time of 0.2 milliseconds, or 0.3% of the mean period.

CHARACTERIZATION OF THE EXPERIMENTAL CONDITIONS

3.1 Boundary Layer

3.1.1 Bleed setting procedure

The boundary layer formed during the final contraction was removed through a bleed slot as shown in Figure 5. The initial attempt at a setting for the bleed port flow rate was accomplished visually by using tufts at the bleed port; those observations proved difficult to interpret with the desired precision. In an attempt to achieve a better bleed setting, velocity profiles were taken just upstream of the bleed slot using a single hot-wire probe. The bleed flow was then adjusted to yield a locally symmetric velocity profile about the leading edge of the splitter plate. Upon examination of the boundary layer profiles at the separation lip, it was found that this approach yielded too large a bleed flow, and a distorted downstream velocity profile.

The final approach taken to set the bleed flow was to adjust the bleed flow rate such that the an optimum turbulent boundary layer profile was obtained at the separation lip.

3.1.2 Turbulent Characteristics

3.1.2.1 At separation

The boundary layer data were plotted in law of the wall coordinates, \textbf{U}^{+} and \textbf{Y}^{+} ;

$$\mathbf{U}^{+} = \frac{\mathbf{u}}{\mathbf{U}_{\tau}} \tag{6}$$

$$y^{+} - \frac{yU_{\tau}}{\nu} \tag{7}$$

$$\mathbf{U}_{\tau} - \mathbf{U}_0 \begin{bmatrix} \mathbf{C}_{\mathbf{f}} \\ 2 \end{bmatrix}^{1/2} \tag{8}$$

The local skin friction coefficient ($C_f = \tau_w/0.5 \rho U_0^2$) was determined from a Clauser [Clauser 1951] plot. The momentum thickness, θ was determined from

$$\theta = \int_0^\infty \frac{\overline{u}}{\overline{U}_0} \left[1 - \frac{\overline{u}}{\overline{U}_0} \right] dy \tag{9}$$

and the displacement thickness, δ^* was determined from

$$\delta^* = \int_0^\infty \left[1 - \frac{\overline{u}}{U_0} \right] dy \tag{10}$$

Clauser plots for the separating boundary layer are presented for the unforced case in Figure 18 and for the forced case in Figure 19. The resulting C_f values were 2.95×10^{-3} for the unforced case and 3.03×10^{-3} for the forced case. The unforced boundary layer had a momentum thickness at separation (θ_0) of 6.72 mm, with a displacement thickness δ^* of 9.11 mm, yielding a shape factor of 1.36. For the forced condition θ_0 was equal to 6.02 mm and δ^* was equal to 8.21 mm yielding a shape factor of 1.36. U_f at separation was 0.485 for the unforced condition and 0.492 for the forced condition. In addition turbulent intensity measurements in the boundary layer yielded a maximum value for u'/U_f equal to 2.65 in the unforced case.

Mean profiles for the separating boundary layer, for both the unforced and forced condition, were plotted in law of the wall coordinates (u^+,y^+) [Coles 1962] as shown in Figure 20. As indicated in the figure, the data show very good agreement with the law of the wall,

$$U^{+} = 5.6 \log_{10} y^{+} + 4.9 \tag{11}$$

over the log law region. This agreement, along with a shape factor of approximately 1.4 and a u'/U_{τ} value of approximately 2.5 indicate an equilibrium turbulent boundary layer [Hussain 1983].

3.1.2.2 Prior to separation

The momentum thickness θ and friction velocity (U_{τ}) for the developing boundary layer are shown in Figure 21 and Figure 22. As indicated in Figure 21 the boundary layer follows the expected pattern of growth up to a streamwise location of x/θ_0 = -1.0. A decrease in the momentum thickness is indicated at the separation lip; this effect is presumably due to acceleration at the separation lip.

The boundary layer growth rate, $(d\theta/dx)$, can be related to the wall friction coefficient for an equilibrium boundary layer as:

$$c_{f} = 2 \frac{d\theta}{dx} \tag{12}$$

This comparison was made with the experimental data over the range $-30 < x/\theta_0 < -1.0$ and found to be in poor agreement. Given the limited streamwise span of the data, accurate resolution of $d\theta/dx$ would have required a determination of θ to a precision not possible with the experimental configuration used. The uncertainty in the determined θ values is hypothesized to be the cause of the poor agreement of the data applied to (12).

3.2 Forcing system

3.2.1 Forcing frequency

The forcing frequency for this study was chosen based on the prior work of Mensing and Fiedler [1985]. Their studies showed a maximum intensity of \tilde{v} at a saturation length X_s , defined as $X_s = f/U_0$, approximately equal to 1. The forcing frequency used in this study, 16.2 Hz, was chosen based on this criteria to give a saturation location of 0.8 m, or 30% of the test section length. The resulting Strouhal number based on the separating boundary layer thickness, $(f\theta_0/U_0)$, was 0.0081. The natural frequency of the shear layer, as exhibited by fluctuations in the entrainment field, was 3.5 Hz or $f\theta_0/U_0 = 0.0018$; see Foss et.al. [1987].

The data sampling and processing method provided data on every forcing period taken during this study. The rms fluctuations of the period were below the measurement uncertainty involved in the sampling (0.2 msec).

The frequency domain content of the forcing system was examined by placing piezo-electric accelerometers on the forcing piston at a variety of locations. Power spectra of the measurements taken at the piston center, and either extreme end are shown in Figure 23 through Figure 25. As indicated the piston motion has little harmonic content at the center of travel. A small amount of energy is found in

harmonics at either end; presumably these are a result of minor deflections of the forcing piston.

3.2.2 Effect of the forcing on the flow

An accurate determination of the forcing level, by a given forcing apparatus, is one of the major problems in experimental work on forced flows. For the present study, two approaches were taken to accurately quantify the effect of the forcing on the separating boundary layer. Measurements were made with no primary flow in order to isolate the effect of the piston forcing on the air mass in its neighborhood, and measurements were made in the separating boundary layer under nominal test conditions.

3.2.2.1 $U_0 = 0$ Data

Both velocity and pressure measurements were made in the neighborhood of the separation lip with no mean flow. Velocity measurements were made using a single wire hot-wire anemometer; pressure measurements were made utilizing a microphone and pinhole chamber arrangement.

For the hot-wire measurements, calibrations were performed using a drop-test calibration technique; see appendix Appendix B for more information on this technique. The wire was calibrated in the data taking orientation, (with respect to the gravitational field), in order to minimize the error introduced by the natural convection field

of the hot-wire. The results of the hot-wire measurements are presented in Figure 26 through Figure 29; the velocity data presented therein are in units of meters per second, and the coordinates are non-dimensionalized with respect to the piston width (\mathbf{w}_p) . As expected, there is a strong shadow effect of the separation lip. Results for $\mathbf{x}>0$ suggest a strong jet pumping effect which generated a mean entrained velocity in the -y direction.

The technique used for the pressure measurements is documented in Appendix C, and tabular results are presented in Appendix D. The data showed no significant change in the amplitude of the rms pressure fluctuations over the measurement domain; the technique used apparently registered the acoustic wave generated by the piston.

3.2.2.2 Perturbations of the separating boundary layer

characterized The forcing amplitude can Ъe by non-dimensional velocity measures; the rms velocity of the piston, the magnitude of the imposed velocity in the direction of piston motion, or the velocity change at some point in the separating boundary these velocities be all of Specifically, layer. non-dimensionalized with respect to the free stream velocity. forcing levels for the current study were large with respect to the prior work of Disimile [1984], and corresponded to the larger amplitudes used by Fiedler and Mensing [1985]. Specific levels are shown in Table 1.

Table 1 - Forcing Amplitude Measures

Forcing Measure	Amplitude
v _{piston} /U ₀	0.021
v _f /U ₀	0.015
$(\tilde{v}_{f}^{2} + \tilde{u}_{f}^{2})^{1/2} / U_{0}$	0.045

As would be expected, there is some attenuation from the piston face velocity to the induced v velocity (v_f) in the separating boundary layer. The large difference in the maximum velocity change in the flow $((\tilde{\mathbf{v}}_f^2 + \tilde{\mathbf{u}}_f^2)^{1/2}/\mathbf{U}_0)$ relative to the magnitude of the induced v velocity $(\tilde{\mathbf{v}}_f/\mathbf{U}_0)$ should be noted.

If the physical size of separating boundary layer is relatively small, for example θ_0 = 1.14 mm in the Fiedler and Mensing [1985] study, hot-wire velocity measurements are limited to those which can be made with a single wire probe. Since a single wire probe resolves a planar velocity magnitude, an important distinction should be made between the total induced velocity change and the induced velocity change in the transverse direction; the former being larger due to steerage of the sharp velocity gradient near the wall. As indicated in Table 1, for the present study the ratio of total to transverse induced velocity fluctuation was 3 to 1.

Due to the small physical size of the separating boundary layer in other studies magnitudes are often expressed using the former measure since only single hot-wire probes can be utilized. This

should be clearly delineated from the magnitude of the induced v velocity, the former being much larger in magnitude due to steering of the sharp velocity gradient near the wall.

3.3 Entrainment

The throttle plates were adjusted to give a "natural" shear layer, or $dU/dX \simeq 0.0$. The value of dU/dX was determined from measurements of \overline{u} in the high speed nonvortical flow at two streamwise locations as indicated in Figure 30. The resulting value of dU/dX represented a velocity defect over the indicated range of less than 1% of the free stream velocity.

3.4 Probe Positioning

Determination of the probe position for the data taken in the boundary layer and near the separation point for the shear layer is critical due to the steep velocity gradients in the Y direction.

A preliminary attempt to verify the wire location by heat transfer to the wall was attempted. However, due to the minimal thermal effect provided by the wall it proved to be difficult to approach the wall close enough to get an accurate position and still not come in physical contact with the wall. A number of calibration tests showed that coming in contact with the wall, even slightly, altered the characteristics of the wire; see Appendix A.

The final positioning method used in the case of the straight wires for the boundary layer and near separation point data was an optical one. A point light source was used to illuminate the wire at an angle of approximately 14 degrees. When the wire was near the wall it then cast a shadow which could be measured through use of a sighting device viewing normal to the wall. This allowed the wire to be accurately positioned to 0.2 mm from the wall surface. In each case the wire was placed slightly closer to the wall than this, then the traverse was driven so as to move the wire away from the wall until any mechanical play in the traversing system had been taken up. The amount of play was nominally .2 mm.

For positioning of the compact vorticity probe the wall shadow approach could not be used due to the construction of the probe. For the runs using the compact vorticity probe, the probe was positioned by placing it directly behind the separation step at X = 5. mm and Y = 0. mm. The Y location was ascertained by means of a sighting device positioned directly downstream of the separation point.

4

RESULTS AND DISCUSSION

4.1 Response of the upstream boundary layer to the forcing input

Mean velocity distributions, $\overline{u}(y)$, were obtained in the boundary layer region for $-30 \le x/\theta_0 \le 0$. These data were evaluated using the Clauser chart technique (Clauser [1954]) to determine the wall shear stress; see Figure 22. As shown in Figure 20, the mean velocity profile at the separation point for the forced and unforced conditions were only slightly different. However, at x/θ_0 = -5 the mean profiles for the forced and unforced conditions were essentially the same; see Figure 31. The effect of the forcing at x/θ_0 = -5 was, however, still visible as a difference in the phase averaged values; see Figure 32. Farther upstream, at x/θ_0 = -10, the effect of the forcing is minimal; see Figure 33.

- 4.2 The Velocity Field in the Neighborhood of the Separation Lip
- 4.2.1 Mean velocity profiles for the unforced condition

Velocity distributions for the forced and unforced conditions, u(y) and v(y), were obtained for the separating flow at $x/\theta_0 = 1$ and $x/\theta_0 = 3$; see Figure 34. The mean velocity profile of the transverse velocity component for the unforced condition, $\overline{v}(y)$, is presented in Figure 35. As indicated in the figure, the transverse velocity has a mean positive value near y = 0, and the magnitude is greater at $x/\theta_0 = 3$ than at $x/\theta_0 = 1$. This behavior is apparently the result of the cavity formed by the piston and bounding plate assembly, which creates a low pressure region on the downstream side of the separation lip.

4.2.2 Mean velocity profiles for forced condition

Mean velocity profiles of the transverse velocity component for the forced condition, $\langle \vec{v} \rangle (y)$, are presented in Figure 36 through Figure 39. Also shown for reference on these figures is the physical geometry of the forcing piston for the indicated phase condition. As indicated in Figure 36, at $\phi = 0^{\circ}$ the piston is fully extended towards the flow, $\langle \vec{v} \rangle$ is larger than the unforced case, and the difference is more pronounced at $x/\theta_0 = 3$ than at $x/\theta_0 = 1$. As the piston retracts through $\phi = 90^{\circ}$ to $\phi = 180^{\circ}$, Figure 37 and Figure 38, the difference between $\langle \vec{v} \rangle$ and \vec{v} is increased. At $\phi = 270^{\circ}$, Figure 39, the piston is at its maximum velocity in the -y direction and while $\langle \vec{v} \rangle \simeq \vec{v}$ at

 $x/\theta_0 = 1$, there is still a significant increase of \sqrt{v} over \overline{v} at $x/\theta_0 = 3$.

In order to better identify the phase behavior of the forcing on the flow, a velocity difference δu can be defined as:

$$\delta u = \langle u(x,y,\phi) \rangle - \langle u(x,y) \rangle \tag{13}$$

where $\langle u(x,y) \rangle$ is the average over all phase angles.

To clarify the response of the separating shear layer to the forcing input, δu and δv are plotted as a function of the phase angle ϕ ; see Figure 40 through Figure 47. At $y/\theta_0=0$, Figure 40 and Figure 41, δu is much larger than δv as a result of the lateral displacement of the fluid with a large velocity gradient. At $y/\theta_0=-1$ δu has decreased with respect to δv and the difference between δu at $x/\theta_0=1$ and at $x/\theta_0=3$ has been reduced. At $y/\theta_0=-3$ the magnitudes of δu and δv are approximately equal and show little change from $x/\theta_0=1$ to $x/\theta_0=3$. In the outer edge of the forming shear layer, $y/\theta_0=-9.5$, δu is nearly zero while δv indicates a strong influence of the forcing. These data suggest a lateral displacement of the separating boundary layer in the ty direction by the action of the forcing. This hypothesis leads to the definition of the quantity ξ , defined as

$$\xi = \frac{\delta u}{\delta \bar{v}} \frac{d < u >}{dy}$$
 (14)

which was computed for both the $x/\theta_0 = 1$ and $x/\theta_0 = 3$ locations; see Figure 48. For an idealized condition of a lateral displacement of a velocity gradient ξ should be a constant. As indicated in Figure 48, ξ is approximately constant for $1 \le x/\theta_0 \le 8$.

4.2.3 Kinematic Reynolds stress in the separating shear layer

The kinematic Reynolds stress distribution for the separating flow, along with data for an equilibrium turbulent boundary layer (Klebanoff [1954]), are presented in Figure 49. As indicated in the figure there is little change in the high speed region, both the data at $x/\theta_0 = 1$ and $x/\theta_0 = 3$ are in good agreement with an equilibrium boundary layer. In the region $-4 \le y/\theta_0 \le -0.5$ the relaxation of $\overline{u'v'}$ as a result of the removal of the wall is indicated; the increase of $\overline{u'v'}$ in the region $-0.5 \le y/\theta_0 \le 1$ for the evolving shear layer can also be seen.

4.3 Evolution of the unforced and forced shear layers

4.3.1 Mean velocity profiles

Mean and phase averaged velocity data were obtained using single wire measurements for the region $1 \le x/\theta_0 \le 230$. Isotachs for the unforced conditions are presented in Figure 50 and Figure 51, along with similar amplitude results from the Fiedler and Mensing [1985] study. As can be seen from the figures, the strongly forced shear layer exhibits a stepped growth rate, with a plateau at $1.0 < (x-x_s)f/U_0 < 1.5$. It is pertinent to note the qualitative agreement between the current

study, (ie. Figure 51), and the prior work by Fiedler and Mensing [1985], (ie. Figure 52). In the latter case the strong levels of forcing led to a premature separation of the boundary layer which was not present in the current study.

Mean velocity profiles for the single wire data; average unforced, long term average forced, and minimum and maximum phase average forced, are presented in Figure 53 through Figure 65. The trends in these data are most easily seen in the large x/θ_0 data where the differences between the long term averaged forced data and the unforced data, along with the differences between the minimum and maximum phase averaged values of the forced data, are quite apparent. Little effect of the forcing is seen in the mean profiles at $x/\theta_0 = 1$; the gradual evolution between this location and that of $x/\theta_0 = 230$ can be easily traced from the figures.

The minimum and maximum values for the forced condition exhibit a dramatic acceleration and deceleration characteristic on the high speed side of the shear layer in the downstream region; see Figure 60. It is inferred that the accelerated state is similar to the "inviscid acceleration past an obstruction" since the phase averaged velocity values, $\langle \vec{u} \rangle$ are significantly larger than U_0 . The data for the unforced condition (at the same streamwise location as Figure 60), indicate the lack of a similar effect; see Figure 66. The corresponding minimum values for the forced condition are are also inferred to represent pressure effects.

4.3.2 Phase averaged data

The evolution of characteristics in the forced flow field can be readily seen from phase averaged isotachs of the single wire data. Plots of δu (as defined in 13) versus the phase angle ϕ are presented in Figure 67 through Figure 79. The characteristics of these data can be plausibly related to the forcing effects as noted in the following:

- the separation lip, of downstream region a) For $1 \le x/\theta_0 \le 5$, Figure 67 to Figure 69, the positive $(\phi \simeq 120)$ and negative $(\phi \simeq 270)$ locations represent the effects of the piston motion in the +y and -y directions respectively. The primary effect of the forcing at this point is a steering of the large mean velocity gradient; as shown in the figure the influence region is quite limited in the y direction. At x/θ_0 = 5, the appearance of isolated correlation contours in phase space can be noted. For the sake of brevity these will be referred to simply as correlation contours in the following discussion.
- b) For $10 \le x/\theta_0 \le 25$, Figure 70 to Figure 72, the positive and negative correlation contours are better defined and the region of influence is wider. At $x/\theta_0 = 25$ the centroid of the correlation contour is located closer to the high speed side of the shear layer than it was at $x/\theta_0 = 10$.

- c) For $40 \le x/\theta_0 \le 77$ (Figure 73 to Figure 75), the magnitudes of the correlation contours reach a maximum and the formation of correlation contours of opposite sign on the low speed side of the shear layer is first noted. The correlation contours on the high speed side of the shear layer will be referred to as the primary correlation contours, while those on the low speed side will be referred to as the secondary correlation contours.
- d) For $115 \le x/\theta_0 \le 153$ (Figure 76 to Figure 77), the primary correlation contours have migrated farther in the direction of the high speed side; the intensity of the primary correlation contours has continued to decrease, while that of the secondary correlation contours has increased.
- e) For $192 \le x/\theta_0 \le 230$, Figure 78 to Figure 79, the intensity of the primary correlation contours has dropped below that of the secondary correlation contours; the secondary correlation contours the field.

The distinctive feature of the correlation contours allow a convection velocity to be defined at a given downstream location. Specifically the phase shift between the correlation contour peaks at two x/θ_0 locations, see Figure 80, can be related to a time difference using the forcing period as follows:

$$t_2 - t_1 = \left[\frac{\phi_2 - \phi_1}{360} + 360 \text{ n} \right] \times \tau_f$$
 (15)

where n is an integer number of forcing periods. If the data locations are sufficiently close together, as is the case in the current study, n is 0. From this time difference and the spatial distance between the data sampling locations, a convection velocity for the disturbance can be defined as:

$$U_{c} = \frac{X_{2}^{-X_{1}}}{t_{2}^{-t_{1}}}$$
 (16)

Using these procedures, the convection speed was determined for the data locations $x/\theta_0 \ge 15$; see Figure 81. The increasing Ucvalues as function of x/θ_0 are rational considering the previously noted migration of the primary disturbance towards the high speed side of the shear layer.

The width of the disturbance region $\Delta(x)$ can be arbitrarily defined using the integral quantities

$$\Delta^{2} = \frac{\int_{0}^{2\pi} \int_{-\infty}^{\infty} |\delta \mathbf{u}| (\mathbf{y} - \mathbf{y}_{c})^{2} d\mathbf{y} d\phi}{\int_{0}^{2\pi} \int_{-\infty}^{\infty} |\delta \mathbf{u}| d\mathbf{y} d\phi}$$
(17)

where y_c is the centroid of the disturbance field, as defined in (18).

$$y_{c} = \frac{\int_{0}^{2\pi} \int_{-\infty}^{\infty} |\delta u|(y) \, dy \, d\phi}{\int_{0}^{2\pi} \int_{-\infty}^{\infty} |\delta u| \, dy \, d\phi}$$
(18)

The data for Δ/θ_0 as a function of x/θ_0 are presented in Figure 82 along with the growth rates of $\theta(x)$ for the forced and unforced conditions.

Empirically, the growth of the disturbance field can be described as a power law relationship:

$$\Delta/\theta_0 = 0.0063 \ (x/\theta_0)^{1.64} \tag{19}$$

for $0 \le x/\theta_0 \le 60.0$ and as a linear relationship:

$$\Delta/\theta_0 = 0.0784 \text{ x/}\theta_0 - 0.319 \tag{20}$$

for $77 \le x/\theta_0 \le 192$.

The discontinuity of the growth rate at $x/\theta_0 \simeq 60$ is apparently related to the indicated saturation (ie. the peak δu value) at this x location. The indicated linear growth rate is nominally the same as the growth rate of $\theta(x)$ over the same domain.

Fiedler and Mensing [1985] also observed a saturation effect; theirs was defined in terms of the maximum of the transverse velocity components. Defining this streamwise location as \mathbf{x}_{s} , their result showed that for a forcing level which was comparable to that used in the present study,

$$\frac{f(x_s - x_0)}{U_0} \simeq 0.75 \tag{21}$$

where x_0 was defined as a virtual origin. This virtual origin was defined from their data of $x_s = x_s(f)$ at a given amplitude. It was observed that (1/f) is a linearly increasing function of x_s . An extrapolation of this relationship to $(1/f) \to 0$ defined the x_0 value for the given forcing amplitude.

An apparent origin cannot be determined herein since a single frequency was used in the present study. In order to compare the two investigations, it can be assumed that only kinematic effects are represented in the f, $\mathbf{x_s}$, and $\mathbf{U_0}$ relationships and a comparison of the values $(\mathbf{fx_s}/\mathbf{U_0})$ can be made for "equivalent" forcing amplitudes.

The present observations permit the maximum value of

$$\left[\tilde{u}_{f}^{2} + \tilde{v}_{f}^{2}\right]^{1/2} / U_{0} - 0.045$$
 (22)

to be determined at $x/\theta_0 = 1$. Similarly, Fiedler and Mensing [1985] present data from a single hot-wire immediately downstream of the

slot. Their values of (0.065) and (0.0065) bracket those of the present study.

Defining a saturation length for the current study based on the maximum δu values results in a value of x_s = 0.5 m. Hence,

$$\frac{fx}{U_0} = 0.62.$$
 (23)

Using the Fiedler and Mensing [1985] (1/f) $\propto x_s$ results and interpolation for the forcing amplitude parameter, a frequency of 13.2 Hz is estimated for the saturation length of the current study: 0.5 m. The corresponding fx_s/U_0 value is 0.60.

The striking agreement between these two results, in spite of the significant differences in the forcing geometries and in the Reynolds numbers of the separating boundary layers (5500 cf 830), supports the assumption that the forcing process is kinematic in character.

4.4 Response of the entrainment field to the forcing input

Velocity vector measurements of the entrained flow were performed in the region $100 \le x/\theta_0 \le 200$ for both the unforced and forced conditions. The data for the unforced condition and the mean forced condition are presented in the form of a velocity vector plot in Figure 83. As indicated in that figure, there is a noticeable mean steering effect of the entrained fluid beyond the active, (ie. vortical), shear layer. Prior investigations in the same facility, Ali et.al. [1985],

verified a uniform velocity at the exit of the entrainment conditioning section, $10 < x/\theta_0 < 420$, for the unforced condition. The observed mean steering is consistent with other observed data for the facility as discussed in the following.

An evident feature of the isotachs for the forced shear layer is their greater width on the low speed side of the shear layer. clearly suggests that a greater mass flux exists at a given downstream location. Other evidence, however, does not support this interpreta-Specifically, with the fan motor set to a fixed operating speed, it was observed that the free stream velocity of the primary flow (\mathbf{U}_{0}) remained unchanged between the unforced and forced conditions. Since the \mathbf{U}_0 value is dictated by the pressure difference from the atmosphere to the test section and since the constancy of the: i) pressure rise from the receiver (ie., the domain that receives the flow from the test section and delivers it to the fan) to the atmosphere and ii) the fan rpm, dictate a constant operating point on the characteristic curve, it is inferred that the volume flow rate through the fan is a constant. It is therefore concluded that the magnitude of the entrainment flow rate into the test section is not affected by the forcing.

These separate observations can only be compatible if there is a significant steering effect of the entrainment streamlines as shown schematically in Figure 84. Specifically, with forcing, the entrainment fluid is added to the active shear layer and the flux of

vortical fluid at a given x/θ_0 value is larger than that of the unforced case. Similarly, the streamline trajectories of the unforced case deliver a significant volume flow rate of non-vortical fluid past a given x/θ_0 plane, shown as $\beta \hat{m}$ in Figure 84

As a result of experimental difficulties, identified below, quantitative measures of the steering could not be obtained to verify the above hypothesis, However, the qualitative trends of the data are apparent, and they support the proposed flow model of Figure 84.

Previous flow visualization measurements in the entrainment region, Foss [1987], indicated a mean flow angle for the entrained fluid of approximately 60°. Based on this data, quantitative measurements were made in the entrainment region using a compact vorticity probe oriented at an angle of 60°. Additional surveys were made at probe orientations of 45° and 90°. The resulting data indicated a strong steering effect, causing the measured velocity to tend to be aligned with the probe body. This effect could be caused by aerodynamic influence of the probe body, momentum wake effects of the wire support prongs, thermal wake interference between the wires, or perhaps a combination of all three. The exact cause of this effect is not clear at the time of this writing.

5

CONCLUSIONS

A relatively small perturbation of the separating boundary layer evolves into a strong perturbation of the developing shear layer.

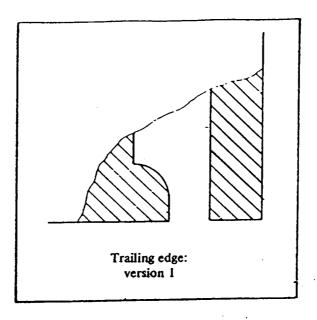
The effect of the forcing on the separating boundary layer for the geometry of the current study is twofold: i) A lateral displacement of the mean velocity profile for $y/\theta_0 > 1$ and ii) an unsymmetrical widening effect for $y/\theta_0 < 0$. For the region $0 < y/\theta_0 < 1$ a combination of these effects is inferred.

For equivalent forcing amplitudes, the qualitative evolution of the shear layer is consistent with the prior work of Fiedler and Mensing [1985]; specifically, quite similar values of (fx_s/U_0) were observed in spite of quite different values of the forcing methods and separation lip geometries.

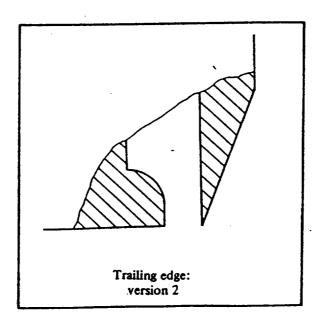
Phase averaged variations (δu) about the mean values of forced flow (δu) exhibit closed contours in phase space. A convection velocity of the closed contours can be computed from the phase shift between two axial locations (see Figure 81). A width measure of the disturbance field can be defined as a moment of δu in phase space (see Figure 82). The apparent motions of the closed contours are consistent with the trends observed for the computed convection velocity.

The entrainment region outside the active shear layer exhibits a mean steering of the flow field for the forced condition relative to the unforced condition. This mean steering is consistent with other observed data for the facility.

The well documented conditions at separation for this study, specifically the detailed measurements of u and v as a function of forcing phase angle, should provide a good test case for numerical simulations.

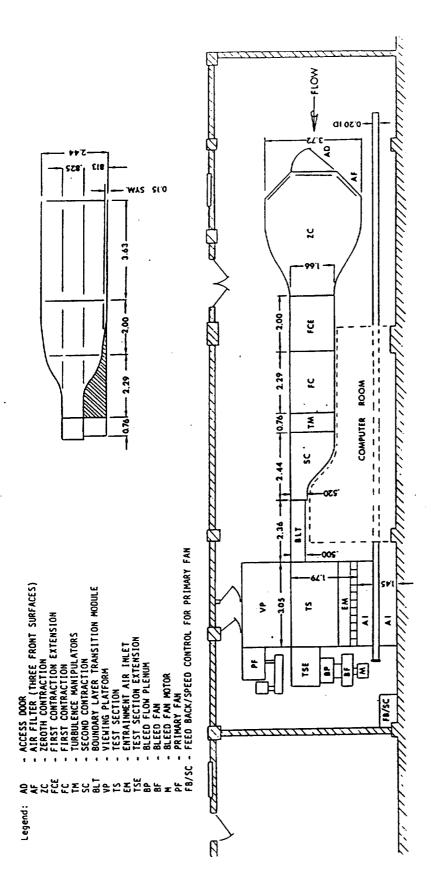


$$R_{\theta} = 830$$



Adapted from Fiedler and Mensing [1985]

Figure 1 - Separation lip geometry for Fiedler and Mensing [1986]



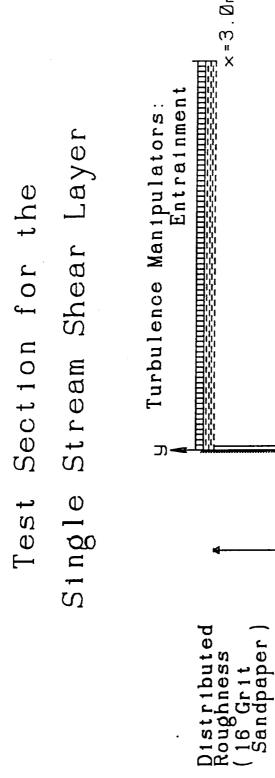
ALL DIMENSIONS ARE IN METERS

DO NOT SCALE

Figure 2 - Plan view of experimental facility

E

1.21



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0.5

Figure 3 - Test section

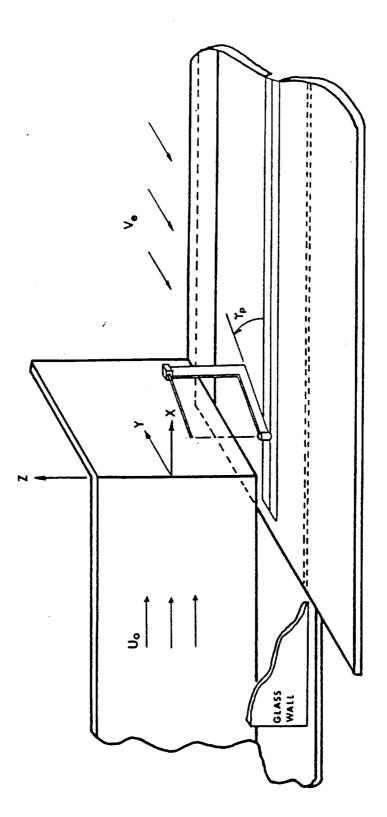
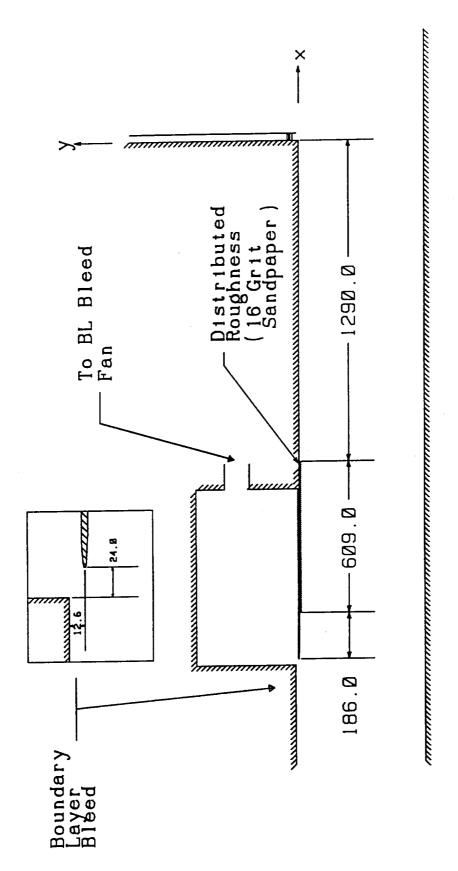


Figure 4 - Schematic Representation of the Traverse System

Adapted from Disimile [1984]



(All Dimensions in mm)

Figure 5 - Boundary Layer Development Section

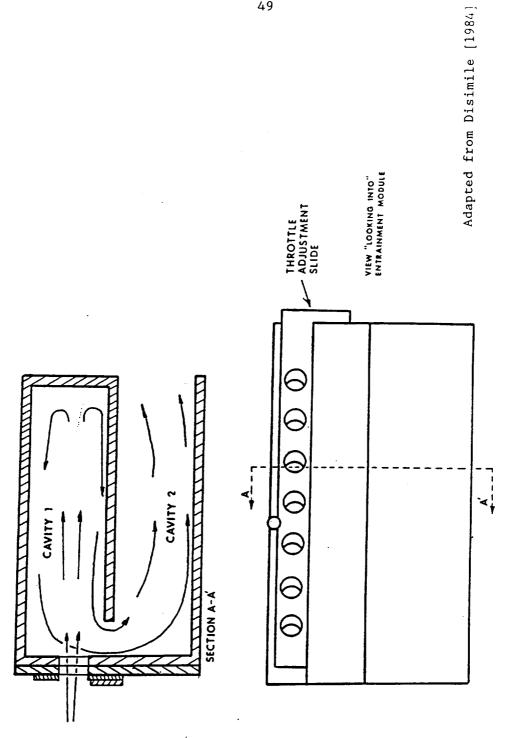
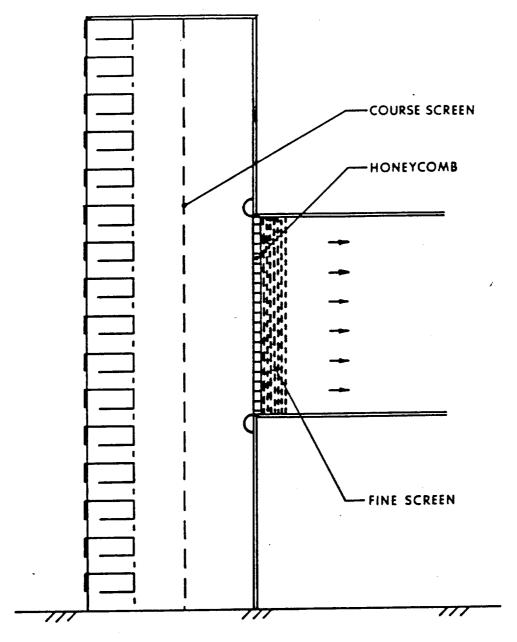


Figure 6 - Entrainment Throttling Chamber Detail



Adapted from Disimile [1984]

Figure 7 - Entrainment Flow Conditioning

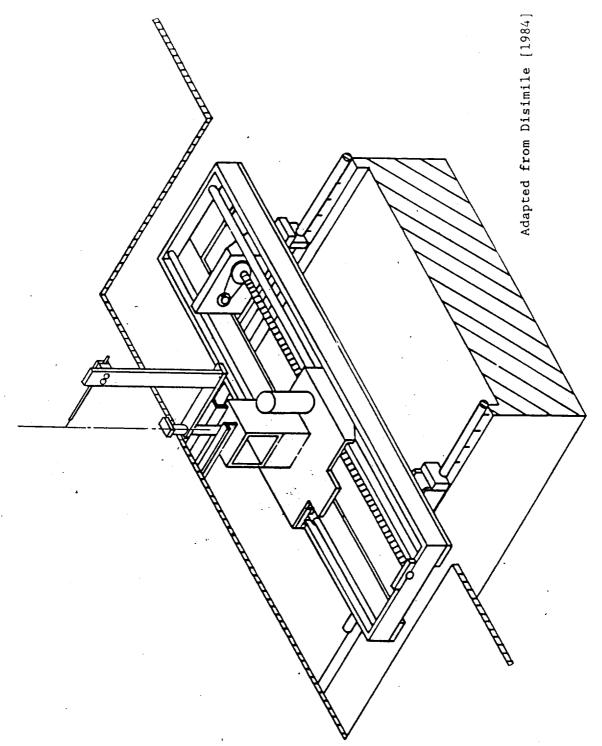


Figure 8 - Schematic Representation of the Traversing Mechanism

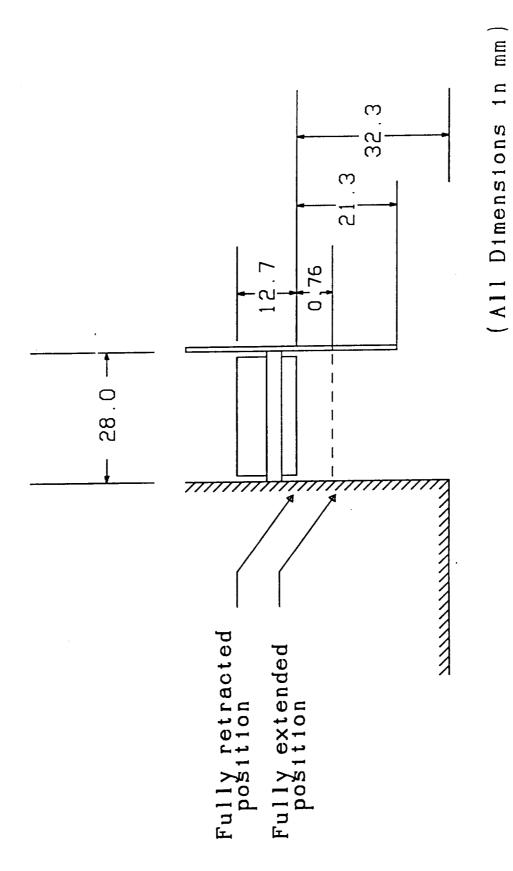


Figure 9 - Forcing Piston Detail

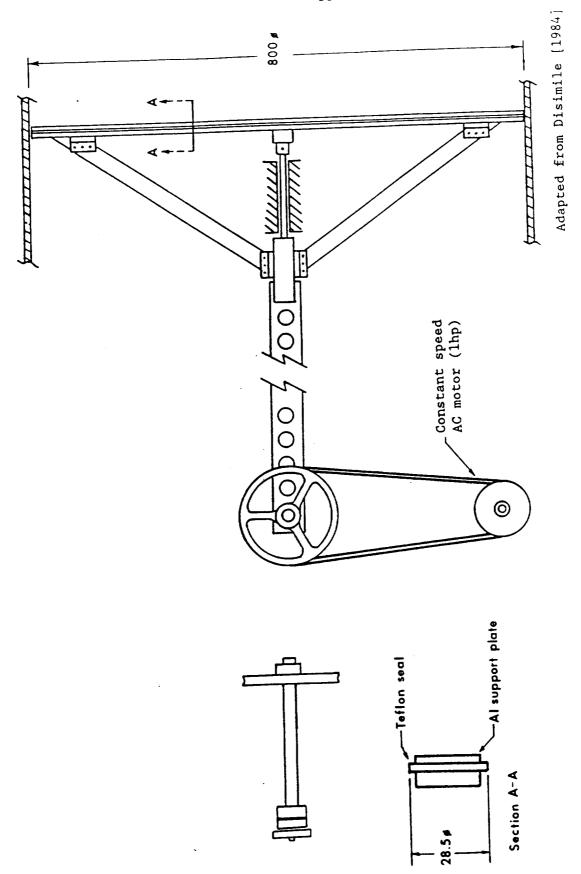


Figure 10 - Forcing Piston Side View

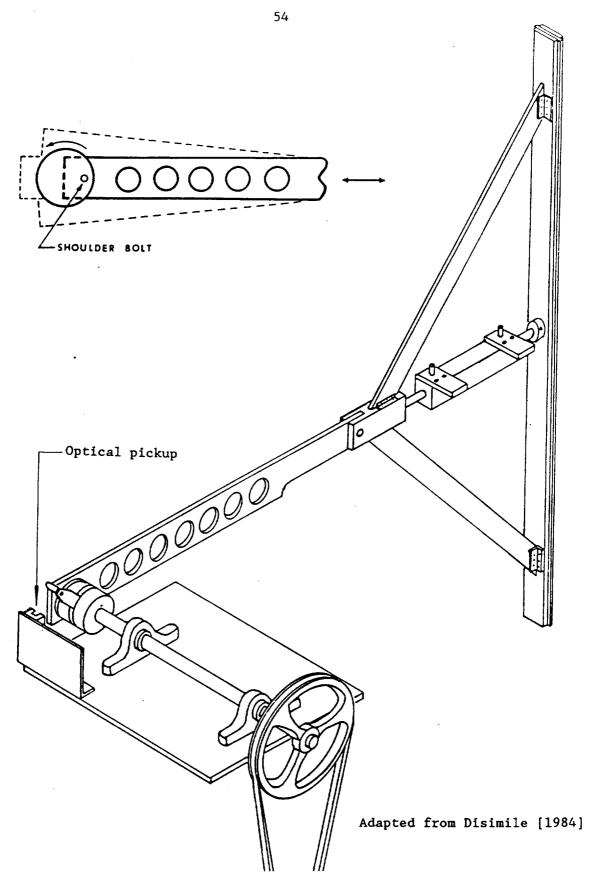


Figure 11 - Forcing Piston Isometric View

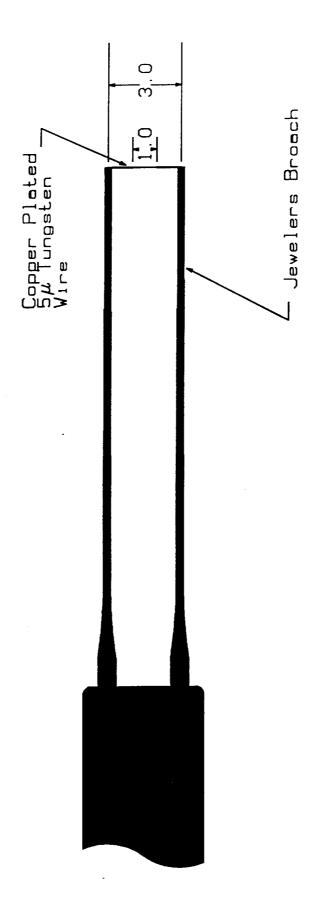
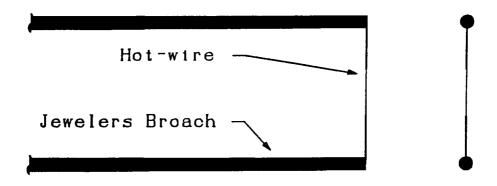
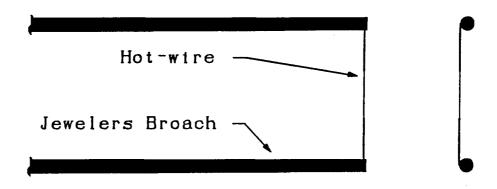


Figure 12 - Typical hot-wire



Normal Wire Mounting



Modified Wire Mounting

Figure 13 - Modified wire mounting for boundary layer surveys

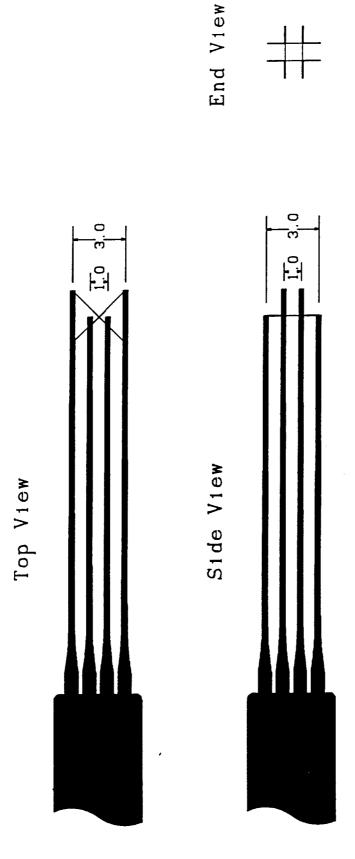


Figure 14 - Schematic presentation of Compact Vorticity Probe

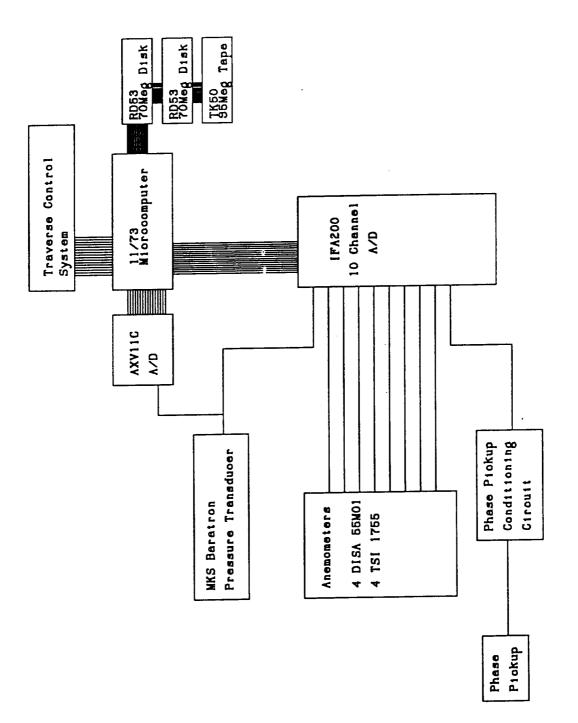


Figure 15 - Data Taking System

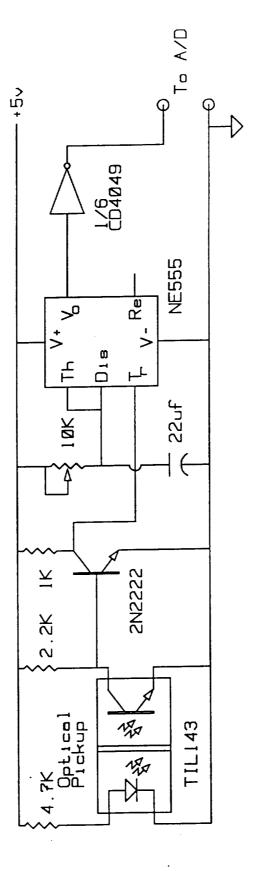


Figure 16 - Optical phase pickup and conditioning circuit

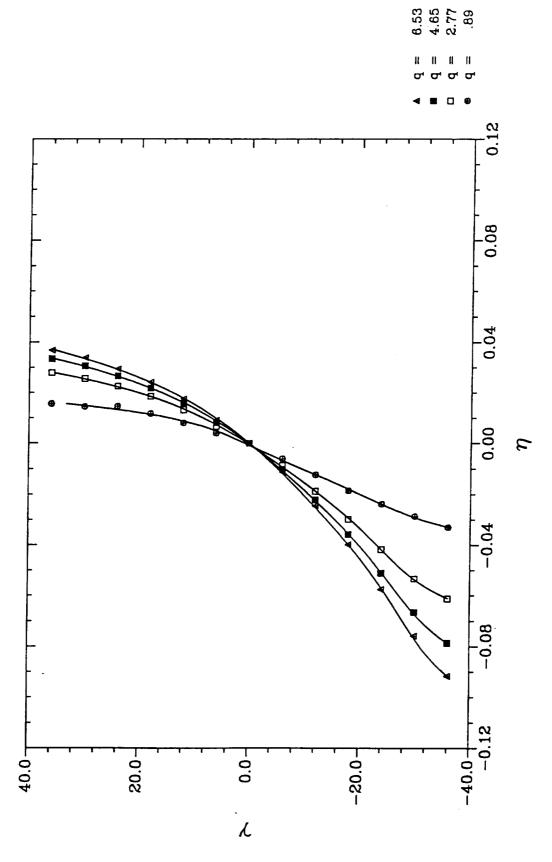


Figure 17 - Raw calibration versus fitted $\gamma = f(\eta)$ curve.

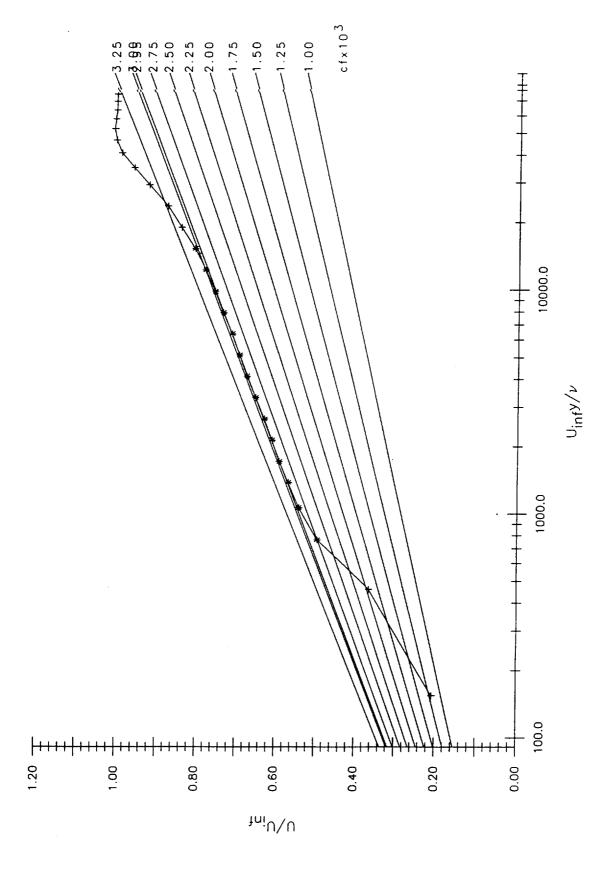


Figure 18 - Clauser Plot of unforced BL at X/θ = 0.0

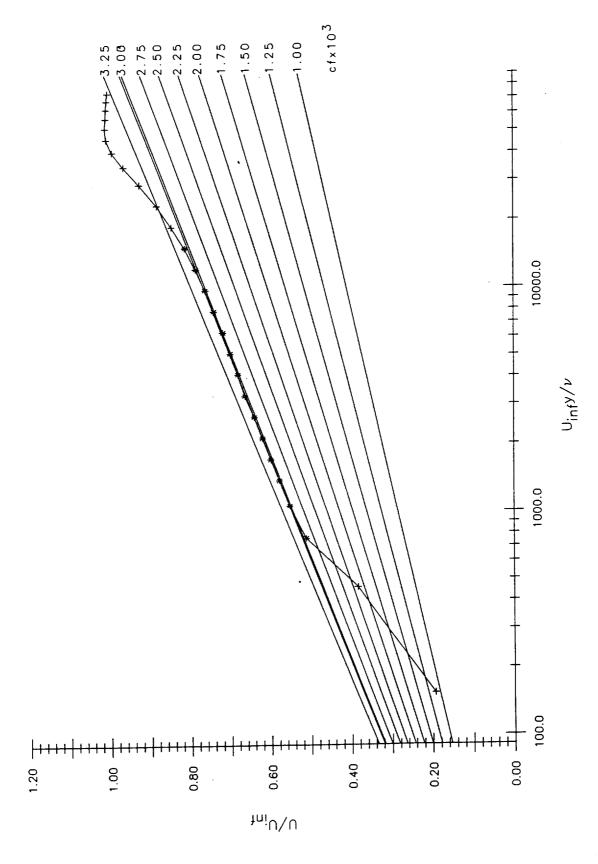


Figure 19 - Clauser Plot of forced BL at X/θ - 0.0

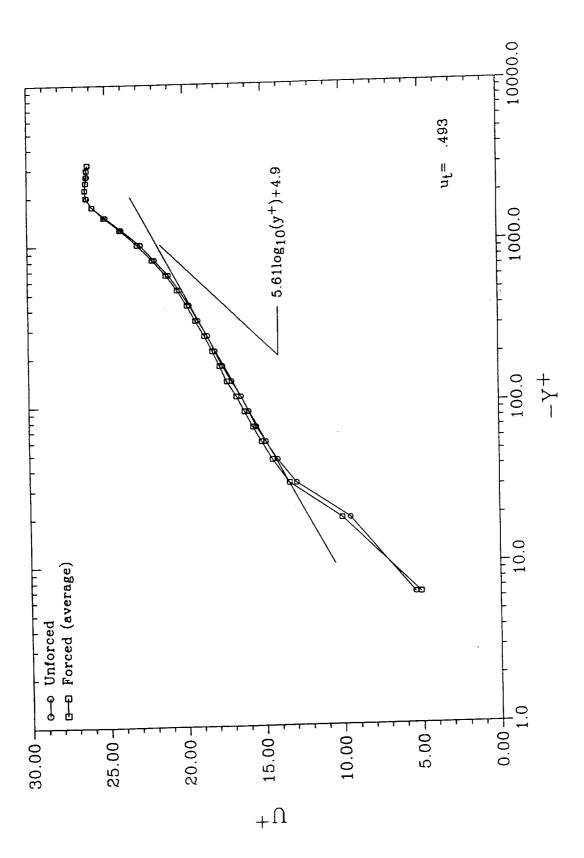


Figure 20 - Boundary layer mean profile at x/θ_0 =0.0

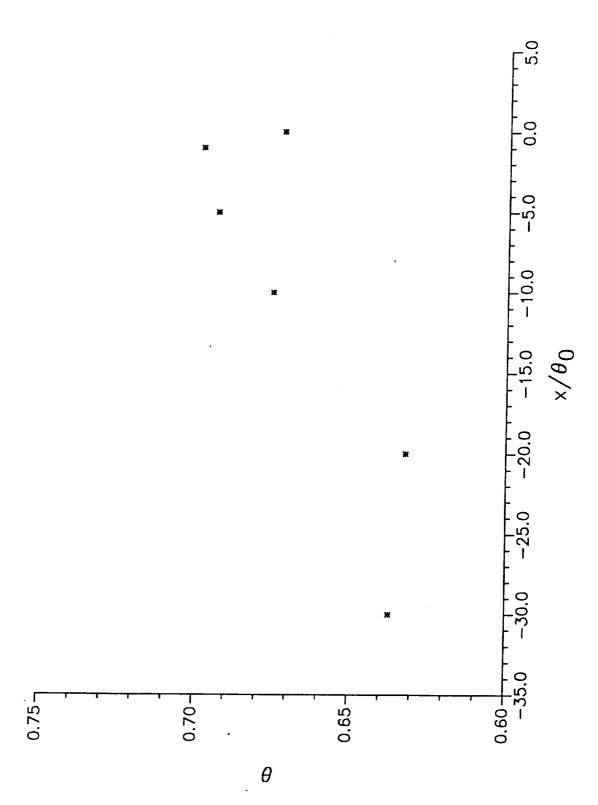


Figure 21 - Boundary layer momentum thickness

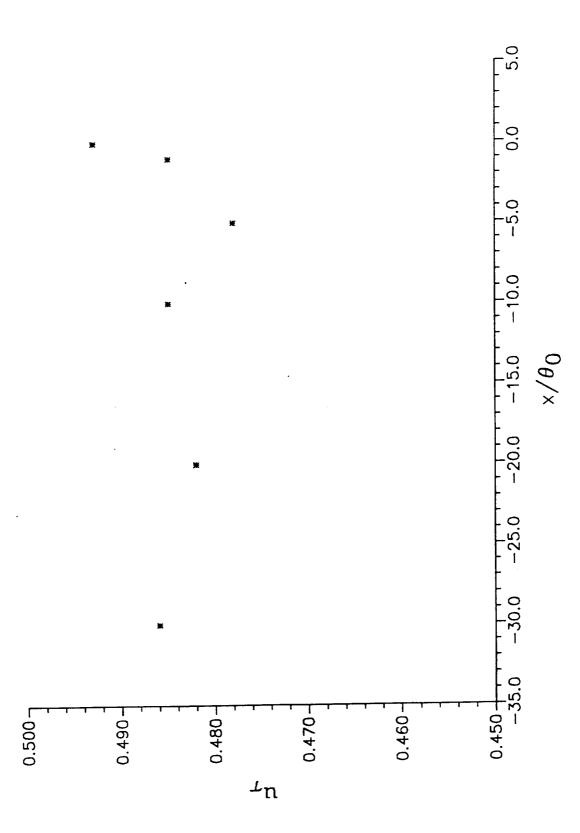


Figure 22 - Boundary layer friction velocity

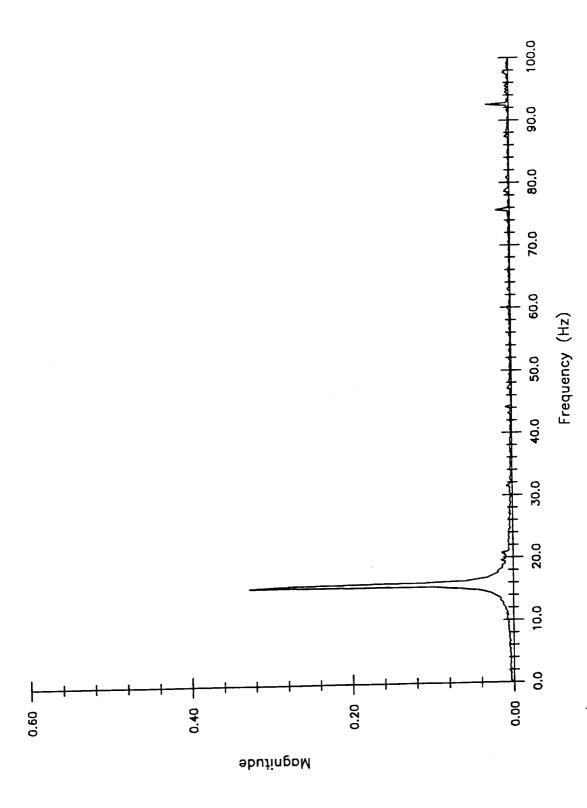


Figure 23 - Power spectrum of piston acceleration (z=0.0)

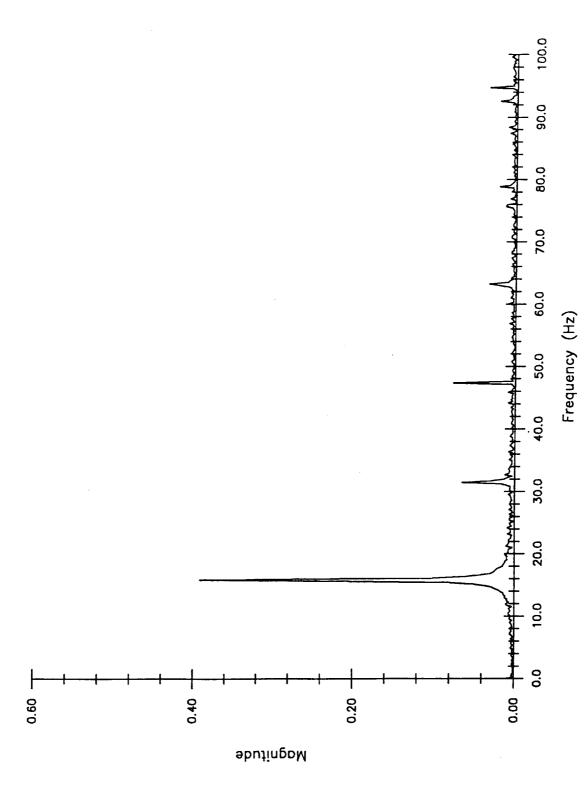


Figure 24 - Power spectrum of piston acceleration (z--h/2)

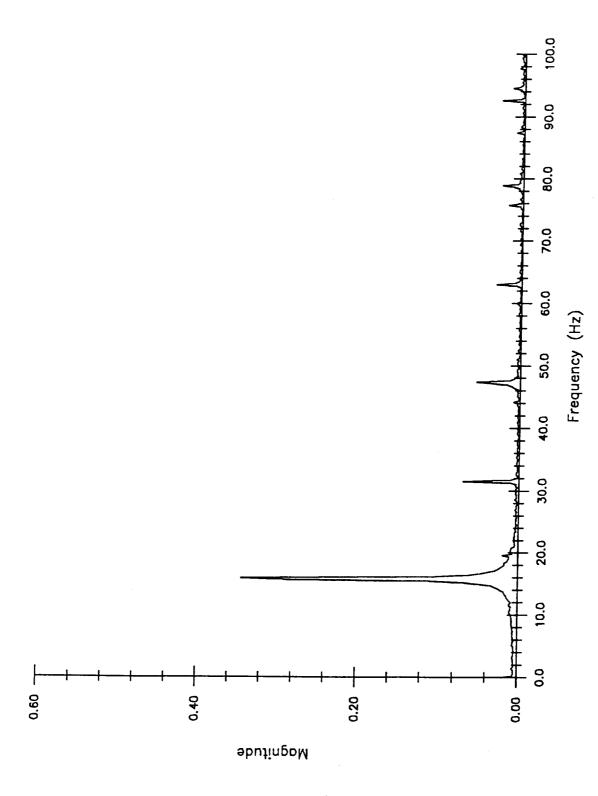


Figure 25 - Power spectrum of piston acceleration (z=+h/2)

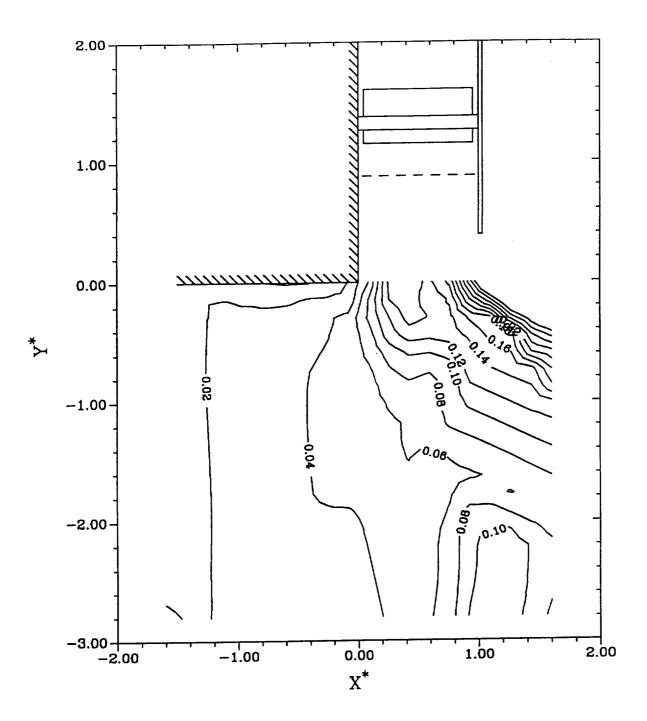


Figure 26 - Hot-wire Response to Forcing with no Flow ϕ = 0

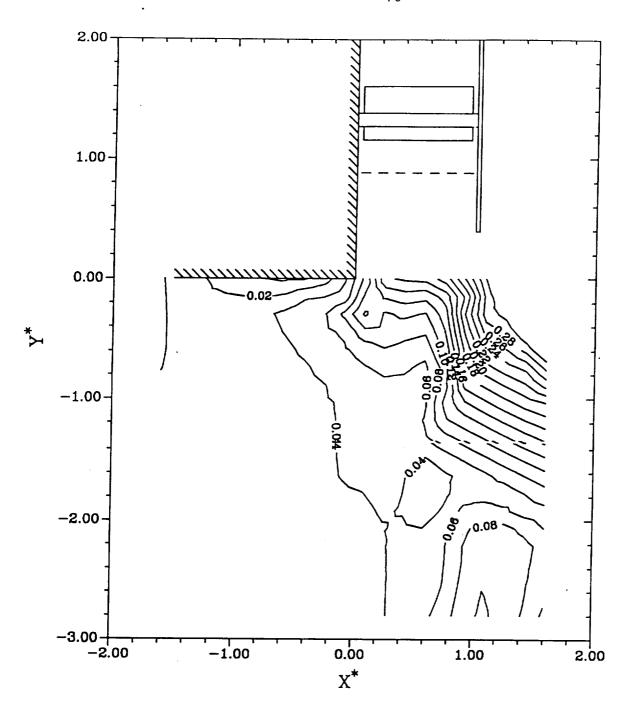


Figure 27 - Hot-wire Response to Forcing with no Flow ϕ = 90

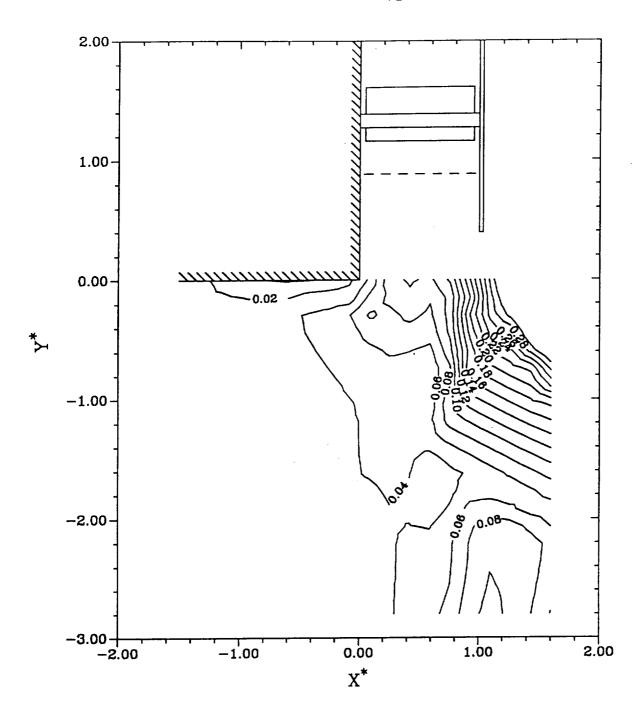


Figure 28 - Hot-wire Response to Forcing with no Flow ϕ = 180

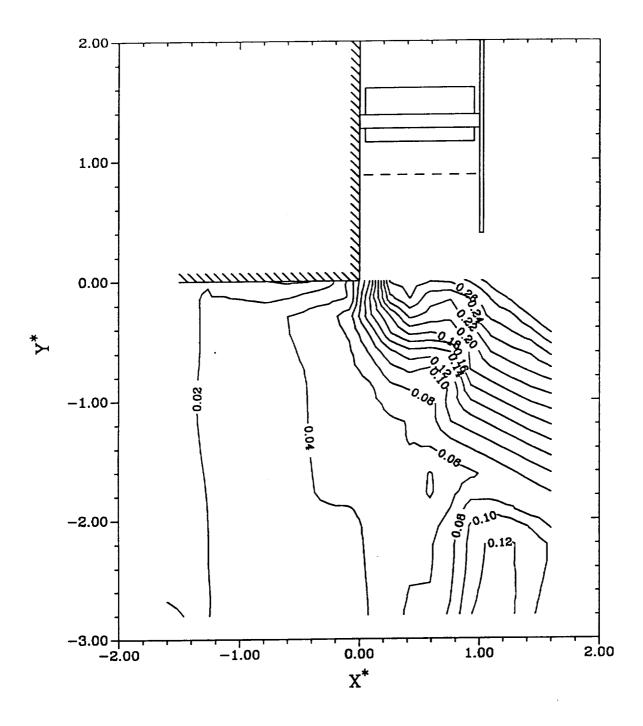


Figure 29 - Hot-wire Response to Forcing with no Flow ϕ = 270

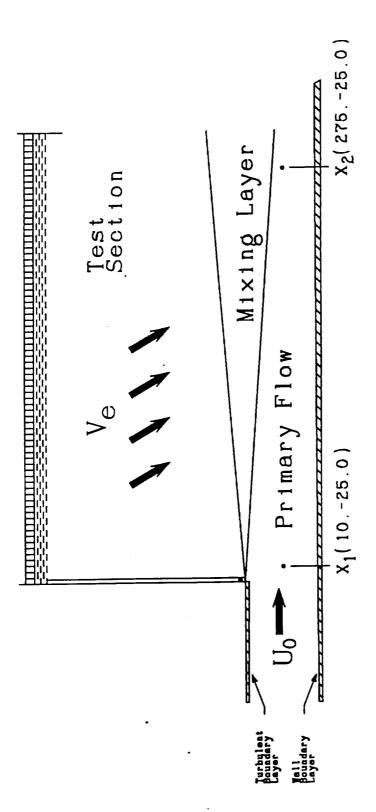
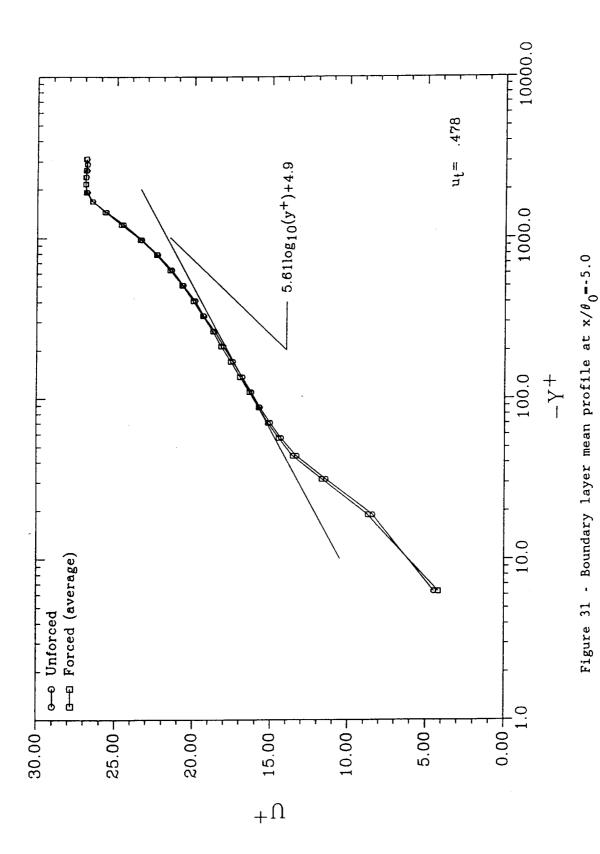
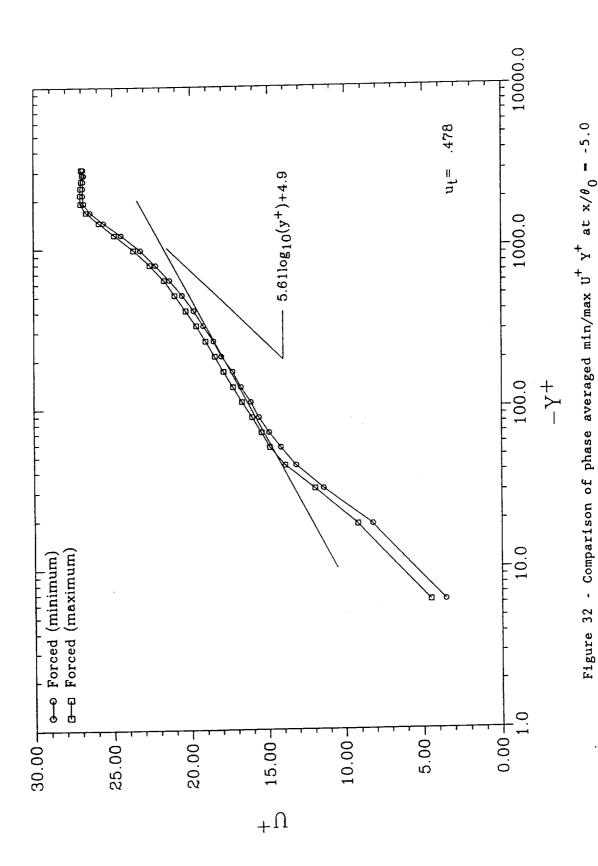
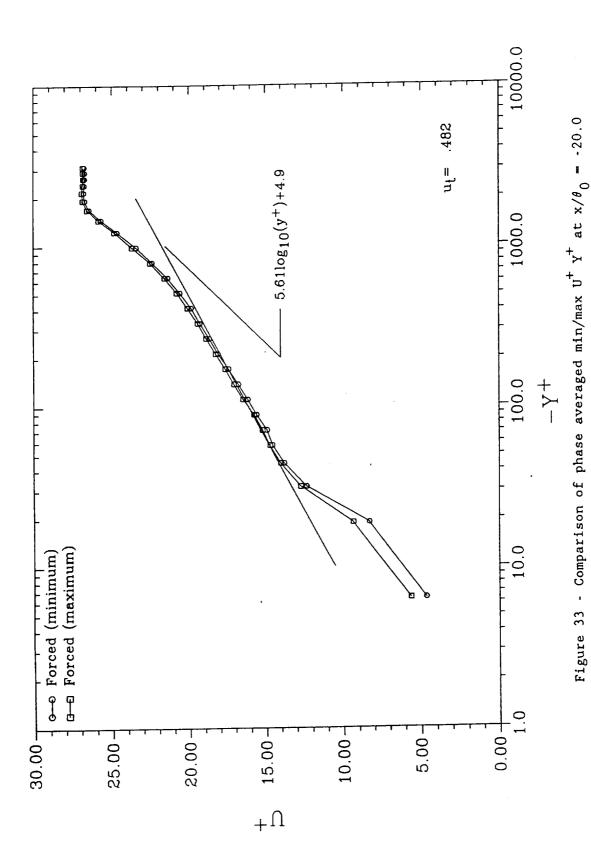


Figure 30 - Entrainment Setting Procedure







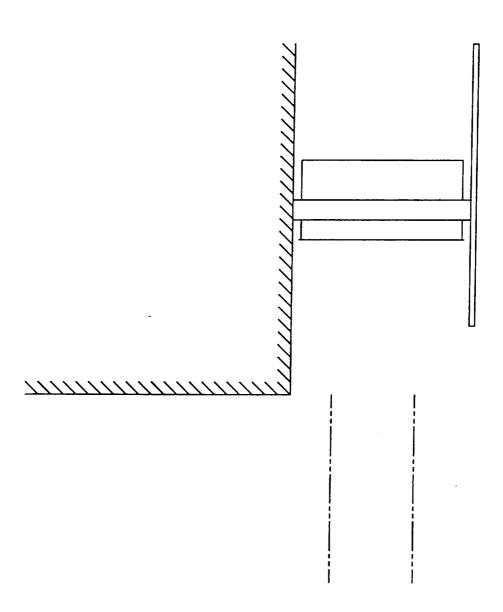
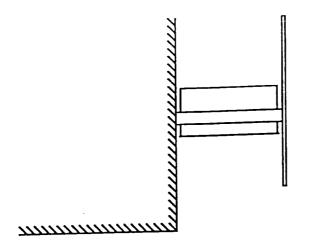


Figure 34 - Streamwise data sampling locations



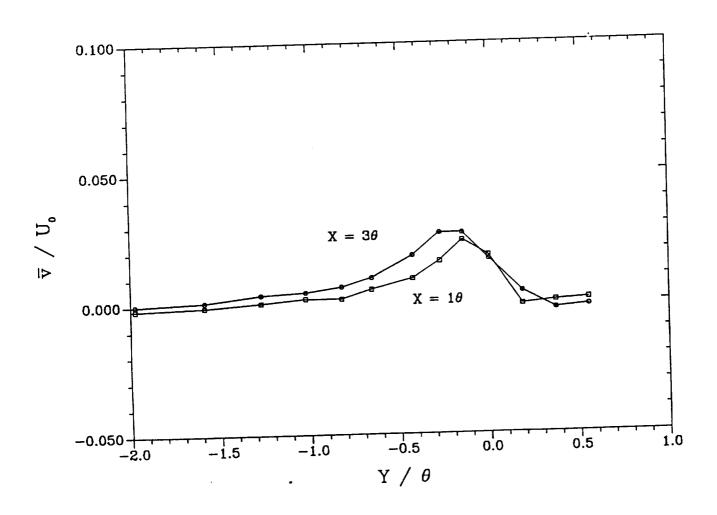
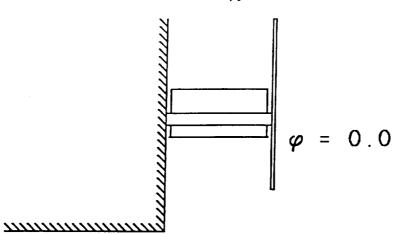


Figure 35 - Unforced $\overline{v}/\overline{u_0}$ in the separating boundary layer



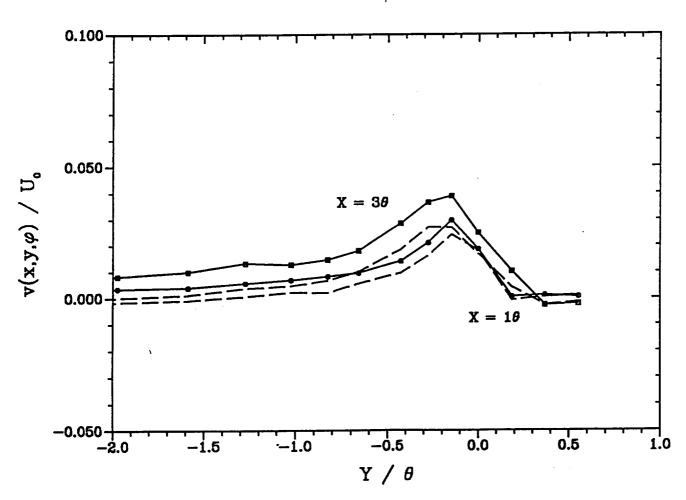
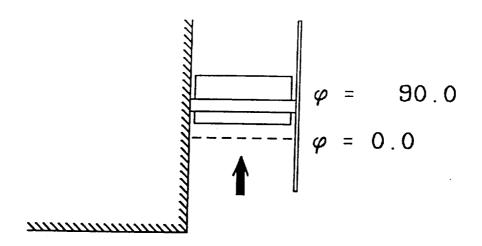


Figure 36 - Phase averaged \bar{v}/U_0 at ϕ =0.0



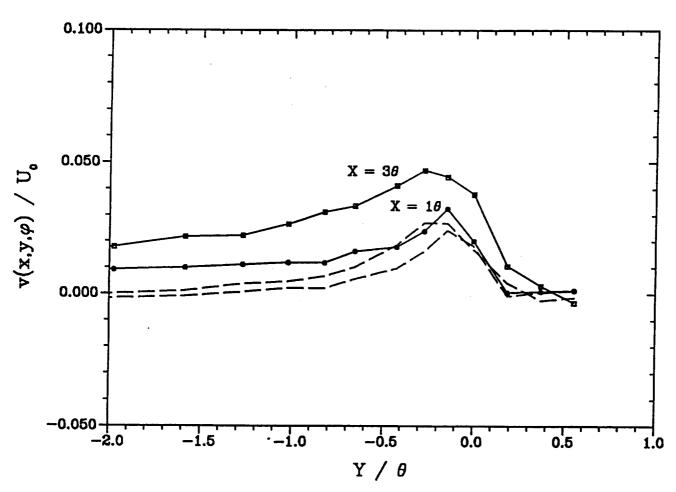
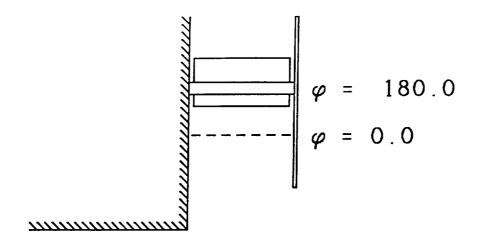


Figure 37 - Phase averaged \overline{v}/U_0 at ϕ =90.0



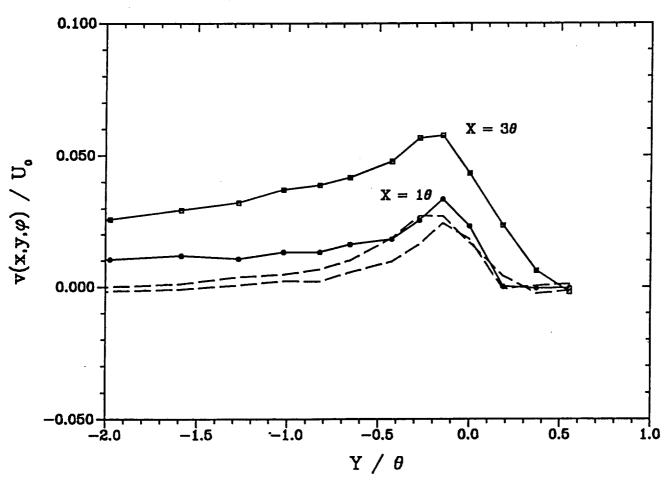
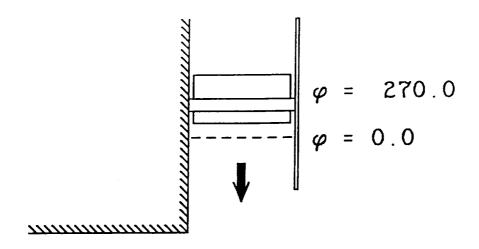


Figure 38 - Phase averaged \overline{v}/U_0 at $\phi=180.0$



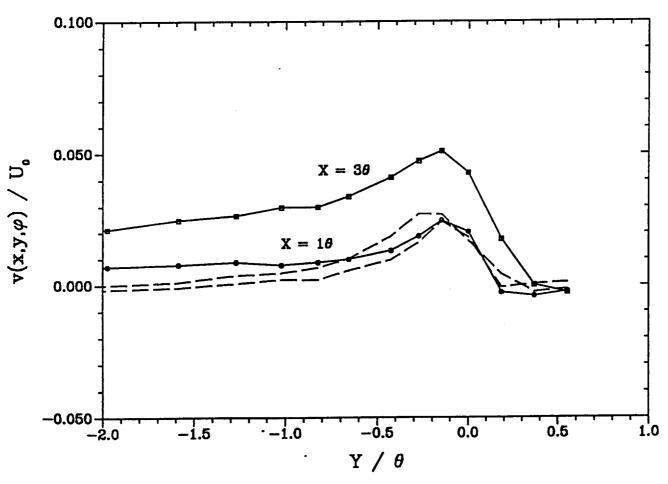


Figure 39 - Phase averaged \overline{v}/U_0 at $\phi=270.0$

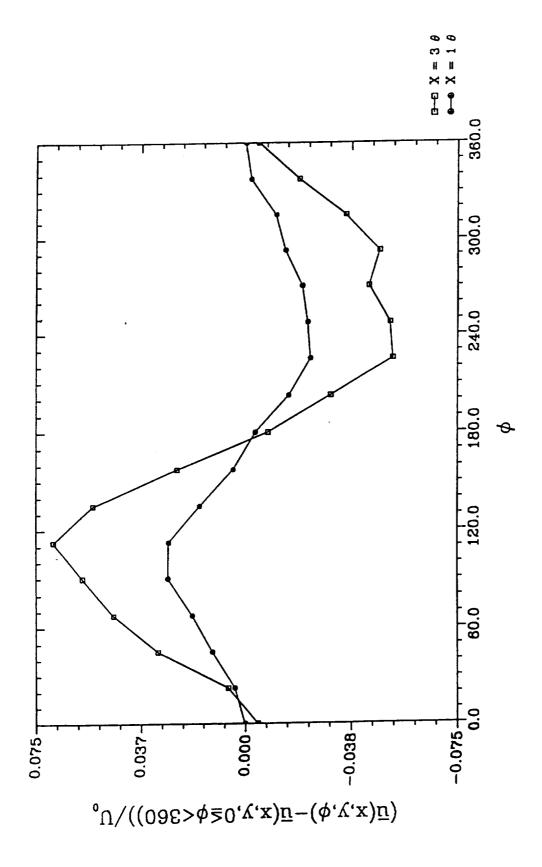
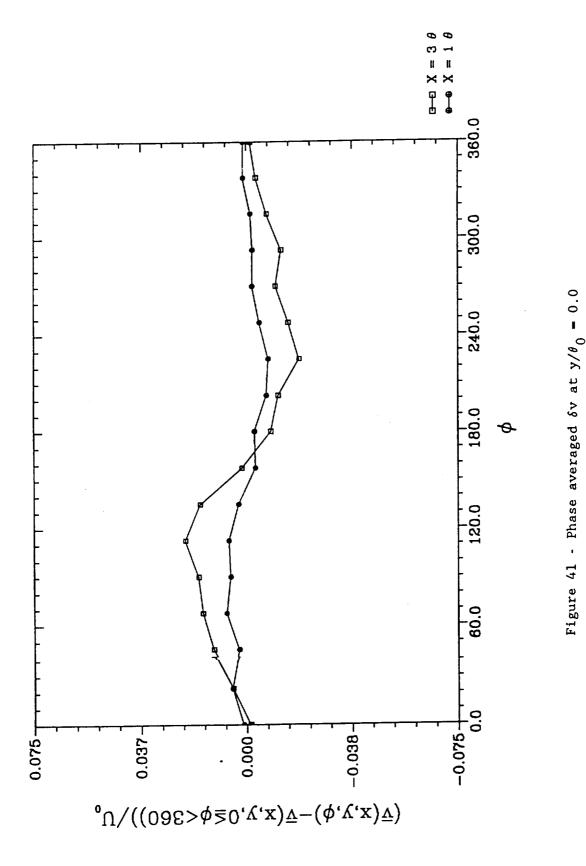


Figure 40 - Phase averaged 6u at y/θ_0 = 0.0



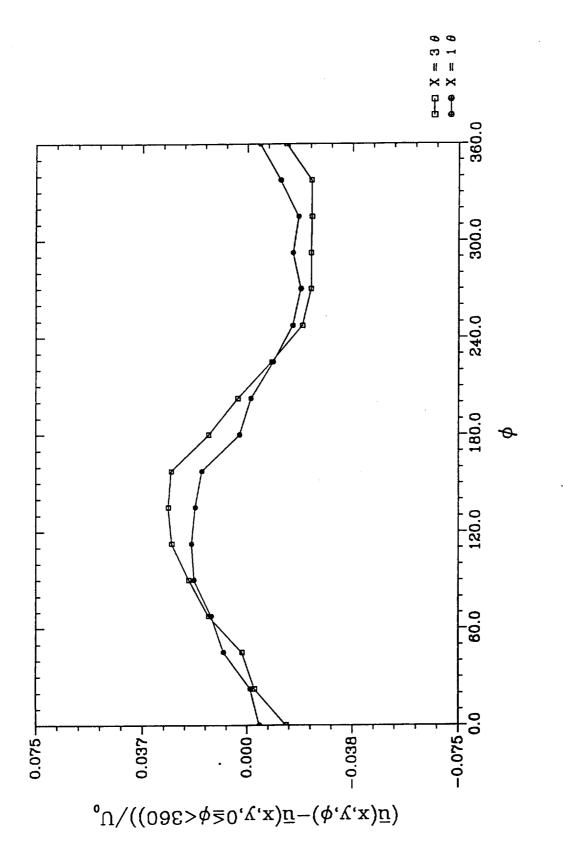


Figure 42 - Phase averaged δu at y/θ_0 = -1.02

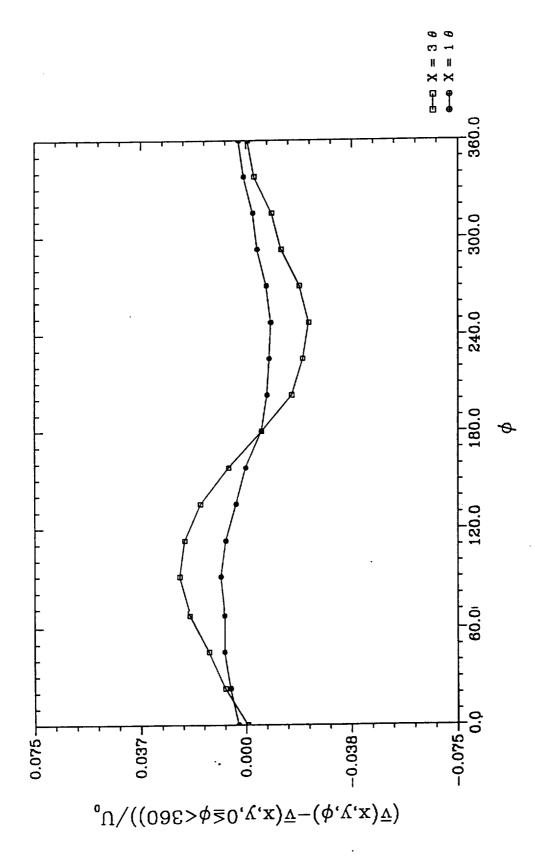


Figure 43 - Phase averaged 6v at y/θ_0 = -1.02

C-1.

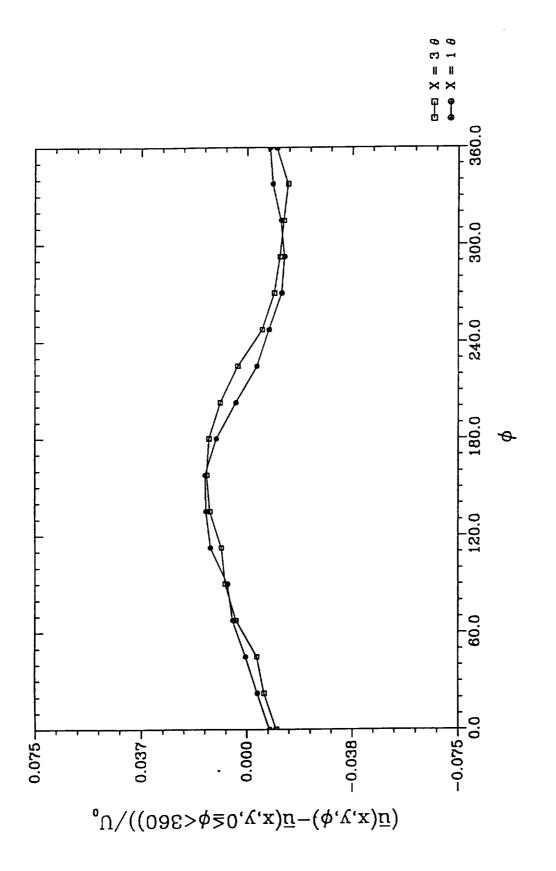


Figure 44 - Phase averaged δu at y/θ_0 = -3.06

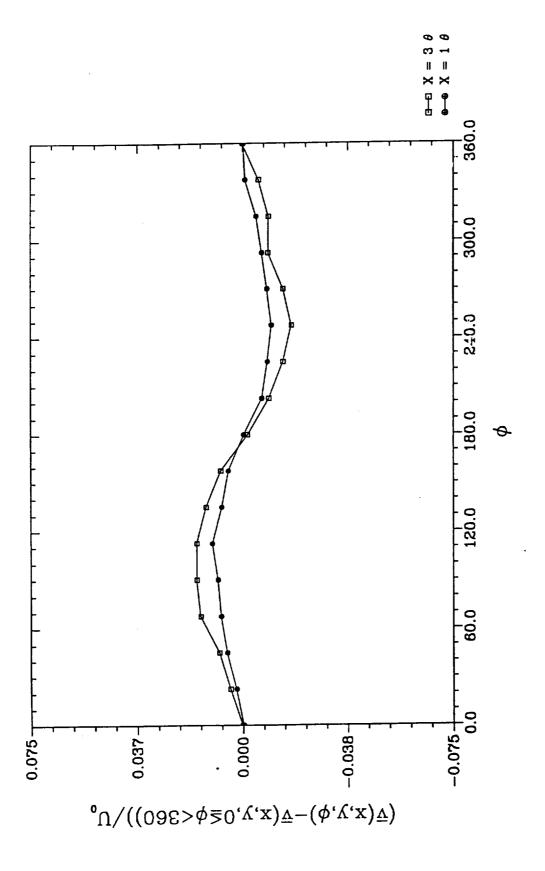


Figure 45 - Phase averaged δv at y/θ_0 = -3.06

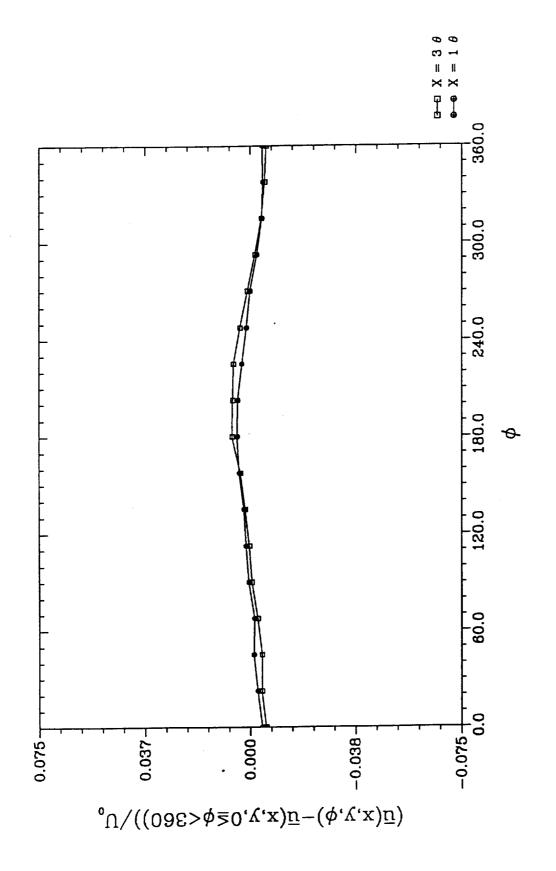


Figure 46 - Phase averaged δu at y/θ_0 = -9.36

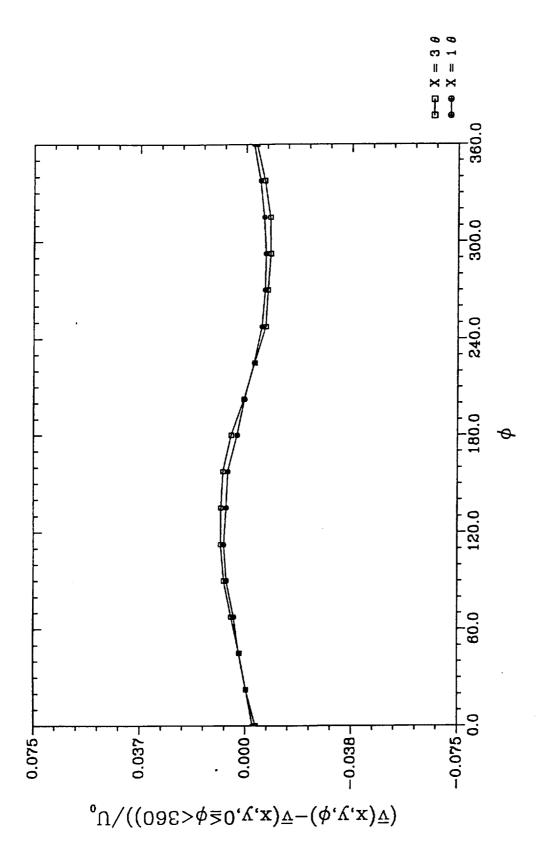


Figure 47 - Phase averaged δv at y/θ_0 = -9.36

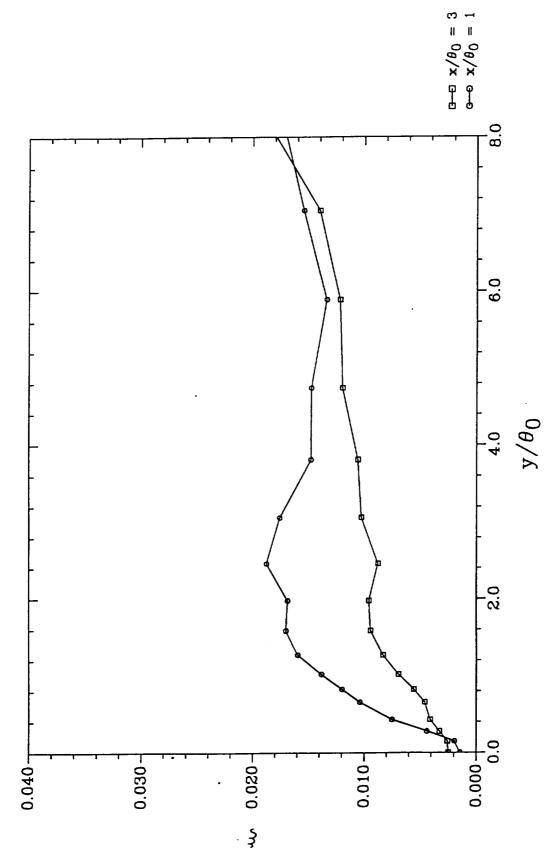


Figure 48 - Forced velocity component intensity relationships

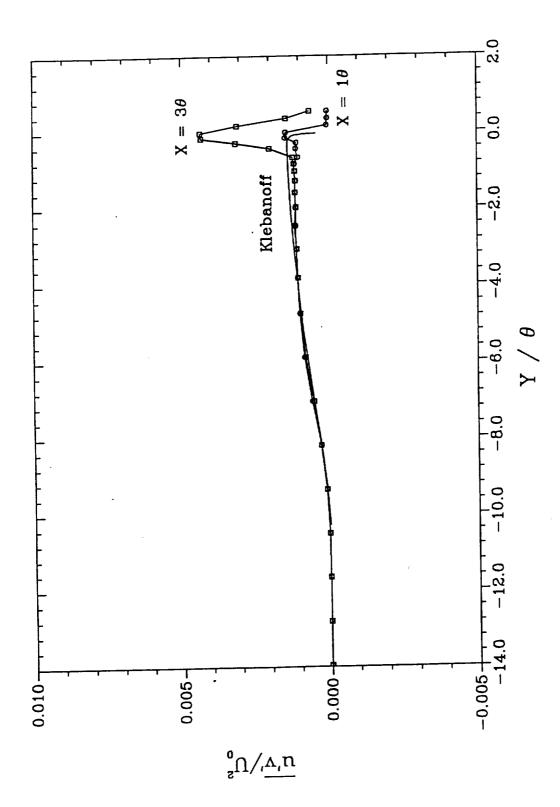


Figure 49 - $\frac{u'v'}{u'v'}$ in the separating boundary layer

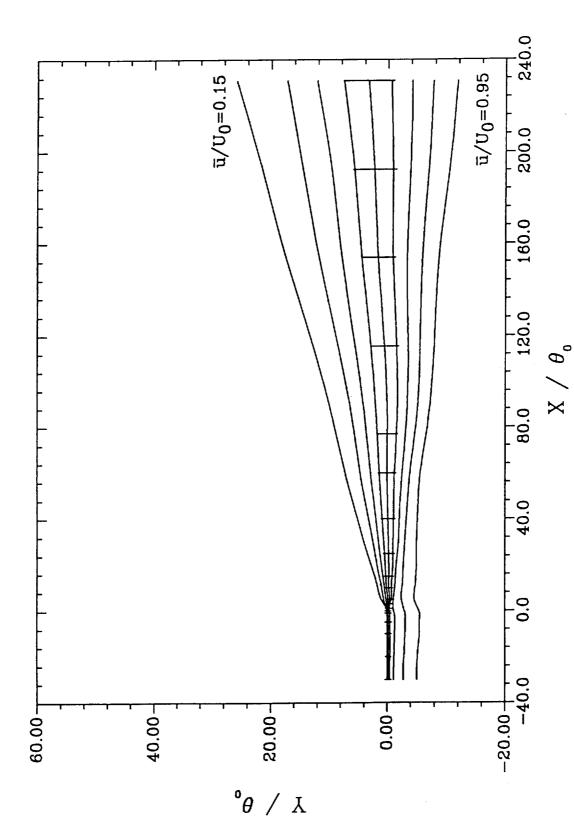
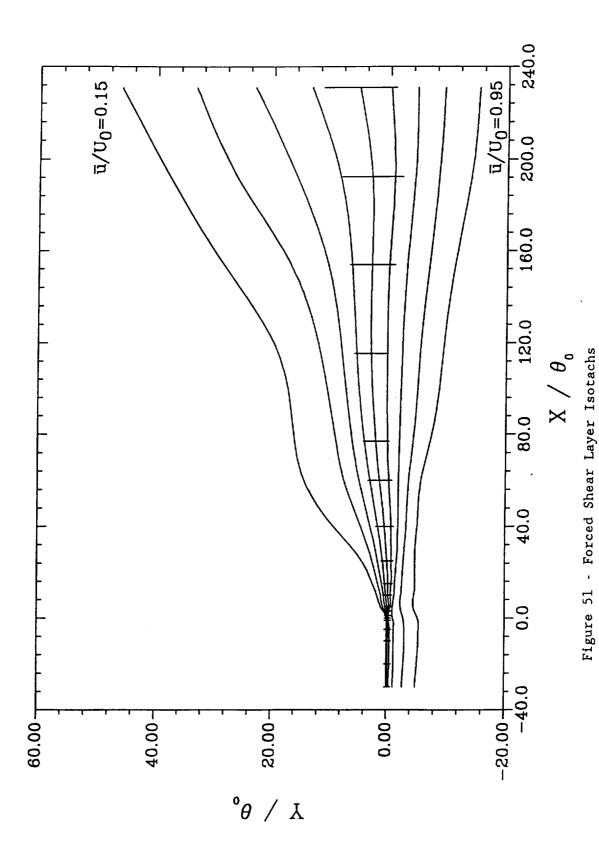


Figure 50 - Unforced Shear Layer Isotachs



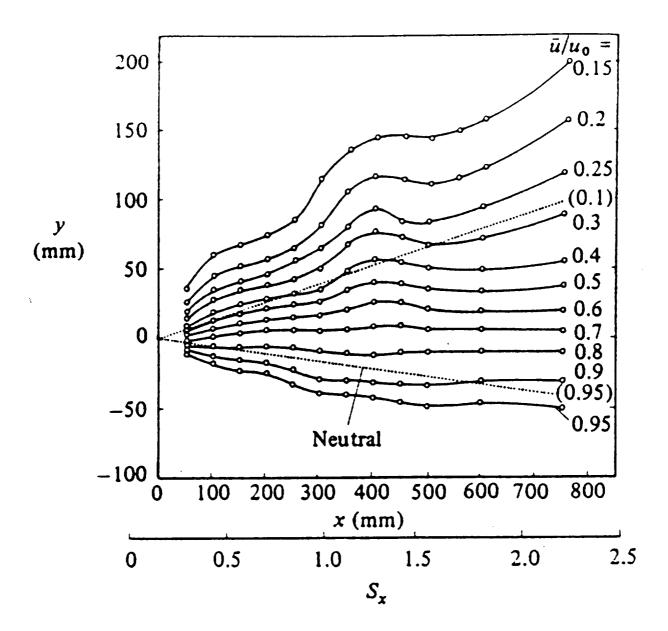
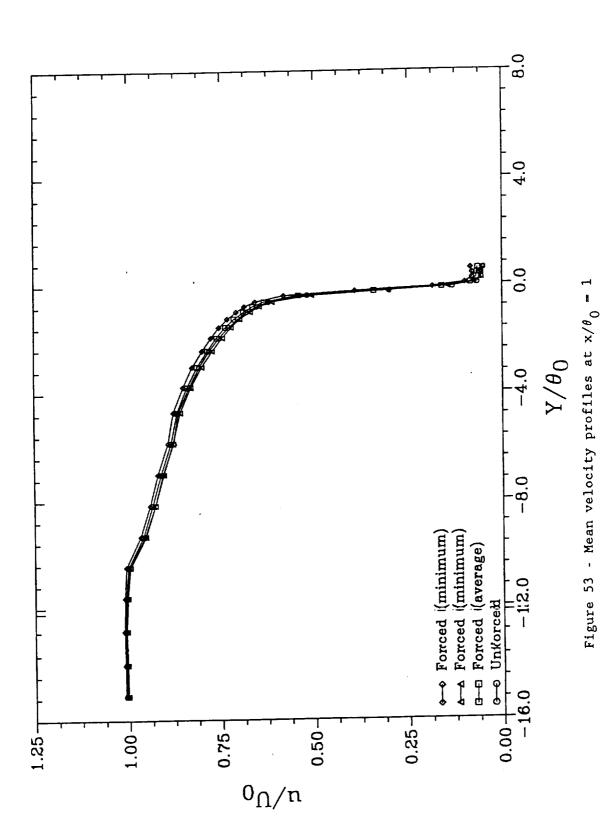
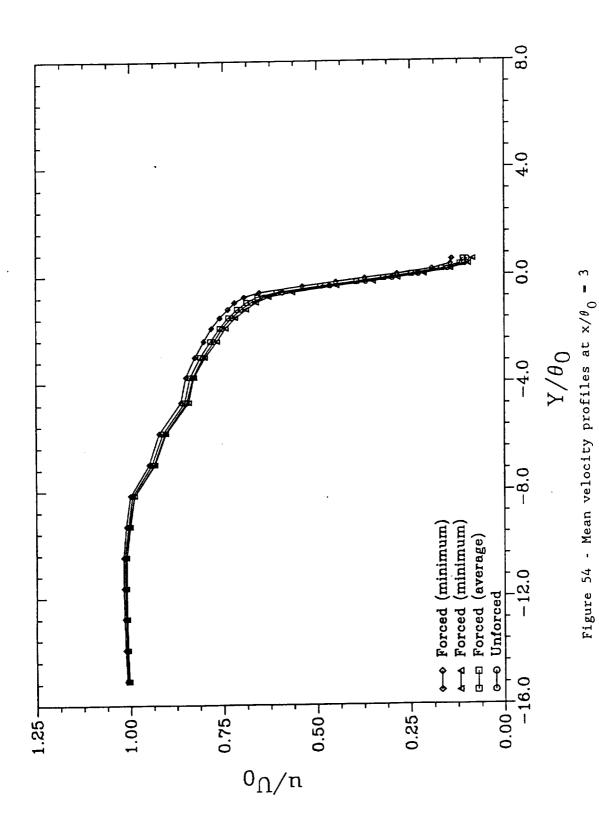


Figure 52 - Forced Shear Layer Isotachs (Fiedler and Mensing [1985])





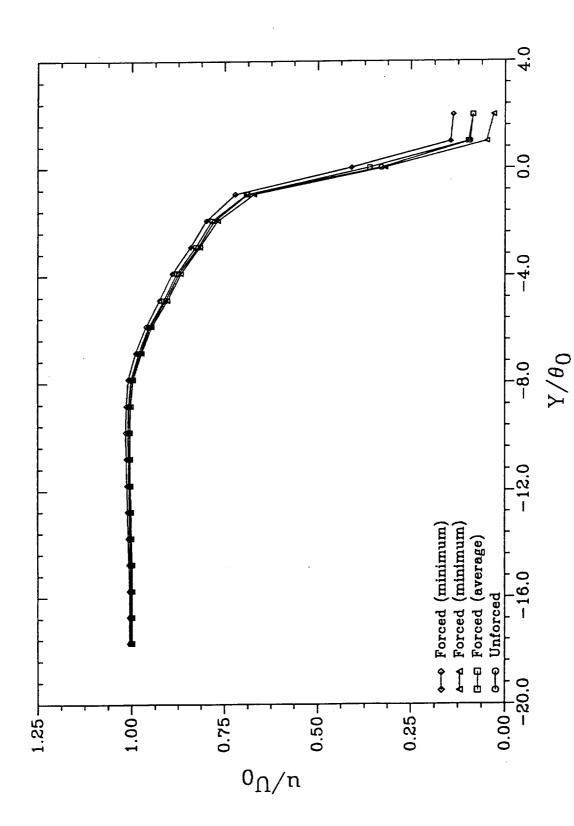


Figure 55 - Mean velocity profiles at x/θ_0 = 5

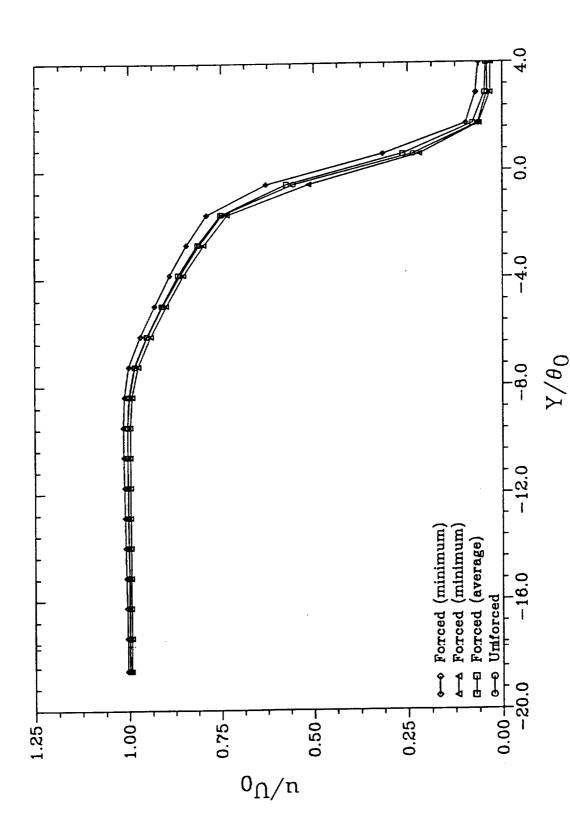
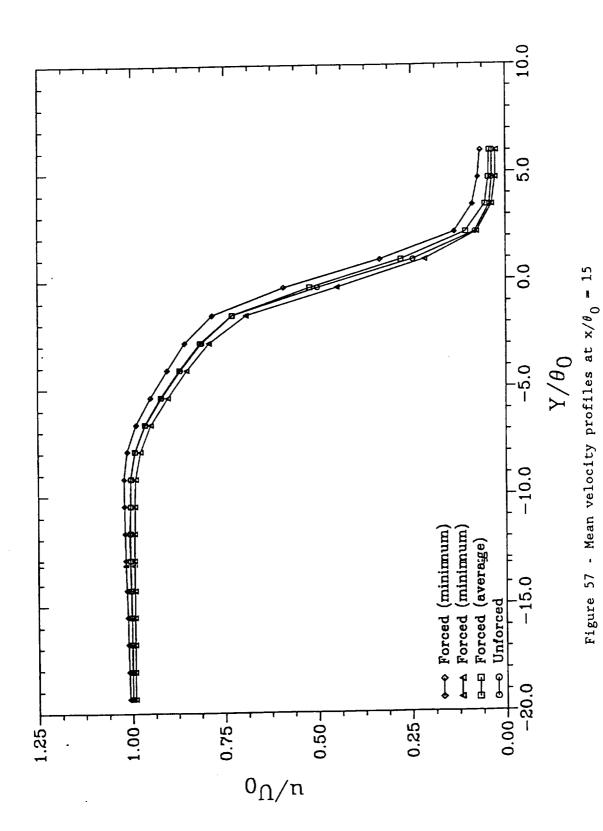
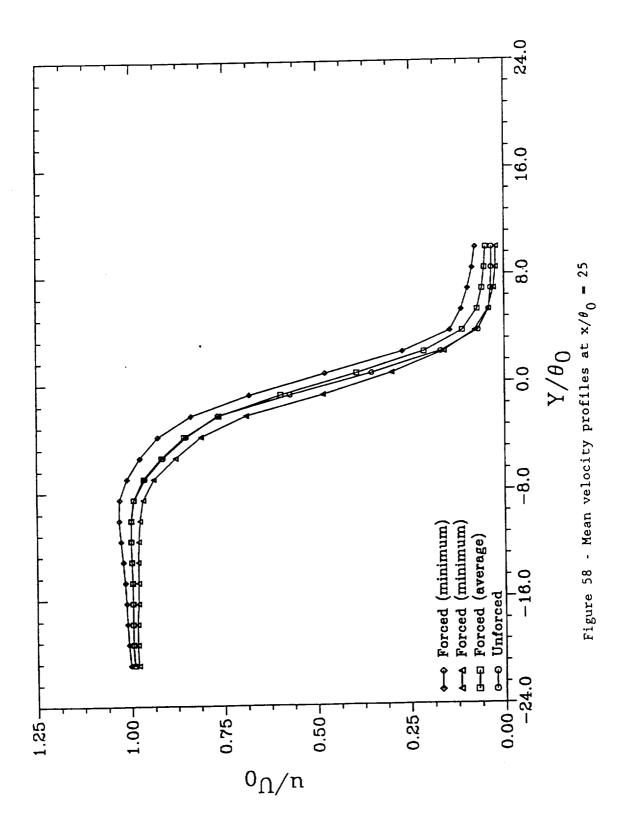
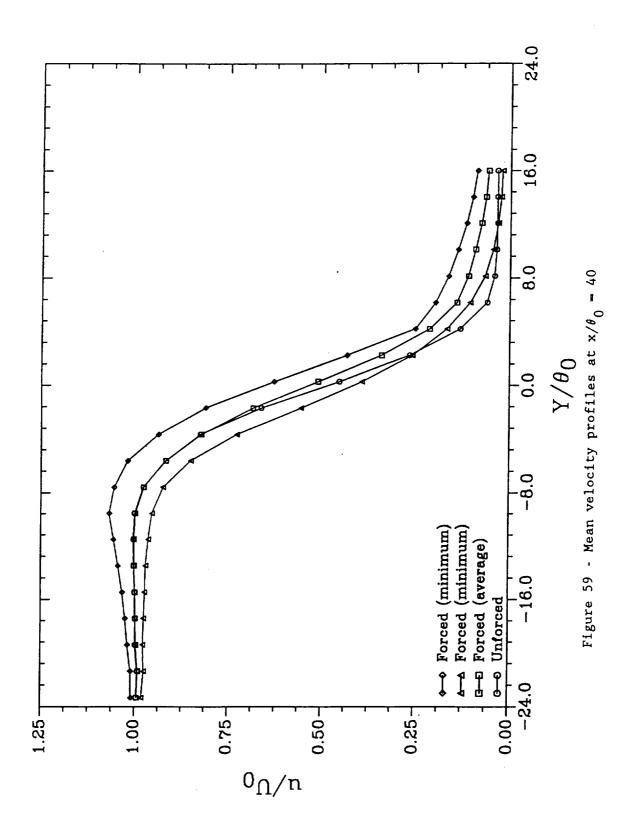
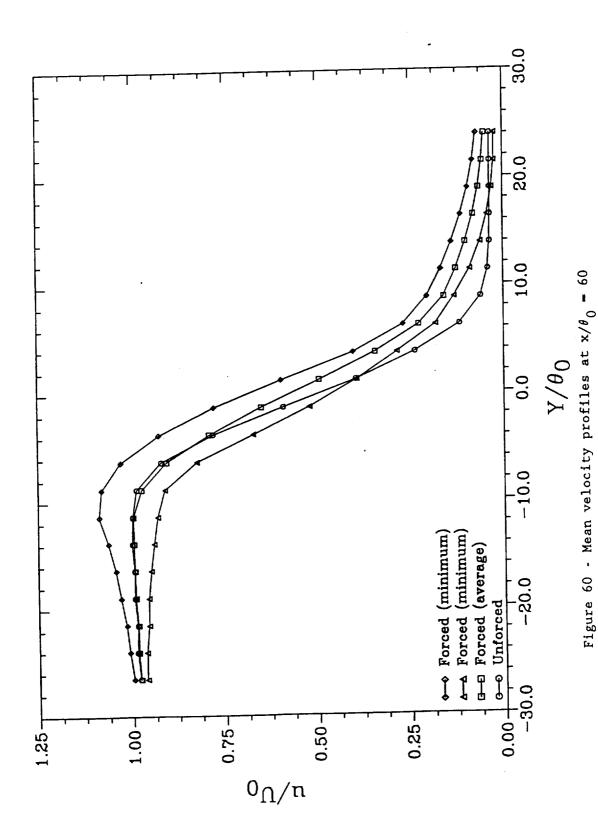


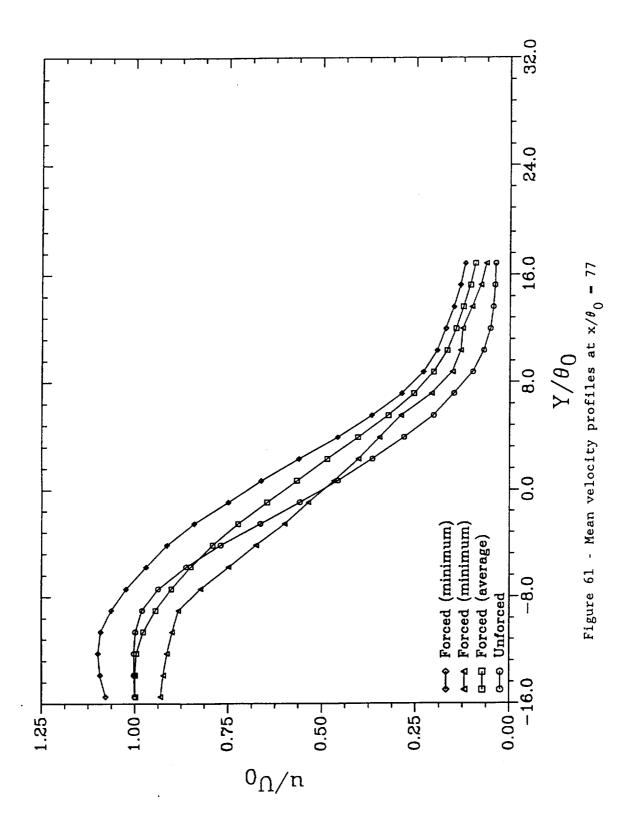
Figure 56 - Mean velocity profiles at $x/\theta_0 = 10$

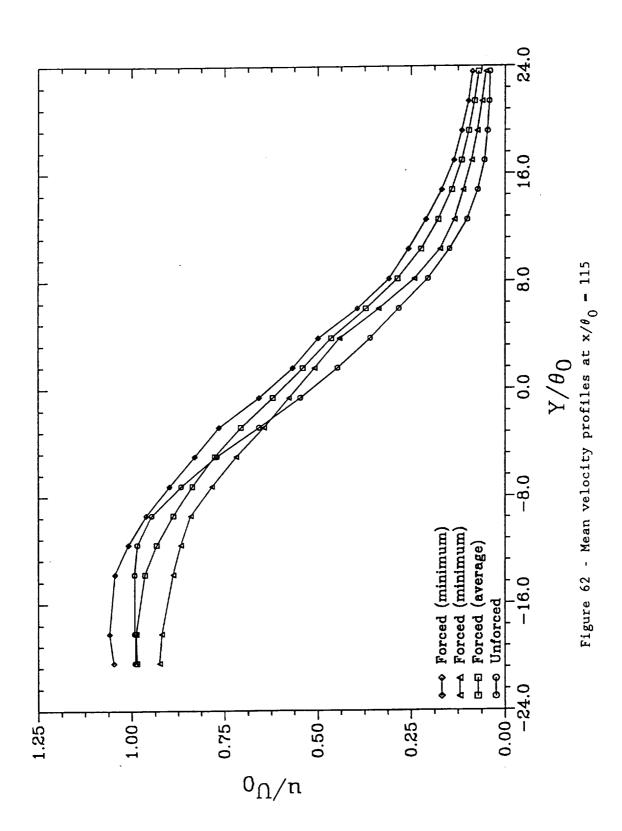


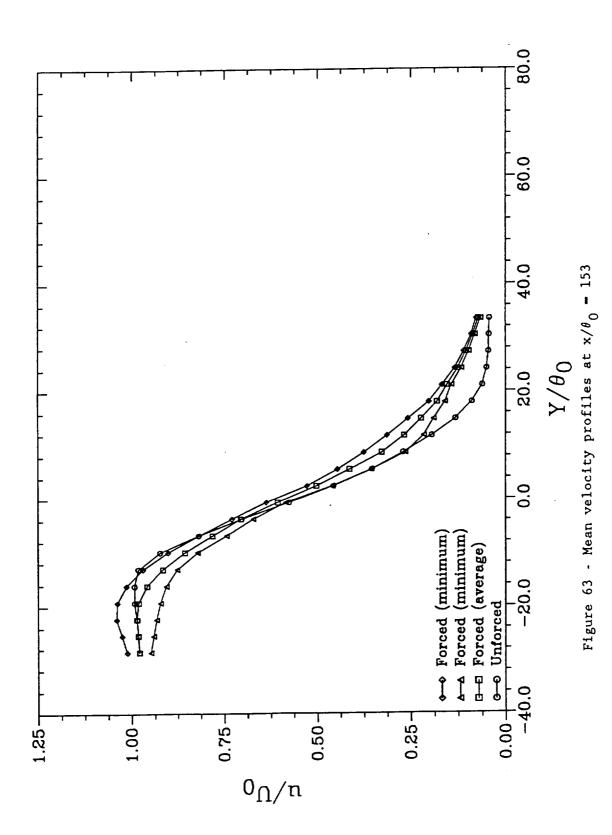


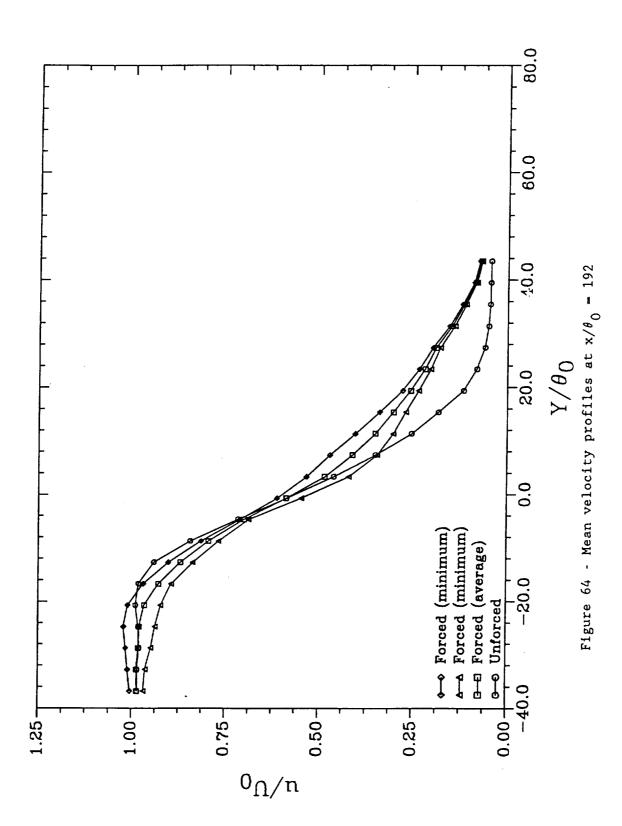


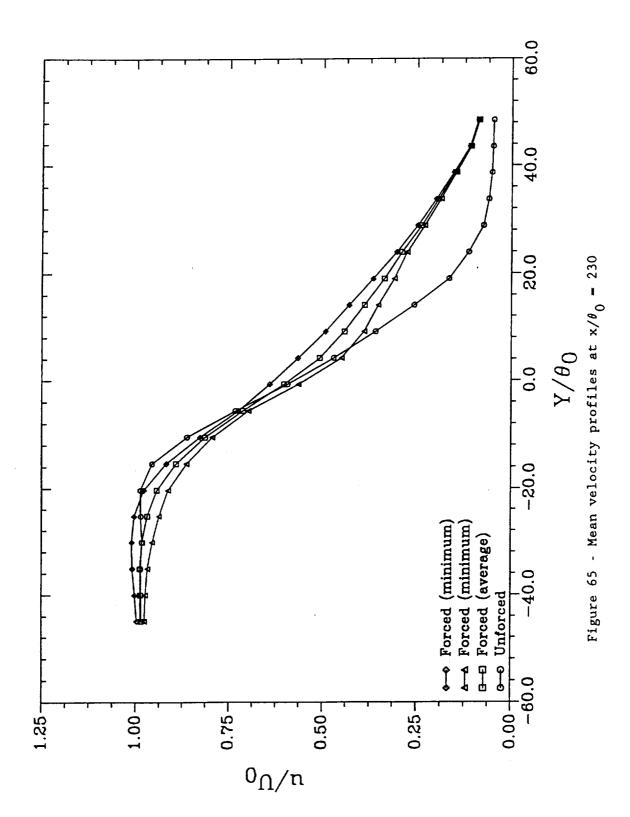


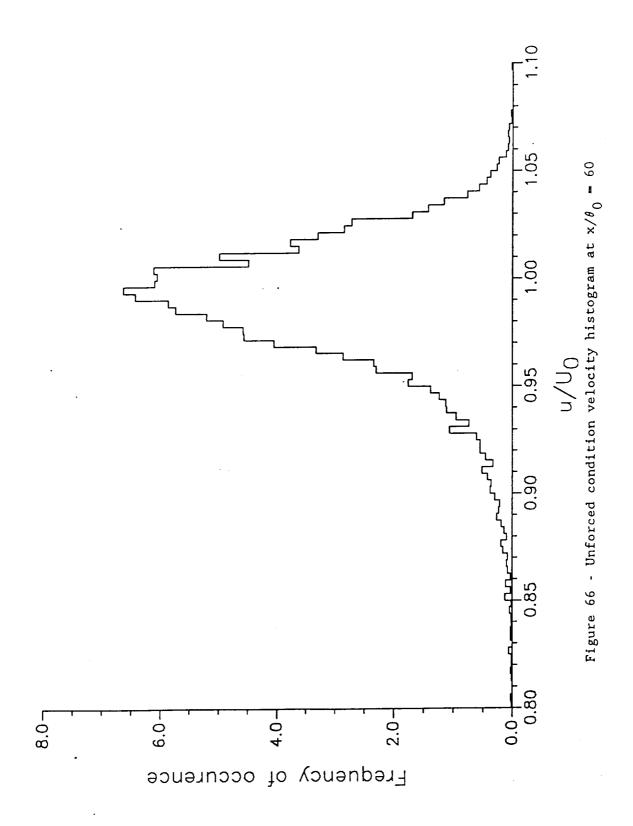


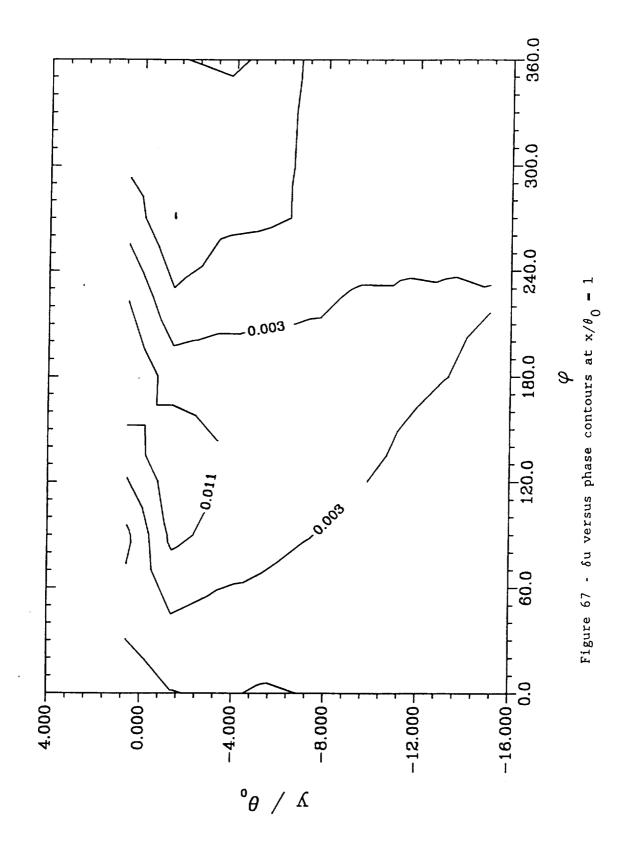


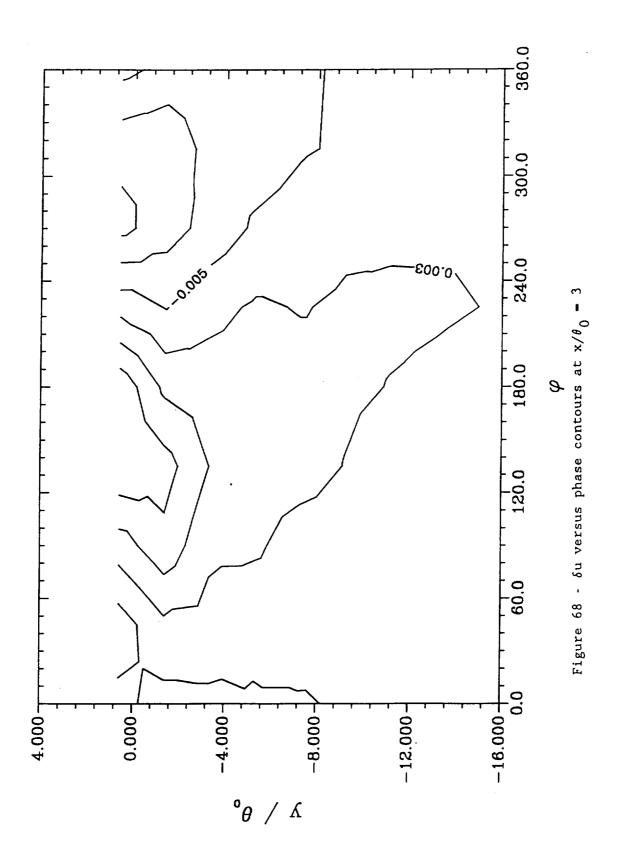


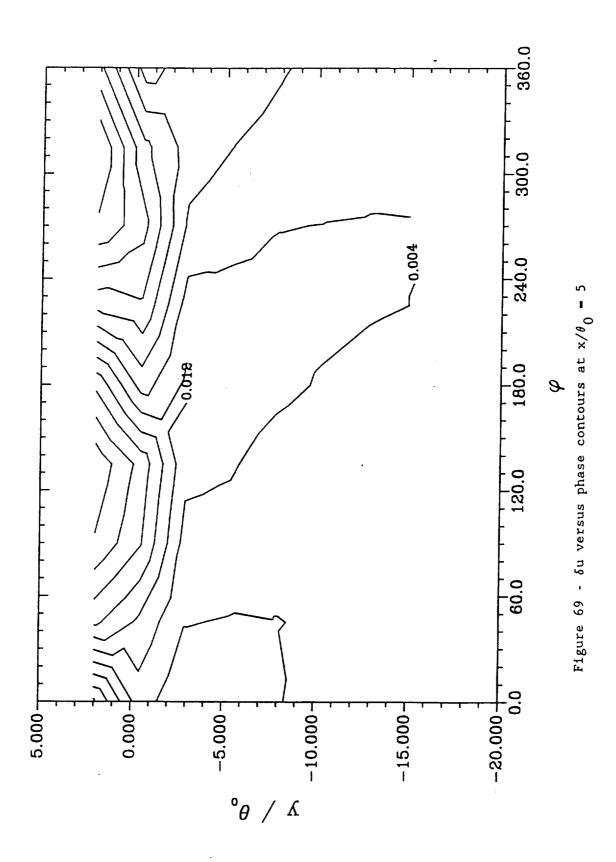


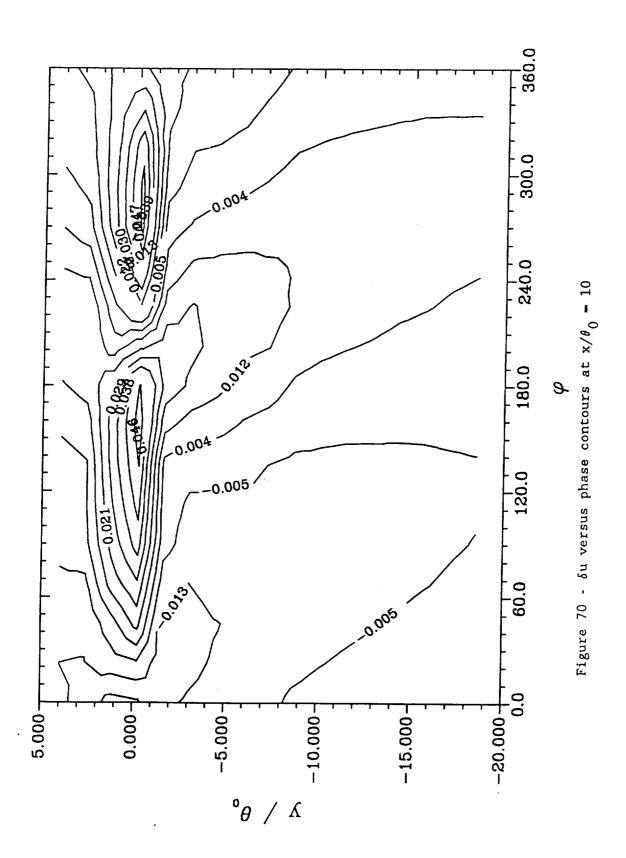


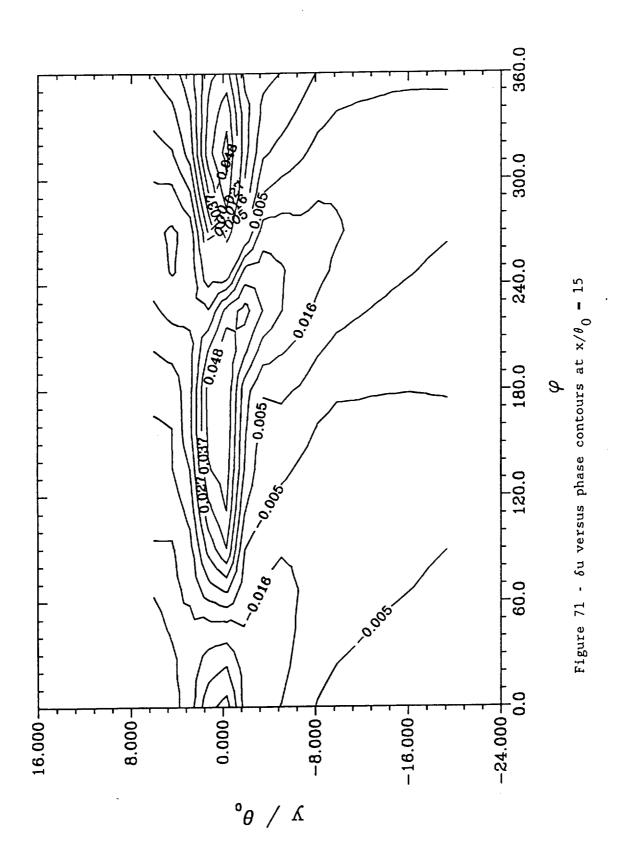


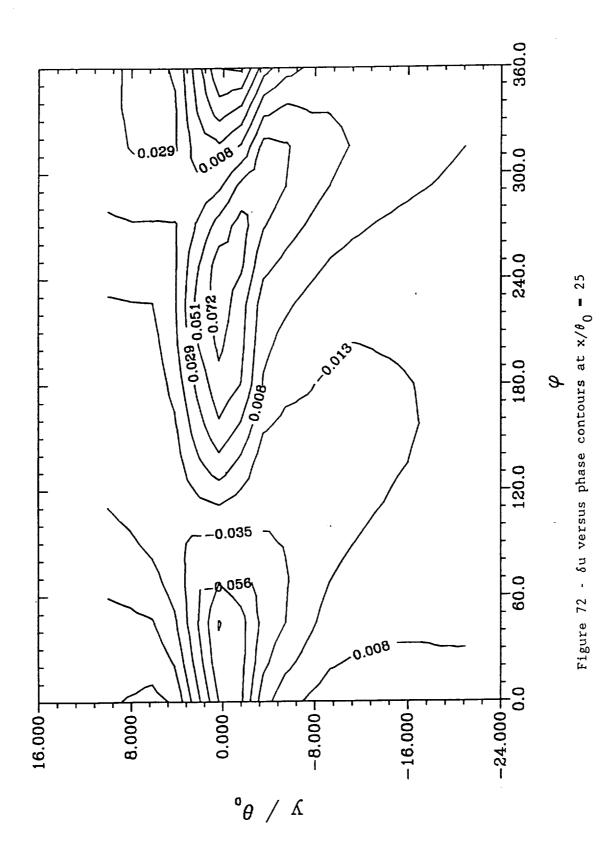


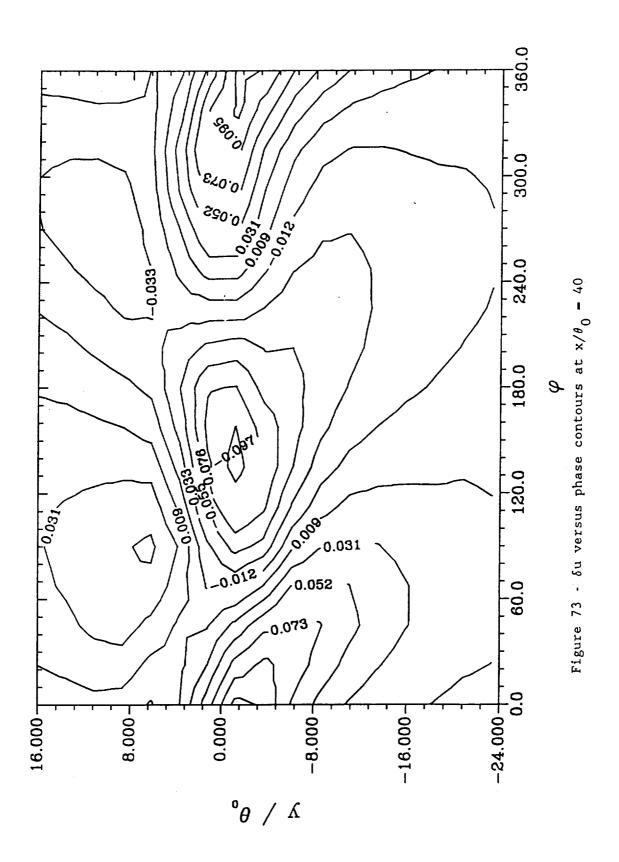


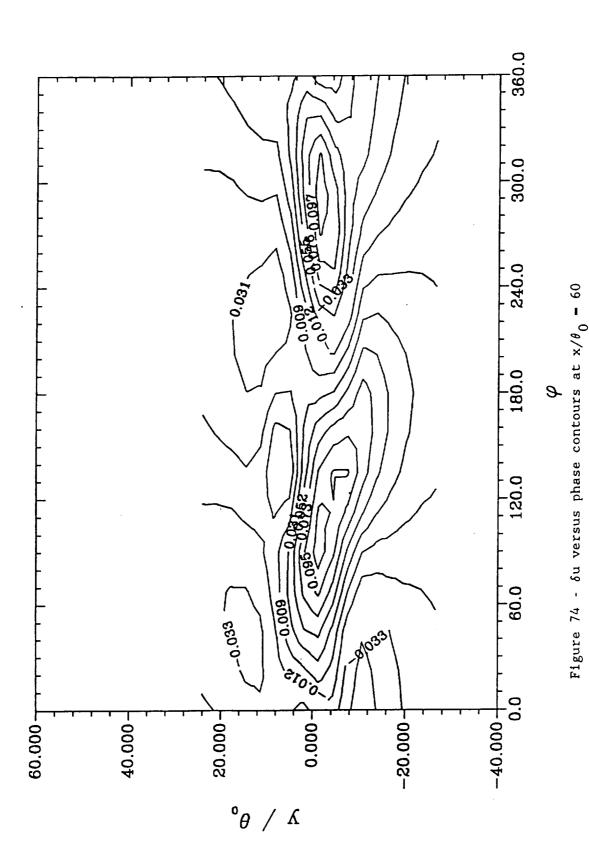


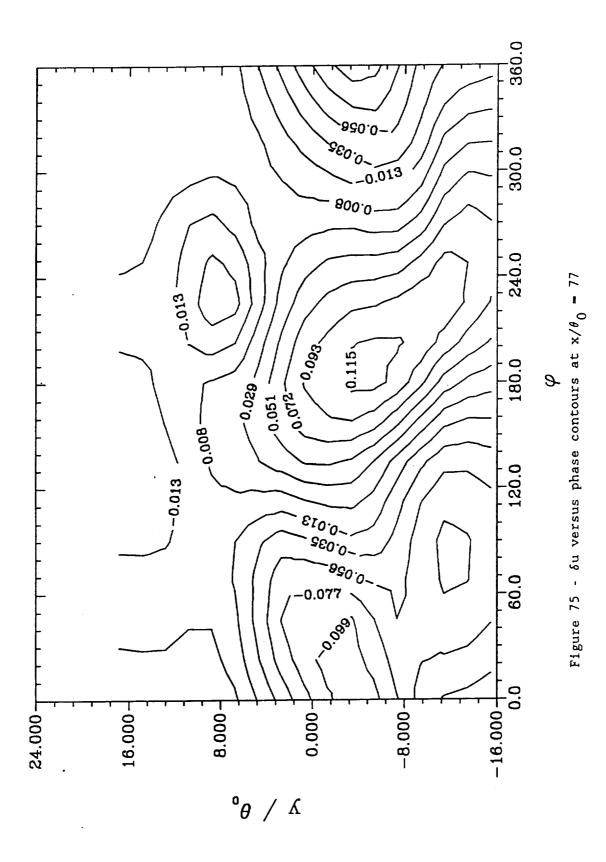


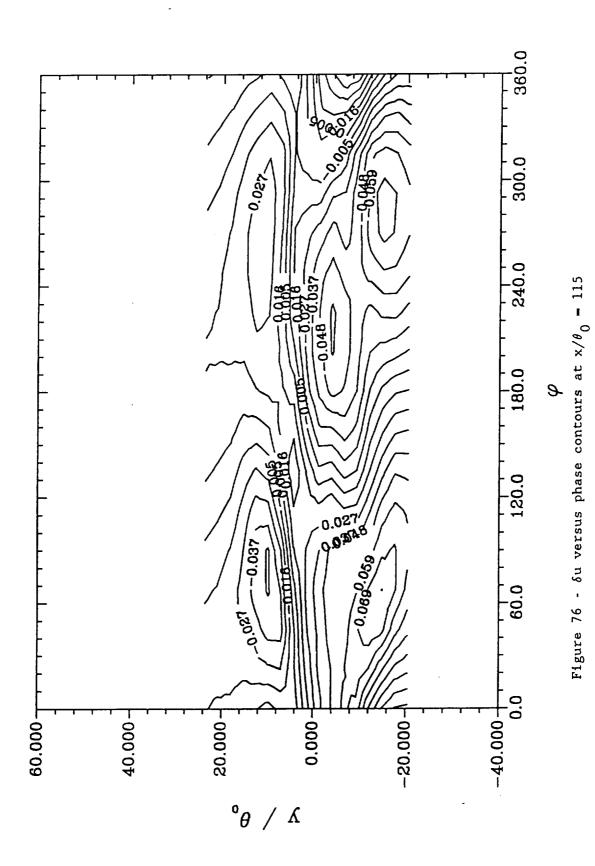


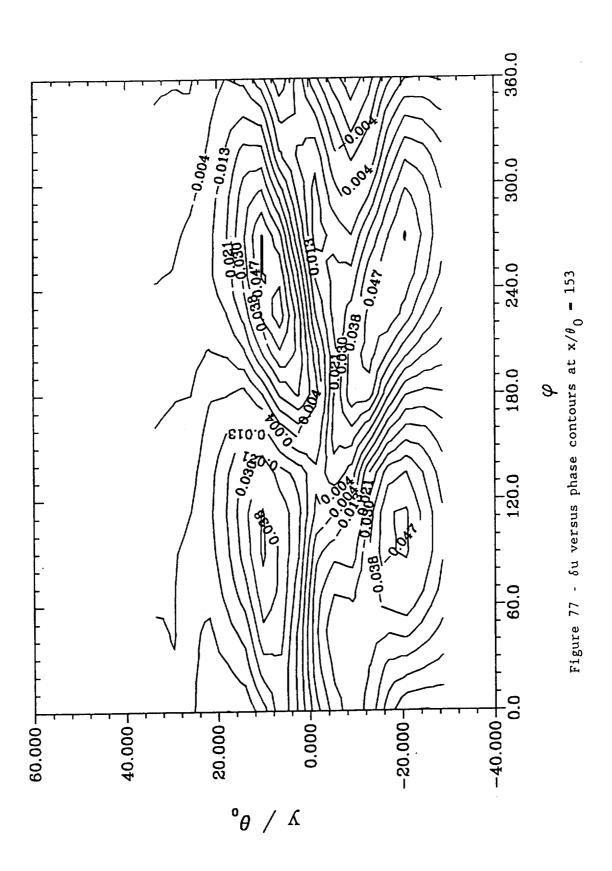


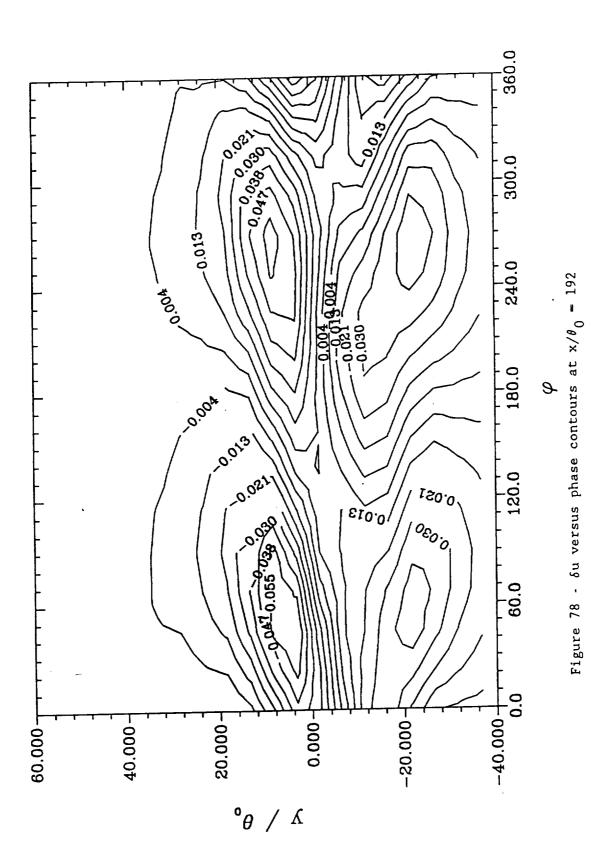


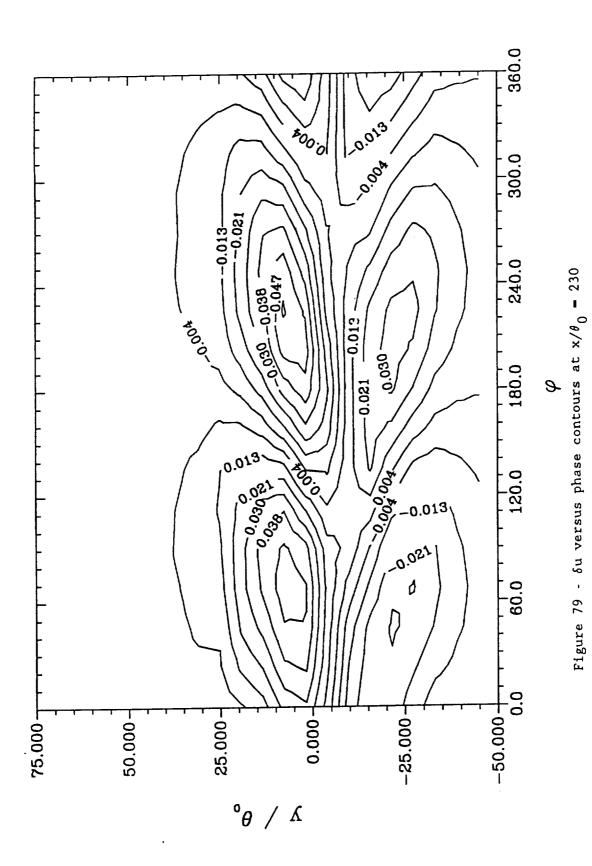


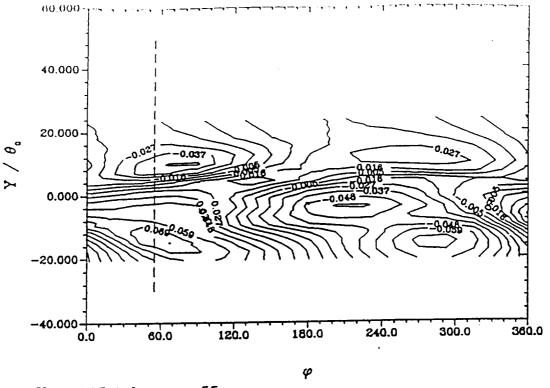












 $X_i = 115.4 \ \theta \ \varphi_i = 55.$

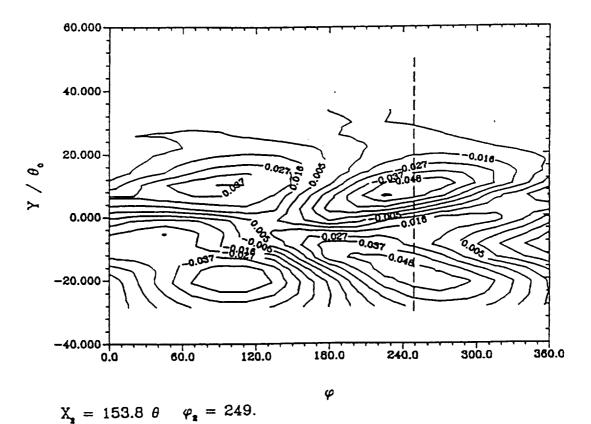


Figure 80 - Determination of disturbance phase location

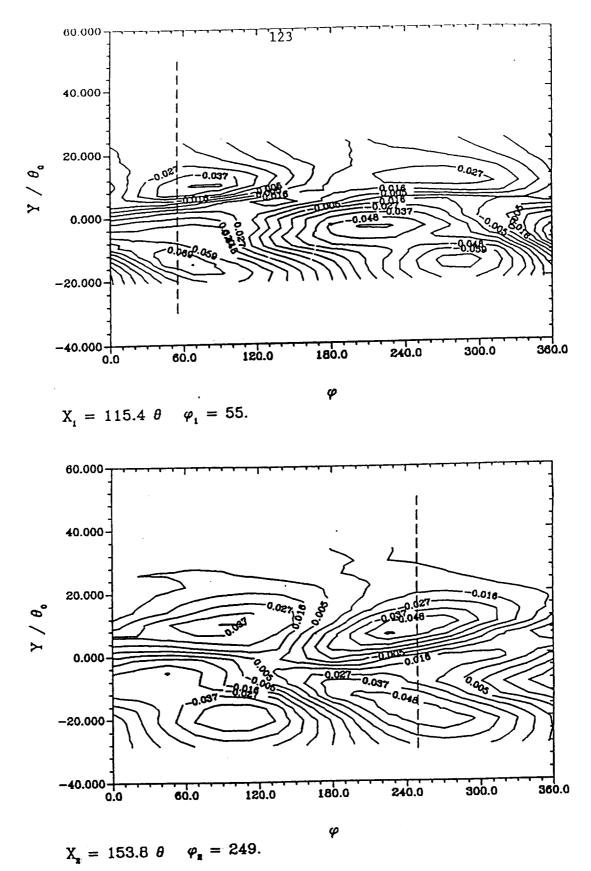


Figure 80 - Determination of disturbance phase location

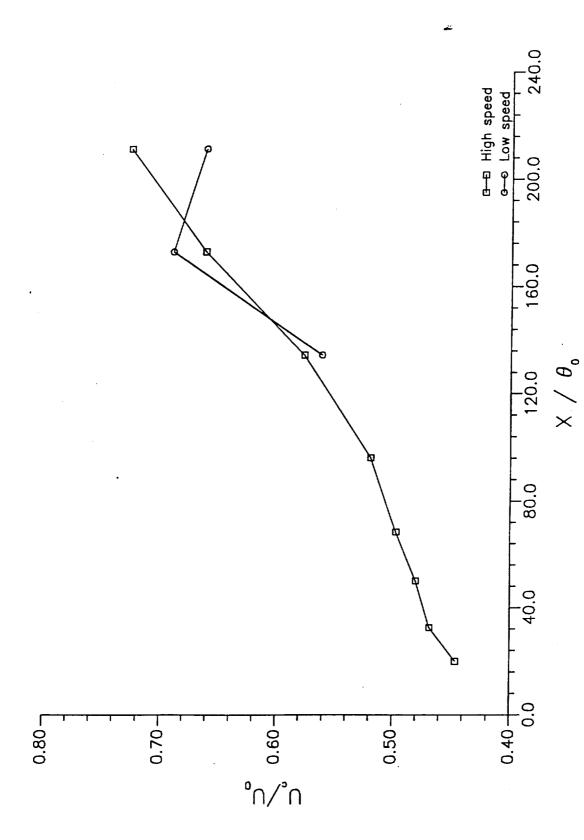


Figure 81 - Convection speed in the developing shear layer

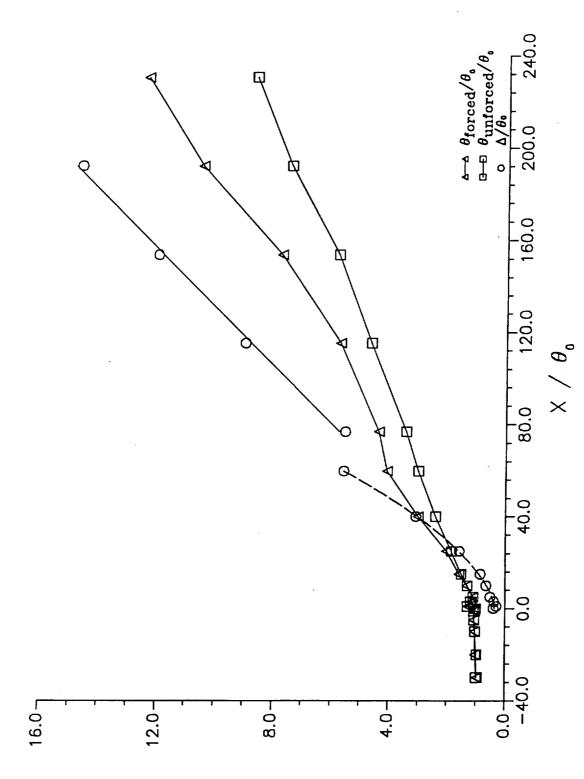
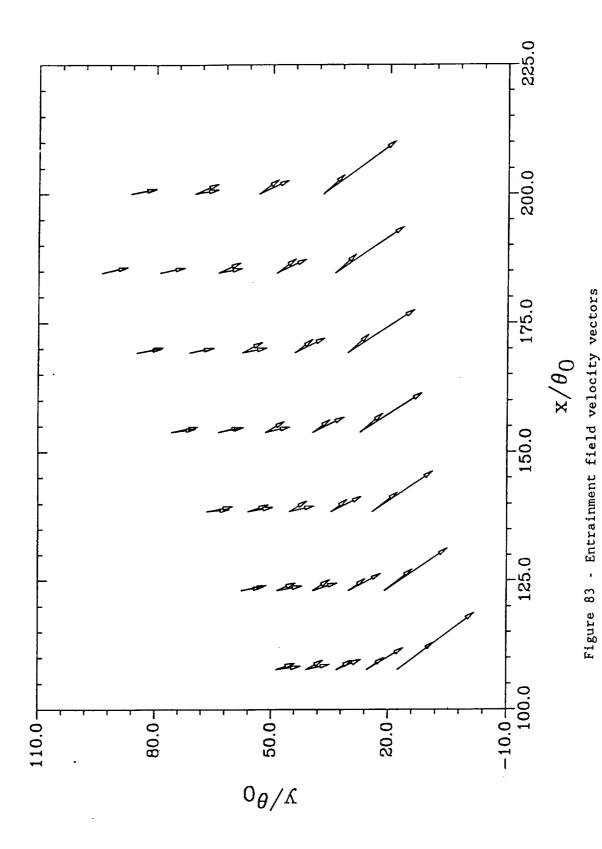
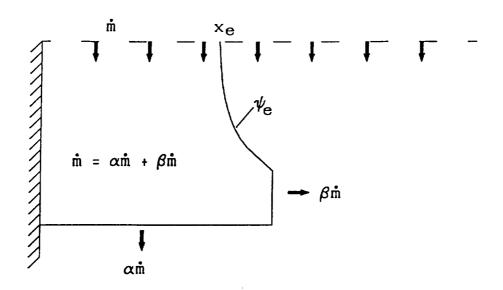
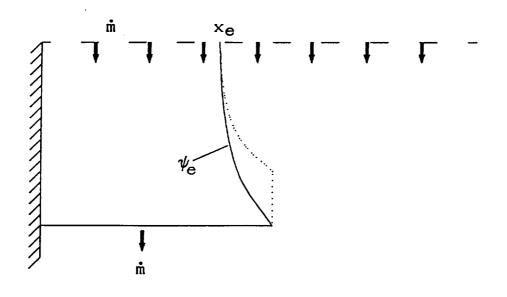


Figure 82 - Width measures in the developing shear layer





Unforced Condition



Forced Condition

Figure 84 - Schematic representation of entrainment mass flux

APPENDICES

APPENDIX A

EFFECT OF WALL CONTACT ON HOT-WIRE CHARACTERISTICS

A hot-wire anemometer, being a thermal device, is strongly effected by the proximity of a thermally conducting wall. Even when heat loss effects are minimized through use of a poorly conducting wall there is appreciable heat loss to the wall at small wire-to-wall distances. If one of the prongs, which supports the copper plated 5 μ tungsten wire, comes into contact with the wall, the heat loss is strongly intensified. This effect can be used to accurately locate the position of the wire by moving the wire towards the wall until a sharp increase in the anemometer output is noted. This positioning method was evaluated for the current study; it was abandoned after it was discovered that bringing the wire into contact with the wall modified the wires characteristics.

To quantify the variation in wire characteristics, a number of consecutive calibrations were performed with the same wire. All calibrations were executed over a period of 3 hours, during which time

the temperature of the room remained constant to within 1°C. The subject wire had been operated for several days, and it was operated for over two hours in the calibration flow before the first calibration. The wall under consideration was Formica faced, and meticulously cleaned using isopropyl alcohol prior to the study. In each case the wire was calibrated: i) one or more times in the calibration stream, ii) positioned using the wall contact method, and iii) moved back into the calibration stream and recalibrated. The above procedure was executed for a number of cases; see Table A.1 for the resulting data. The calibrations indicated with a "yes" under the heading contact in Table A.1 came into contact with the wall prior to the calibration.

The velocity error in Table A.1 was obtained using the following procedure. The calibration constants for the first calibration were used to compute a reference voltage from an arbitrary reference velocity of 10.0 meters per second. The velocity error for each calibration was then evaluated as the difference between the computed flow speed (using the reference voltage) and the reference velocity of 10.0 meters per second.

Table A.1 - Wall Contact Calibration Results

		_		Std.	Computed	Velocity
Run Co	ntact A	В	n	Dev.	velocity	error
Α	9.041	3.769	0.41	0.007	10.00	0.00
в у	es 8.744	3.520	0.42	0.005	11.98	1.98
С	8.852	3.380	0.43	0.012	12.11	2.11
D	8.707	3.519	0.42	0.008	12.09	2.09
E Y	es 8.365	3.621	0.41	0.010	13.00	3.00
F	8.648	3.336	0.43	0.009	13.09	3.09
G Y	es 8.142	3.779	0.40	0.011	13.14	3.14
Н	8.475	3.467	0.42	0.006	13.23	3.23
I	8.496	3.453	0.42	0.008	13.28	3.28
J	8.589	3.325	0.43	0.012	13.37	3.37
K Y	es 8.247	3.621	0.41	0.009	13.36	3.36
L	8.414	3.459	0.42	0.009	13.48	3.48

As indicated in Table A.1, the hot-wire characteristics underwent a large change when the wire was brought into contact with the wall. The mechanism behind the change is unknown. For the current study, it was of sufficient interest to ascertain that this type of positioning method was not usable given the experimental configuration.

APPENDIX B

DROP TEST CALIBRATION TECHNIQUE

A novel low speed calibration method was employed for calibration of the hot-wire used in the zero free stream velocity $(\mathbf{U}_0 = 0)$ study. The general details of the calibration technique have been previously detailed, Haw [1987]. The specifics on the method used to obtain the reference velocity for the current study are detailed in the following.

The force balance for an arm in a uniform gravitational field can be written as

$$\alpha = \frac{\text{mgsin}(\theta)\overline{r}}{J}$$
 (B.1)

where α is the angular acceleration of an arm of mass m and moment of inertia J.

Since the mechanical properties of the arm are constant all of the constant terms can be merged into a single constant A. Adding additional constants to account for aerodynamic drag (B) and for bearing friction (C), the resulting force balance is

$$\alpha = A \sin(\theta) - B\omega^2 - C\omega \tag{B.2}$$

This equation of motion can be solved numerically to yield the position and velocity at any time given the appropriate initial conditions. To improve the numerical accuracy, the equation for the angular velocity of the arm can be expanded in terms of a Taylor series and applied at discrete time steps to yield:

$$\theta_{i+1} = \left\{ \left[(\omega_i''' \frac{\Delta t}{4} + \omega_i'') \frac{\Delta t}{3} + \omega_i' \right] \frac{\Delta t}{2} + \omega_i \right\} \Delta t + \theta_i$$
(B.3)

$$\omega_{i+1} = \left[(\omega_i'', \frac{\Delta t}{3} + \omega_i'') \frac{\Delta t}{2} + \omega_i' \right] \Delta t + \omega_i$$
(B.4)

where the subcripts i and i+1 denote the current and the subsequent time steps and the deriviatives of the velocity are given as:

$$\omega' = \alpha = A\sin(\theta) - B\omega^2 - C\omega \tag{B.5}$$

$$\omega'' = (A\cos(\theta))\omega - 2B\omega\omega' - C\omega'$$
 (B.6)

$$\omega''' = \omega'[A\cos(\theta) + 2B\omega'] + \omega[\omega A\sin(\theta) - 2B\omega''] - C\omega''$$
 (B.7)

The constants A, B, and C were obtained by minimizing the mean square error in position between the numerical simulation, (from (B.3) and (B.4)), and a series of experimentally measured data points. Although an analytic solution was not possible, numeric results were readily obtained using a steepest descent solution method to minimize the mean squared positional error. The constants obtained in this manner were used in the numerical simulation for the fall, (B.3) and (B.4), to provide the calibration velocities.

APPENDIX C

ZERO MEAN FLOW PRESSURE MEASUREMENTS

Measurements of the pressure field induced by the piston were made for the condition of zero mean flow $(\mathbf{U}_0 = 0)$. The forcing frequency was sufficiently high, and the pressures sufficiently low to make measurements using a conventional tap and pressure transducer configuration impractical. A microphone, modified with a surrounding cavity and pinhole arrangement, was used as detailed in the following.

A Bruel and Kjaer type 4166 wide response condenser microphone was used with a locally fabricated cavity and pinhole. The microphone had a free air response of 0 to 20 KHz and an open circuit sensitivity of 48.6 mv per Pa. The microphone cavity consisted of a 17 mm diameter cylinder 5 mm long with a 1 mm hole at one end and the microphone face (17 mm diameter) forming the other end. The resulting resonant frequency of the chamber (1900 Hz), was well above the measurement range of interest.

APPENDIX D

NUMERICAL DATA

The following tables contain the primary experimental data for the current study. The data in the tables are non-dimensionalized in the following forms:

- a) The velocity measurements of the active shear layer and boundary layer are non-dimensionalized with the free stream velocity $({\bf U}_0); \quad \text{the corresponding data locations are non-dimensionalized with the separating boundary layer momentum thickness } (\boldsymbol{\theta}_0).$
- b) The measurements of the velocity and pressure for the no-flow data are presented in dimensional form. The velocity measurements are given in meters per second; the pressure measurements are given as output voltage from the microphone amplifier. In both cases the corresponding data locations are non-dimensionalized with respect to the forcing piston width $(\mathbf{w}_{\mathbf{p}})$.

Table D.1 - No Flow Hot-wire Mean Velocities

	IJ	nforce	i	Pha	se ave	eraged	data (at ang	$(1e \phi)$	
x/w _p	y/w _p	data	0.0		90.0	135.0	180.0	225.0	270.0	315.0
, _p	J, "b									210
1.5	.77	.044	.167	.151	. 243	.211	.127	.214	. 341	.319
1.5	.38	.038	.142	.133	.210	.191	.113	.167	. 276	.261
1.5	.00	.036	.147	.120	.178	.162	.104	.172	. 274	.261
1.5	38	.037	.155	.113	.146	.139	.101	.169	.269	.261
1.5	77	.030	.152	. 107	.123	.119	.093	.154	.251	.245
1.5	-1.54	.040	.138	.098	.098	. 095	.080	.122	.201	. 204
1.5	-3.08	.029	.086	.067	.065	.064	.055	.068	.104	.115
1.5	-6.15	.042	.060	.052	.047	. 047	.045	.047	.059	.066
1.5	-10.00	.025	.053	.049	.047	. 045	.045	.049	.056	.057
	-23.08	.030	.053	.051	.049	.048	.048	.050	.053	.054
-2.9	38	.027	.024	.024	.030	.032	.028	.026	.028	.027
-1.0	38	.024	.034	.037	.057	.058	.042	.039	.054	.050
.0	38	.030	.100	.085	. 163,		.085	.098	.191	.189
1.0	38	.034	.140	.098	.134	.132	.087	.135	. 244	. 244
2.9	38	.036	.086	.098	.149	.137	.084	.101	.158	.141
5.0	38	.029	.358	. 263	.308	.356	.305	.279	. 301	.297
-5.0	-1.00	.042	.022	.023	.025	.027	.025	.024	.024	.023
-1.0	-1.00	.039	.036	.040	.059	.062	. 046	.041	.053	.052
.0	-1.00	.041	.062	.067	.112			.068	.105	.102
1.0	-1.00	.041	.116	.081	.098			.102	.180	.183
2.9	-1.00	.033	.087	.082	.115	.107	.073	.096	.147	.135
5.0	-1.00	.046	.190	. 252	. 309				. 281	.243
	-10.00	.024	.018	.018	.019				.018	.018
	-10.00	.029	.022	.023	.024					.022
	-10.00	.032	.021	.022	.023				.021	.021
-1.0	-10.00	.034	.028	.027	.028				.029	.028
	-10.00	.025	.036	.034	.032					.039
	-10.00	.037	. 045	.041	.037				.048	.049
	-10.00	.032	.067	.061	.055					
	-10.00	.021	.110	.103	.095					
	-10.00	.018	.047	.044	. 042	.040	.040	.044	.051	.051

Table D.2 - No Flow Hot-wire Rms Velocities

	1	Unforce	ed	Ph.	ase ave	eraged	data (at angle ϕ)				
x/w _p	y/w _p	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0	
		000									
1.5		.002	.014		.020	.016	.008	.016	.022	.025	
1.5	. 38	.001	.016	.013	.019	.014	.007	.017	.023	.028	
1.5	.00	.002	.017	.007	.012	.008	. 005	.017	.025	.028	
1.5	38	.004	.012	.004	.008	.007	.004	.012	.019	.019	
1.5	77	.002	.011	.004	. 007	.006	.004	.012	.019	.017	
1.5	-1.54	.006	.009	.004	.005	.006	. 004	.013	.018	.014	
1.5	-3.08	.001	.013	.007	.005	.005	.005	.010	.019	.019	
1.5	-6.15	.005	.013	.010	.007	.006	.007	.008	.013	.015	
1.5	-10.00	.002	.011	.010	.008	.007	.008	.010	.013	.013	
1.5	-23.08	.002	.018	.017	.016	.015	.015	.016	.018	.018	
-2.9	38	.002	.003	.003	.003	.003	.003	.003	.003	.003	
-1.0	38	.003	.002	.002	.003	.003	.002	.002	.003	.002	
.0	38		.004	.003	.005	.005	.003	.003	.005	.007	
1.0	38	.005	.013	.004	.012	.010	.004	.018	.026	.022	
2.9	38	.005	.011	.010	.014	.012	.007	.014	.018	.017	
5.0	38	.003	.070	.095	.153	.110	.054	.029	.021	.033	
-5.0	-1.00	.005	. 004	.004	.005	.005	.004	.004	.004	.004	
-1.0	-1.00	.003	.002	.003	.004	.005	.003	.003	.003	.003	
.0	-1.00	.002	.003	.005	.007	.006	.004	.004	.006	.005	
1.0	-1.00	.004	.015	.005	.010	.011	.004	.017	.028	.024	
2.9	-1.00	.003	.012	.008	.014	.012	.007	.015	.019	.018	
5.0	-1.00	.004	.032	.058	.062	.131	.147	.082	.044	.029	
	-10.00	.004	.004	.004	.004	.004	.004	.004	.004	.004	
	-10.00	.005	.005	.005	.005	.005	.005	.005	.005	.005	
	-10.00	.005	.008	.008	.009	.009	.009	.008	.007	.007	
	-10.00	.005	.006	.006	.006	.006	.006	.006	.007	.007	
	-10.00	.003	.007	.006	. 005	.005	.005	.006	.008	.008	
	-10.00	.004	.009	.008	.006	.006	.007	.009	.011	.011	
	-10.00	.006	.017	.015	.014	.014	.015	.018	.020	.019	
	-10.00	.002	.022	.022	.022	.022	.023	.025	.026	.025	
10.0 -	10.00	.004	.024	.021	.019	.018	.020	.025	.029	.028	

Table D.3 - No Flow Microphone Mean Voltages

		Unfor		Ph	ase av	eraged	data	(at an	gle ø))
x/w _p	y/w _p	data	a 0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
P	ħ						•			
1.5	5 .77	7 2.32	6 .945	1.352	2.188	3.299	3.354	3.383	2 524	1 243
1.5	5 .38	2.32	7 1.028	1.409	2.193	3.259	3.288	3 333	2 477	1 320
1.5	.00	2.326	1.015	1.442	2.223	3.260	3.295	3 299	2 452	1 320
1.5	38	2.327	7 1.145	1.516	2.246	3.233	3 208	3 211	2.432	1 306
1.5	77	2.327	1.206	1.562	2.204	3.165	3 179	3 191	2 427	1 /1/
1.5	-1.54	2.326	1.274	1.664	2.303	3.178	3 102	3 073	2.727	1 450
1.5	-3.08	2.326	1.312	1.644	2.188	3.050	3 110	3 108	2.342	1 547
1.5	-6.15	2.326	1.488	1.776	2.232	3.019	2 972	2 966	2 401	1 624
1.5	-10.00	2.327	1.489	1.810	2.272	3.018	2.997	2.903	2 357	1.645
1.5	-23.08	2.327	1.667	2.034	2.529	3.063	2.913	2.626	2 044	1 658
-2.9	38	2.326	1.417	1.728	2.119	2.982	3.101	3.048	2 493	1 661
-1.0	38	2.326	1.371	1.648	2.115	3.063	3.154	3.126	2 462	1 585
.0	38	2.326	1.289	1.517	2.092	3.156	3.264	3.227	2.506	1 486
1.0	38	2.325	1.257	1.480	2.089	3.210	3.291	3.268	2 498	1 463
2.9	38	2.326	1.293	1.487	2.115	3.202	3.240	3.262	2 439	1 462
5.0	38	2.326	1.467	1.620	2.104	3.041	3.064	3.113	2 489	1 589
-5.0	-1.00	2.327	1.444	1.738	2.175	2.950	3.098	3.022	2 423	1 684
-1.0	-1.00	2.327	1.385	1.618	2.129	3.061	3.160	3.135	2.426	1 574
.0	-1.00	2.327	1.338	1.553	2.080	3.143	3.218	3.162	2.471	1 527
1.0	-1.00	2.327	1.329	1.502	2.045	3.191	3.243	3.234	2.502	1 489
2.9	-1.00	2.328	1.375	1.488	2.063	3.166	3.233	3.233	2.485	1 511
5.0	-1.00	2.327	1.553	1.621	2.189	3.013	3 028	3 083	2 482	1 507
-15.0	-10.00	2.327	1.584	1.875	2.330	3.012	2.999	2 824	2 306	1 7/17
-10.0	-10.00	2.328	1.609	1.838	2.268	3.048	2.976	2.827	2 326	1 717
-5.0	-10.00	2.327	1.602	1.786	2.266	3.027	2.985	2.857	2.371	1 689
-1.0	-10.00	2.326	1.577	1.796	2.223	3.060	2.994	2.855	2.407	1 673
.0	-10.00	2.326	1.617	1.741	2.211	3.046	2 988	2 897	2 412	1 665
1.0	-10.00	2.325	1.589	1.769	2.196	3.054	2.993	2.891	2.420	1 679
2.9	-10.00	2.325	1.617	1.759	2.182	3.036	2.986	2.893	2.425	1 684
5.0	-10.00	2.327	1.622	1.760 :	2.162	3.020	2.976	2.891	2.435	1 692
10.0	-10.00	2.326	1.650	1.789	2.160	2.975	2.934	2.847	2.443	1.735

Table D.4 - No Flow Microphone Rms Voltages

	1	Unforc	ed	Ph.	ase ave	eraged	data (at angle ϕ)			
x/w _p	y/w _p	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
1.5		.016	. 292	.122	.116	.126	.199	.161	.195	.171
1.5		.017	. 275	.126	.102	.129	.172	.140	.178	.174
1.5		.018	. 254	.112	.111	.128	.155	.132	.170	.140
1.5		.016	. 235	.112	. 102	.102	.158	.126	.160	.132
1.5		.017	. 240	.106	.108	.097	.151	.122	.156	.126
1.5		.016	.222	.097	.106	. 094	.140	.114	.152	.122
1.5		.015	.184	.092	.099	.091	.135	.101	.141	.102
1.5		.015	.156	.091	.110	.085	.108	.094	.123	.089
1.5		.016	.136	.081	.105	. 084	.093	.086	.105	.089
1.5		.016	.133	.111	.100	.099	.078	.090	.099	.084
-2.9		.015	.169	. 095	.103	.089	.115	.102	.132	.087
-1.0		.016	.195	.113	.106	.098	.119	.113	.147	.109
.0		.017	.213	.112	.098	.101	.121	.119	.134	.131
1.0		.016	.236	.106	.101	.104	.134	.169	.169	.152
2.9		.016	. 228	.100	.097	.107	.135	.164	.168	.137
5.0		.017	. 211	.095	. 093	.090	.114	.111	.137	.122
-5.0		.015	.165	.106	. 107	.090	.117	.099	.136	.095
-1.0		.017	.218	.101	.100	.091	.121	.135	.150	.109
.0	-1.00	.017	. 235	.106	.101	.097	.133	.153	.154	.128
1.0	-1.00	.017	.216	.109	.093	.098	.134	.165	.166	.134
2.9	-1.00	.016	. 232	.097	.091	.098	.127	.137	.167	.133
5.0	-1.00	.016	. 194	.089	.099	.110	.126	.126	.136	.126
-15.0	-10.00	.016	.120	.092	. 103	.091	.098	.082	.102	.084
	-10.00	.016	.134	.098	. 108	.088	.101	.087	.107	.085
	-10.00	.016	.135	.090	.092	.086	.096	.080	.108	.084
-1.0	-10.00	.016	.138	.083	.099	.078	.100	.083	.105	.082
	-10.00	.016	.135	.083	.093	.085	.093	.082	.101	.083
1.0	-10.00	.017	.134	.073	. 094	.075	.091	.080	.098	.084
2.9	-10.00	.016	.131	.073	.089	.074	.093	.076	.102	.075
	-10.00	.017	.137	.081	.089	.073	.097	.076	.101	.078
10.0	-10.00	.016	.138	.089	.095	.076	.097	.083	.096	.082

Table D.5 - Compact Probe \overline{u} (x/ θ_0 =1.0)

		Unford	ced	Pl	hase av	eraged	data (at angle ϕ)			
x/θ_0	y/θ_0	data	a 0.0	0 45.0	90.0	135.0	180.0	225.0	270.0	315.0
1.0	. 55						.062	.054	.046	.039
1.0	. 37					.066	.069	.057	.047	.041
1.0	.18				.059	.081	.090	.078	.066	.060
1.0	00			7 .238	.254	. 243	. 223	. 203		.216
1.0	15			. 508	.527	.521	.491			.468
1.0	28		.576	.595	.611	.610	. 590			. 559
1.0	43		.625	.640	.652	.654	. 638			.613
1.0	66		.655	.672	.680	. 684	. 669			.643
1.0	82			.686	. 697	. 702	.690			.663
1.0	-1.02	_		. 706	.717	.716	.700	.688	.678	.679
1.0	-1.27	. 706	. 709	.724	.732	.737	. 725	.709	.699	.701
1.0	-1.59	. 724		.739	. 749	.752	.744	.728	.721	.720
1.0	-1.98	. 746	. 752	.763	.768	.771	.764	. 749	.742	.743
1.0	-2.46	.772	.773	. 782	. 789	.792	. 788	.773	.764	.769
1.0	-3.06	. 796	. 794	.802	. 809	.817	.813	.799	.790	.790
1.0	-3.81	.830	. 827	.837	. 844	. 846	. 843	.833	.824	.825
1.0	-4.74	. 865	. 865	.869	.879	.883	.880	.872	.862	.860
1.0	-5.89	. 909	. 906	.912	.917	. 922	.920	.915	.909	. 905
1.0	-7.05	. 948	. 945	. 951	. 957	.960	.959	.953	. 947	.944
1.0	-8.20	. 980	.978	.980	. 985	. 986	.990	. 985	.979	.977
1.0	-9.36	. 996	. 995	.998	.999	1.001		1.002	.999	.995
		1.001	1.000	1.002		1.006			1.004	
	11.66	. 999	.999	1.000	1.001	1.004	1.007	1.006	1.004	1 001
	12.81	1.002	1.000	1.001	1.002	1 004	1 007	1 007	1 00%	002
1.0 -	13.97	1.001	1.000	1.000	1.001	1.003	1.005	1.006	1.004	L.002

Table D.6 - Compact Probe \tilde{u} (x/ θ_0 =1.0)

	1	Unforce	ed	Pha	ase av	eraged	data (at angle φ) 180.0 225.0 270.0 315.0			
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
1.0	.55									
1.0								.0235		
1.0	.18	.0209	.0228	.0239	.0258	.0266	.0285	.0274	.0246	.0250
1.0	00	.0737	.0733	.0753	.0777	.0708	.0683	.0693	.0745	.0755
1.0	15	.0933	.0900	.0918	.0901	.0891	.0971	.1002	.0946	.0948
1.0	28	.0814	.0803	.0802	.0747	.0771	.0816	.0865	.0835	.0832
1.0	43	.0754	.0759	.0709	.0734	.0726	.0748	.0757	.0787	.0781
1.0	66	.0738	.0726	.0715	.0723	.0717	.0716	.0745	.0788	.0722
1.0	82	.0748	.0724	.0733	.0721	.0716	.0724	.0722	.0743	.0748
1.0	-1.02	.0734	.0744	.0731	.0712	.0716	.0710	.0730	.0726	.0720
1.0	-1.27	.0712	.0713	.0700	.0697	.0695	.0712	.0723	.0727	.0727
1.0	-1.59	.0716	.0697	.0706	.0681	.0677	.0685	.0695	.0702	.0713
1.0	-1.98	.0697	.0702	.0689	.0668	.0650	.0669	.0702	.0707	.0692
1.0	-2.46	.0676	.0682	.0671	.0669	.0653	.0663	.0676	.0691	.0683
1.0	-3.06	.0669	.0664	.0648	.0642	.0650	.0651	.0660	.0674	.0653
1.0	-3.81	.0639	.0642	.0649	.0621	.0620	.0616	.0653	.0666	.0651
1.0	-4.74	.0609	.0616	.0606	.0600	.0596	.0611	.0595	.0623	.0601
1.0	-5.89	.0560	.0563	.0545	.0546	.0538	.0547	.0553	.0565	.0542
1.0	-7.05	.0481	.0480	.0480	.0456	.0456	.0480	.0483	.0484	.0496
1.0	-8.20	.0351	.0363	.0350	.0329	.0347	.0338	.0351	.0350	.0361
1.0	-9.36	.0215	.0226	.0211	.0204	.0207	.0209	.0214	.0198	.0223
1.0	-10.51	.0116	.0113	.0116	.0110	.0111	.0118	.0106	.0122	.0125
1.0	-11.66	.0080	.0084	.0079	.0078	.0077	.0077	.0081	.0081	.0082
1.0	-12.81	.0067	.0064	.0063	.0066	.0063	.0064	.0063	.0065	.0069
1.0	-13.97	.0060	.0059	.0061	.0060	.0059	.0059	.0061	.0058	.0060

Table D.7 - Compact Probe \overline{v} (x/ θ_0 =1.0)

	τ	Jnforce	ed	Pha	ase ave	eraged	data	(at ang	$gle \phi$)	
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
J				001	000	000	001	000	.001	.001
1.0	.55	.001	.001		000					
1.0	. 37	.000	.001	.001	001		002	002	.000	.001
1.0	.18	001	.000	.000	.000			005		000
1.0	00	.018	.019	.020	.023	. 020	.014	.010	.015	.016
1.0	15	.024	.030	.032	.033	.025	.022	.020		.024
1.0	28	.016	.021	.024	.025	.018	.014		.013	.014
1.0	43	.010	.014	.018	.018	.013	.007	.004	.006	.009
1.0	66	.005	.009	.016	.016	.010	.002	002	.001	. 004
1.0	82	.002	.008	.012	.013	.009	.003	003	001	.002
1.0	-1.02	.002	.007	.012	.013	.008	001	004	003	.002
1.0	-1.27		.006	.011	.011	.009	001	004	003	000
1.0	-1.59	001	.004	.010	.012	.008	002	007	004	002
1.0		002	.003	.009	.010	.007	001	006	007	002
1.0		001	.003	.007	.012	.008	.001	008	008	002
1.0		003	.000	.006	.009	.008	.000	008	008	004
1.0		003	.000	.007	.012	.010	001	008	010	005
1.0		003	.001	.006	.012	.010			009	
1.0		002	.000	.004	.010	.009	.004	004	007	005
1.0		001	.001	.005	.011	.010	.004	003	007	006
1.0	-8.20		.000	.005	.010	.011	.006		005	
1.0		001	000	.005	.009	.009	.006		004	
1.0			000	.004	.008	.009	.006		004	
	-11.66		001	.003	.007	.008	.006	.000		004
	-12.81		002	.002	.006	.007	.005		004	
	-13.97			.003	.007	.008			003	

Table D.8 - Compact Probe \tilde{v} (x/ θ_0 =1.0)

	τ	Jnforce	ed	Pha	se ave	eraged	data (at angle ϕ) 180.0 225.0 270.0 315.0				
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0	
1.0	. 55	.0060	.0091	.0096	.0089	.0179	.0209	.0167	.0119	.0092	
1.0		.0061						.0185			
1.0	.18	.0126	.0156	.0154	.0156	.0184	.0277	.0242			
1.0	00	.0561						.0550			
1.0	15	.0615	.0583	.0600	.0563	.0576	.0611	.0648			
1.0	28	.0457	.0443	.0444	.0430	.0427	.0468	.0480	.0457		
1.0	43	.0412	.0409	.0408	.0395	.0402	.0402	.0405	.0429	.0416	
1.0		.0391	.0400					.0395	.0412		
1.0	82	.0402	.0383	.0394	.0385	.0406	.0390	.0406	.0392		
1.0								.0391		.0389	
1.0		.0396						.0387		.0391	
1.0	-1.59	.0401	.0401	.0396	.0383	.0383	.0409	.0397	.0408	.0377	
1.0								.0386		.0395	
1.0	-2.46	.0398	.0385	.0391	.0396	.0393	.0401	.0400	.0401		
1.0	-3.06	.0393	.0395	.0384	.0388	.0387	.0400	.0402	.0401	.0393	
1.0	-3.81	.0381	.0384	.0386	.0381	.0371	.0371	.0384	.0403	.0385	
1.0	-4.74	.0373	.0365	.0359	.0364	.0364	.0355	.0367	.0368	.0363	
1.0	-5.89			.0325	.0330	.0329	.0323	.0326	.0331	.0327	
1.0	-7.05	.0286	.0285	.0274	.0274	.0274	.0278	.0287	.0292	.0290	
1.0	-8.20		.0228	.0217	.0210	.0205	.0211	.0226	.0225		
1.0	-9.36	.0157	.0154	.0151	.0160	.0156	.0159	.0156	.0146	.0156	
1.0	-10.51	.0100	.0100	.0093	.0098	.0093	.0097	.0104	.0097	.0108	
1.0	-11.66	.0063		.0063		.0062	.0058	.0063	.0071	.0063	
	-12.81			.0047			.0048	.0052	.0049	.0050	
	-13.97	.0041	.0041	.0040	.0040	.0039	.0039	.0040	.0041	.0042	

Table D.9 - Compact Probe $\overline{u'v'}$ $(x/\theta_0=1.0)$

		Unforc	ed	Ph.	ase av	eraged	data	(at an	gle φ)	
x/θ 0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
1.0	. 55	.0005	.0006	.0008	.0003	.0011	.0016	.0013	.0009	.0007
1.0	. 37	.0003	.0007	.0007	.0003	.0008	.0021	.0012	.0008	.0006
1.0	.18	.0007	.0012	.0013	.0013	.0011	.0026	.0018	.0015	.0014
1.0	00	.0186	.0175	.0212	.0211	.0192	.0205	.0181	.0208	.0196
1.0	15	.0188	.0141	.0194	.0174	.0172	.0202	.0235	.0196	.0197
1.0	28	.0139	.0127	.0134	.0111	.0122	.0167	.0149	.0131	.0167
1.0	43	.0142	.0140	.0121	.0118	.0137	.0145	.0127	.0163	.0141
1.0	66	.0133	.0130	.0127	.0129	.0134	.0136	.0132	.0151	.0119
1.0	82	.0148	.0140	.0136	.0133	.0153	.0143	.0149	.0146	.0140
1.0	-1.02	.0146	.0147	. 0145	.0137	.0148	.0154	.0153	.0136	.0129
1.0	-1.27	.0144	.0144	.0139	.0123	.0135	.0158	.0150	.0154	.0135
1.0	-1.59	.0144	.0132	.0130	.0120	.0129	.0147	.0127	.0146	.0136
1.0.	-1.98	.0143	.0143	.0132	.0133	.0124	.0139	.0142	.0160	.0138
1.0	-2.46	.0143	.0129	.0124	.0131	.0125	.0134	.0153	.0150	.0146
1.0	-3.06	.0140	.0137	.0130	.0140	.0130	.0146	.0149	.0152	.0136
1.0	-3.81	.0136	.0143	.0143	.0126	.0116	.0121	.0145	.0152	.0137
1.0	-4.74	.0126	.0123	.0108	.0118	.0119	.0122	.0123	.0129	.0128
1.0	-5.89	.0108	.0101	.0094	.0101	.0099	.0099	.0103	.0099	.0100
1.0	-7.05	.0076	.0075	.0074	.0069	.0072	.0073	.0074	.0077	.0082
1.0	-8.20	.0038	.0037	.0035	.0033	.0029	.0034	.0036	.0038	. 0034
1.0	-9.36	.0014	.0014	.0013	.0013	.0012	.0015	.0014	.0010	.0016
1.0	-10.51	.0004	.0004	.0003	.0003	.0002	.0005	.0003	.0003	.0004
1.0	-11.66	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0001	.0000
1.0	12.81	.0001	.0000	.0001	.0000	.0000	.0001	.0001	.0000	.0001
1.0 -	13.97	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000	.0000

Table D.10 - Compact Probe \overline{u} (x/ θ_0 =3.0)

		Unfor	ced	P	Phase averaged			data (at angle d)				
x/θ_0	y/θ_0	data	a 0.0	0 45.0	90.0	135.0	180.0	225.0	270.0	315.0		
3.0	. 5:	5 00										
										.085		
3.0							. 144	.124	.112	.117		
3.0							.213	.185	.180	.190		
3.0					.390	. 386	. 324	.280	. 288	. 296		
3.0				.468	.505	. 506	.441	.391	.382	.402		
3.0	28			.552	.578	.578	. 525		.467	.483		
3.0	43	.579	.594	.612	.644	. 649	. 597	. 556	.548	.566		
3.0	66	.638	.642	.660	.682	.687	.660	.627	.614	.623		
3.0	82	.659	.664	.675		.699	.687	.661	.648	.647		
3.0	-1.02	.680	.677	.693		.720	. 705	.683	.669	.668		
3.0	-1.27	.699	. 703			.735	.726	.702	.692	.693		
3.0	-1.59	.719				.751	.742	.727	.712	.714		
3.0	-1.98					.767	.764	.750	.734	.733		
3.0	-2.46					.789	.784	.773	.761			
3.0	-3.06					.814	.814	.804	.791	.762		
3.0	-3.81					.843	.847	.836	.824	.788		
3.0	-4.74		.862		.873	.879	.883	.874		.821		
3.0	-5.89		.904		.913	.919	.925		.863	.857		
3.0	-7.05		.942		.950	.956		.919	.909	. 904		
3.0	-8.20		.974		.979	.982	.962	.957	.948	. 942		
3.0	-9.36	.995	.992	.993	.997		.989	.986	.979	.976		
	-10.51					1 004	1.004		.998	.993		
	-11.66				1.001 1.001	1.004	1.008		1.005			
	-12.81		1 000	1 000	1.001	1.004	1.008	1.009	1.007	1.003		
		1 002	1.001	1.000	1.001 1.002	1.004	1.00/	1.009	1.007	1.003		
3.0	- 13.31	1.002	1.002	T.00T	1.002	1.004	1.007	1.009	1 008 ¹	1 ሰሰፊ		

Table D.11 - Compact Probe \tilde{u} (x/ θ_0 =3.0)

		Unforc	eđ	Ph	ase av	eraged	data	(at an	gle φ)	
x/θ 0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
3.0										.0396
3.0	. 37	.0630	.0659	.0773	.0748	.0749	.0737	.0662	.0620	.0651
3.0		.0899	.0975	.0987	.0974	.0981	.0998	.0917	.0905	.0910
3.0	00	.1068	.1128	.1150	.1057	.1108	.1162	.1129	.1079	.1114
3.0	15	. 1150	.1157	.1146	.1055	.1114	.1270	.1221	.1173	. 1174
3.0	28	.1107	.1076	.1051	.0960	.1029	.1178	.1251	.1181	.1119
3.0	43	.0971	.0901	.0846	.0827	.0838	.1027	.1121	.1094	.0984
3.0	66	.0804	.0770	.0764	.0734	.0740	.0804	.0897	.0850	.0817
3.0	82	.0763	.0742	.0730	.0705	.0709	.0738	.0771	.0770	.0800
3.0	-1.02	.0734	.0719	.0734	.0703	.0689	.0725	.0746	.0748	.0731
3.0	-1.27	.0724	.0696	.0712	.0694	.0698	.0684	.0720	.0725	.0718
3.0	-1.59	.0713	.0697	.0696	.0706	.0686	.0682	.0704	.0717	.0710
3.0	-1.98	.0692	.0704	.0672	.0673	.0654	.0671	.0676	.0712	.0680
3.0								.0663		
3.0	-3.06	.0656	.0642	.0668	.0641	.0629	.0657	.0654	.0659	.0660
3.0	-3.81	.0637	.0629	.0646	.0626	.0608	.0604	.0646	.0638	.0644
3.0	-4.74	.0603	.0602	.0604	.0596	.0612	.0593	.0576	.0606	.0619
3.0	-5.89	.0552	.0552	.0545	.0553	.0553	.0524	.0549	.0552	.0546
3.0	-7.05	.0467	.0466	.0463	.0460	.0451	.0437	.0451	.0476	.0479
3.0	-8.20	.0354	.0342	.0348	.0333	.0344	.0319	.0339	.0354	.0351
3.0	-9.36	.0209	.0217	.0227	.0177	.0189	.0188	.0196	.0208	.0224
3.0	-10.51	.0107	.0119	.0102	.0097	.0103	.0106	.0103	.0109	.0104
3.0	-11.66	.0071	.0072	.0071	.0072	.0075	.0076	.0071	.0075	.0081
	-12.81			.0058	.0058	.0059 ·	.0056	.0057	.0063	.0060
3.0	-13.97	.0052	.0053			.0052		.0054		0054

Table D.12 - Compact Probe \overline{v} $(x/\theta_0^{-3.0})$

	1	Unforce	ed	Pha	ise ave	eraged	data (at angle ϕ)				
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0	
3.0	.55	002	002	003	002	003	005	001	.001	001	
3.0	. 37	003	003	.003	.006	.000	001	001	004	001	
3.0	.18	.004	.010	.011	.023	.017	.006	.001	.001	.005	
3.0	00	.017	.025	.038	.043	.043	.017	.007	.016	.019	
3.0	15	.027	.039	. 044	.058	.051	.030	.019	.017	.023	
3.0	28	.027	.036	. 047	.057	.047	.032	.018	.023	.027	
3.0	43	.018	.029	.041	.048	.041	.023	.010	.012	.020	
3.0	66	.010	.018	.033	.042	.034	.012	001	.000	.010	
3.0	82	.007	.015	.031	.039	.030	.007	003	004	.005	
3.0	-1.02	.005	.013	.027	.037	.030	.008	007	006	.004	
3.0	-1.27	.004	.013	.022	.032	.026	.006	011	007	.002	
3.0	-1.59	.001	.010	.022	.029	.025	.002	009	010	.000	
3.0	-1.98	.000	.008	.018	.026	.021			012		
3.0	-2.46	001	.006	.015	.022	.019			011		
3.0	-3.06	003	.003	.011	.019	.016			012		
3.0	-3.81	004	.001	.008	.016	.014	.001	012	013	007	
3.0	-4.74	004	000	.006	.015	.012			012		
3.0	-5.89	004	001	.007	.012	.012			010		
3.0	-7.05	003	002	.004	.009	.011			010		
3.0	-8.20	004	002	.003	.008	.010			009		
3.0	-9.36	004	004	.002	.008	.009			008		
3.0	-10.51	004	004	.002	.006	.008			008		
3.0	-11.66	004	004	.000	.005	.007			008		
3.0	-12.81	004	005	000	.004	.006			007		
	-13.97			.000	.004	.006	.005	001	006	006	

Table D.13 - Compact Probe \tilde{v} (x/ θ_0 -3.0)

	Unforced			Ph	ase av	eraged	l data (at angle ϕ)			
x/θ 0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
3.0		.0390	.0388	.0461	.0504	.0560	.0524	.0430	.0359	.0354
3.0	. 37	.0526	.0577	. 0647	.0670	.0651	.0674	.0560	.0485	.0521
3.0	.18	. 0747	. 0807	.0868	.0854	.0833	.0806	0736	0702	07/49
3.0	00	.0864	.0942	.0973	.0948	.0951	.0907	.0869	.0845	.0882
3.0	15	.0875	.0888	.0878	.0862	.0821	.0885	.0902	.0855	.0862
3.0	28	.0770	.0749	.0741	.0697	.0727	.0777	.0809	.0757	
3.0	43	.0614	.0578	.0539	.0546	.0503	.0644	.0685	.0632	
3.0	66	.0468	. 0453	.0439	.0427	.0442		.0528	.0490	.0462
3.0	82	. 0424	.0430	.0419	.0409			.0457	.0452	
3.0		.0411		.0393	.0383	.0387	.0416	.0425	.0423	
3.0	-1.27	.0400	.0395	.0390	.0380	.0385	.0407	.0408	.0409	
3.0	-1.59	. 0402	.0396	.0388			.0406		.0403	
3.0				.0393		.0386	.0397			
3.0		.0405		.0393	.0389	.0398	.0404			.0389
3.0		.0391		.0386	.0385		.0387			
3.0		.0386		.0386	.0381	.0369	.0383	.0392		
3.0	-4.74	.0368	. 0364	.0362	.0362		.0367			.0372
3.0		.0332		.0325	.0324			.0315		
3.0	-7.05			.0272	.0274	.0264	.0272	.0283	.0284	.0284
3.0	-8.20			.0222	.0212		.0214			.0223
	-9.36					.0148	.0145	.0149		.0157
		.0098	.0103	.0096	.0087	.0093	0085	0095		.0094
3.0	-11.66	.0062	.0060	.0062	.0064	.0061	.0062	.0064		.0062
3.0	-12.81	.0048 .	.0048	. 0048	. 0047	.0048	.0048			.0048
3.0	-13.97	.0039 .	.0038	.0038	.0037	.0037	.0038			.0038

Table D.14 - Compact Probe $\overline{\mathbf{u}'\mathbf{v}'}$ $(\mathbf{x}/\theta_0=3.0)$

	,	Unforced Phase averaged y/θ_0 data 0.0 45.0 90.0 135.0					l data (at angle φ)			
x/θ 0	y/θ 0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
3.0	. 55	.0080	.0080	.0111	.0156	.0189	.0156	.0094	.0081	.0056
3.0	.37	.0180	.0194	.0306	.0318	.0299	.0292	.0185		
3.0		.0390	.0498	.0538	.0539			.0351		.0395
3.0		.0547		.0753	.0597	.0606	.0611	.0576		
3.0	15	. 0542	.0543	.0565	.0490	.0450	.0611	.0582	.0562	
3.0	28	. 0395	.0344	.0418	.0311	.0343	.0397	.0515	.0391	
3.0	43	.0250	.0216	.0196	.0200	.0141	.0238	.0290	.0258	
3.0	66	.0152	.0144	.0130	.0096	.0137	.0167	.0202		.0154
3.0		.0146	.0129	.0122	.0118	.0117	.0154	.0145		.0165
3.0	-1.02	.0144	.0118	.0115	.0119	.0095	.0133	.0165	.0155	.0139
3.0	-1.27	.0141	.0128	.0117	.0118	.0129	.0138	.0137		.0141
3.0		.0143		.0135	.0118	.0129	.0134	.0147	.0157	.0128
3.0	-1.98	.0139	.0140	.0131	.0115	.0108	.0134	.0136	.0146	.0127
3.0	-2.46	.0144	.0136	.0132	.0116	.0132	.0135	.0145	.0136	.0136
3.0		.0136		.0132	.0114	.0121	.0127	.0149	.0143	.0140
3.0		.0132		.0137	.0134	.0118	.0121	.0154	.0125	.0133
3.0	-4.74					.0131			.0126	.0129
3.0	-5.89				.0087	.0092	. 0084	.0096	.0104	.0107
3.0	-7.05		.0065	.0062	.0063	.0068	.0061	.0062	.0075	.0070
3.0	-8.20		.0037	.0040		.0037		.0036	.0044	.0036
	-9.36		.0014		.0009	.0012	.0011	.0012	.0011	.0015
		.0003 .	.0005	.0003	.0002	.0002	.0001			.0002
			0001			.0001				.0000
		. 0000 .					.0000			.0000
3.0 -	13.97	. 0000 .	0000	.0000	.0000	.0000 .	0000	.0000	.0000	.0000

Table D.15 - Mean velocity straight wire results

	U	Inforce	d	Pha	se ave	eraged	data	(at ans	le ø)	
x/θ_0	y/θ ₀		0.0					225.0		315.0
, 0	37,0	auca	0.0	43.0	,	133.0	100.0	223.0	2,0.0	323.0
-30.0	03	.175	.151	. 144	.149	.148	.169	.168	.168	.168
-30.0	09	.377	.379	.372	.374	.377	.398	.399	.389	.394
-30.0	15	.470	.473	.468	.472	.476	.482	.484	.485	.479
-30.0	21	.515	.515	.514	.516	.522	.523	.522	.522	.517
-30.0	28	.552	.552	.551	.554	. 554	.557	.557	.557	. 555
-30.0	34	.574	.577	.578	.579	.581	.579	.583	.581	.577
-30.0	43	.595	.596	.595	.600	.601	.603	.600	.601	.599
-30.0	53	.617	.617	.621	.618	.621	.624	. 623	.622	.619
-30.0	66	. 644	.644	.644	.645	.646	.646	. 646	.646	. 646
-30.0	82	.661	.663	.668	.665	.667	.668	.669	.667	.666
-30.0	-1.02	.689	.688	.688	.687	.690	.692	.690	.688	.689
-30.0	-1.28	.707	.707	.705	.708	.712	.710	.712	.710	.708
-30.0	-1.59	.728	.724	.728	.730	.728	.733	.730	.731	.729
-30.0	-1.98	.751	.748	.751	.754	.753	.756	.753	.753	.752
-30.0	-2.46	.779	.778	.778	.782	.784	.783	.780	.780	.780
-30.0	-3.06	.805	.804	.807	.809	.811	.815	.810	.811	.809
-30.0	-3.81	.839	.845	.843	.843	.847	.849	.846	.845	.845
-30.0	-4.74	.879	.881	.881	.882	.883	.887	.885	.883	.883
-30.0	-5.89	.925	.926	.927	.928	.928	.929	.927	.928	.928
-30.0	-7.05	.961	.961	.962	.964	.964	.965	.964	.962	.963
-30.0	-8.20	.984	.985	.987	.986	.986	.988	.986	.986	.985
-30.0	-9.36	.990	.991	.992	.993	.993	.993	.991	.992	.991
	-10.51	.989	.991	.991	.992	.993	.992	.991	.991	.990
	-11.66	.990	.992	.993	.993	.994	.994	.993	.992	.992
	-12.82	.991	.991	.992	.993	.993	.993	.992	.992	.991
	-13.97	.988	.989	.990	.990	.991	.991	.990	.989	.989
	-15.12	.990	.989	.990	.991	.991	.991	.990	.989	.989
-20.0	03	. 200	.185	.175	.190	.182	.199	.184	.211	.194
-20.0	09	.324	.327	.316	.330	.329	.350	.333	.342	.341
-20.0	15	.465	.464	.462	.462	.470	.476	.472	.472	.472
-20.0	21	.519	.517	.515	.521	.522	.523	.522	.521	.518
-20.0	28	. 542	.544	.546	. 545	.547	.550	.550	.547	.548
-20.0	34	.562	.561	.563	.564	.567	.567	.561	.558	.559
-20.0	43	.582	.583	.587	.587	.586	.588	.582	.584	.582
-20.0	53	.604	.604	.606	.607	.613	.612	.609	.610	.606
-20.0	66	.629	.628	.630	.633	.638	.636	.633	.632	.631
-20.0	82	.655	.651	.657	.656	.657	.659	.654	.652	.651
-20.0	-1.02	.678	.679	.681	.681	.680	.682	.679	.679	.677
-20.0	-1.28	.699	.697	.700	.701	.705	.704	.701	.701	. 703
-20.0	-1.59	.719	.721	.725	.723	.723	.723	.725	.723	.722
-20.0	-1.98	.743	.743	.742	.751	.749	.748	.747	.746	.742
-20.0	-2.46	.773	.774	.773	.776	.777	.776	.772	.771	.770
-20.0	-3.06	.800	.802	.803	.805	.807	.806	.802	.802	.799
-20.0	-3.81	.834	.837	.835	.838	.840	.837	.837	.838	.837
-20.0	-4.74	.875	.873	.878	.879	.880	.879	.879	.875	.874
				2 - · ·						

Table D.15 (cont'd).

-20.0	-5.89	.920	.920	.921	.923	. 926	.924	.922	. 920	.920
-20.0	-7.05	.957	.959							
-20.0	-8.20	.986	. 986	.988	.988	.990	.989	.988	.987	
-20.0	-9.36	.997	.996	.998	.999	1.000	.999	.998	.996	.996
-20.0	-10.51	. 998	.998	1.000	1.001	1.001	1.001	999	.998	.997
-20.0			.996	.997	.998	.999	.999	.997	.996	.996
-20.0	-12.82	. 995	. 995	. 996	.998	.998	.998	.997	. 996	.995
-20.0			. 995	. 996	.997	. 998	.998	.997	. 996	.995
-20.0	-15.12			. 996	.997	. 998	.998	.997	. 996	. 995
-10.0	03			.141	.172	.172	.171	. 185	.173	.167
-10.0	09			. 357	. 375	. 382	. 382	. 385	. 375	.366
-10.0	15					.477	. 479	.478	.473	.468
-10.0	21		.518	.519	. 526	. 525	. 526	. 522	.517	.512
-10.0	28		. 547		.559	. 556	. 556	. 546	. 546	. 544
-10.0	34	. 565	. 562				. 573	. 567	. 565	. 562
-10.0	43		. 586	. 589		. 597	. 592	. 591	. 585	. 587
-10.0	53		.611	.614			.616	.613	. 609	. 608
-10.0	66	. 632	. 632	.635	. 641		. 640	.638	. 634	. 630
-10.0	82	. 654	. 653	. 658	. 663		.663		. 656	. 653
-10.0	-1.02	. 677	. 677	. 678	. 683	. 684	. 685		. 678	. 672
-10.0	-1.28	. 697	. 697	. 699	. 700		. 702		. 696	. 694
-10.0	-1.59	.719	.717	.720	.727		. 725		.719	.717
-10.0	-1.98	.742	.744	.746	. 750	.751	.751		. 743	. 740
-10.0	-2.46	.766	.767	.771	.773	.779	.776		.767	.764
-10.0	-3.06	.797	.798	. 800	. 802	. 805	. 804		. 796	.793
-10.0	-3.81	.832	.831	. 834	. 839	. 839	.836	.833	. 827	.828
-10.0	-4.74	.870	.870	. 872	. 878	. 877	. 878	.872	.871	.870
-10.0	-5.89	.913	.916	.916	.922	. 924	. 920	.919	. 914	.913
-10.0	-7.05	.953	.955	. 954	.957		. 960	. 956	. 954	. 955
-10.0	-8.20	.982	.986	.986	.989	.990	. 990	. 987	. 984	. 984
-10.0								1.003		. 999
	-10.51									
	-11.66							1.004		
-10.0								1.002		
-10.0		. 998	.999			1.002			.999	. 998
-10.0		.997	.998			1.001			.999	.998
-5.0	03	.167	.140	. 141		.167		.160	.153	.168
-5.0	09	.313	.313	.315	.329	.338	. 342	. 323	. 307	.325
-5.0	15	.426	. 427	.434	.442	.440	. 445	.436	.425	.428
-5.0	21	.496	.501	. 504	.510	.517	.514	. 503	.498	.498
-5.0	28	.534	.535	. 543	. 545	.550	. 544	.535	.532	. 528
-5.0	34	.560	.562	. 565	. 574	. 575	. 572	. 562	.558	.558
-5.0	43	.585	.583	.588	.595	.595	.595	.587	.582	.582
-5.0	53	.606	.605	.611	.614	.622	.613	.609	.604	.602
-5.0 -5.0	66	.627	.628	.633	.639	.644	. 642	.632	.627	.625
-5.0 -5.0	82	.650	.655	.657	.661	.664	.659	.653	. 649	. 644
-5.0	-1.02	.673	.677	.679	.681	.687	.685	.678	.677	.672
-5.0	-1.28	. 694	.693	. 699	. 706	. 706	. 704	. 698	.691	. 692

Table D.15 (cont'd).

-5.0	-1.59	. 719	.718	.722	. 729	.730	.727	.721	.715	.715
-5.0										
-5.0										
-5.0										
-5.0										
-5.0	-4.74									
-5.0	-5.89									
-5.0	-7.05									
-5.0	-8.20				.989		.991			
-5.0	-9.36	.998					1.005			
-5.0	-10.51									1.002
	-11.66					1.007				1.002
	-12.82	.999			1.003					1.002
	-12.62	.999		1.002				1.004		
		.999								
	-15.12			1.002						1.001
-1.0	03	.165 .306	.156	.144 .314	.182	.191	.179 .342	.161	.167	
-1.0 -1.0	09 15		.314		.339	.353		.321		
-1.0	13	.453 .518	.460 .523	.467	.482	.491	.475	.461		
	21			.529	. 547	. 548	.537	.518	.510	
-1.0 -1.0	28	.553 .575	.560 .578	. 566	.579	. 580	.568	. 554	.550	. 548
-1.0	43	.594	.600	. 585 . 606	.595 .619	.597 .620	.588	.572 .595	.566	.570
-1.0	43	.615	.619	.630	.643	.641	.609		.585	.594
	66		. 643			.663	.630	.617	. 608	.612
-1.0		.637		.653	.662		.655	.639	.633	.632
-1.0	82	.661	.665 .683	.673	.683	.685	.676	. 663	.657	.658
-1.0	-1.02	. 680	. 704	.689	.698	.704	.693	. 682	.675	.676
-1.0	-1.28	.700		.710	.718	.719	.710	.702	. 695	.697
-1.0	-1.59	.720	.722	.732	.739	.743	.732	.724	.717	.716
-1.0	-1.98	.743	.741	.751	.759	.764	.755	.747	.743	.740
-1.0	-2.46	.768	.771	.779	.785	.788	.779	.771	.766	.765
-1.0	-3.06	.798	.800	.808	.814	.815	.812	. 803	.797	.793
-1.0	-3.81	. 830	.830	.835	. 844	.848	. 844	.833	.828	. 828
-1.0	-4.74	.870	. 872	.871	.881	.883	.881	.873	.866	. 865 . 908
-1.0	-5.89	.912 .950	.912	.917	.921	.925	.922	.916	.911	
-1.0 -1.0	-7.05 -8.20	.930	.951 .982	.953	.958 .988	.962	.962	.956	.952 .983	. 949 . 980
		.997	.996	.985		.991	.991 1.004	.987		
-1.0	-9.36								.998	.996
1.0	-10.51 -11.66	1.001	1.000	1.002	1.003	1.006	1.006	1.006	1.003	1.000
	-12.82	.998	.999				1.004			1.000
	-13.97	.999	.998				1.003			.999
	-15.12 03	.999	.997	.997	.998		1.001			.998
.0		. 206	.185	.172	.191	.228	.215	.173	.180	.202
.0	09	.364	.374	.378	.399	.414	.398	.368	.363	.375
.0	15	.494	.508	. 524	. 535	.538	.521	.495	.486	.495
.0.		. 540	. 548	. 563	.570	.580	.561	.538	.532	.540
.0	28	.567	.575	.586	.600	.601	.585	.560	.558	.563
.0	34	. 591	. 595	. 608	.619	.621	. 603	. 584	. 582	. 583

Table D.15 (cont'd).

.0	43	. 609	.615	.628	.642	.642	. 624	.607	. 602	.602
.0										
.0										
.0									. 665	
.0									.685	
.0									.707	
.0									.731	
.0									.751	
.0									.777	
.0									.801	
.0							.855		.841	
.0							.893		.875	
.0							.936		.923	
.0							.973		.960	
.0						1.000			.994	
.0								1.011		
.0	-10.51									
.0	-11.66									
.0	-12.82									
.0	-13.97									
.0	-15.12							1.009		1.005
1.0	. 58	.051	.053	.063	.058	.072	.084	.077	.064	.056
1.0	.40		.059	.068	.059	.069	.080	.077	.066	
1.0	. 21	.056	.063	.071	.061	.066	.080	.077	.070	
1.0	.03	.067	.076	.081	.079	.086	.100	.097	.085	.079
1.0	12	.132	. 145	.151	.164	.185	.179	.168	.151	.145
1.0	25	.300	.316	.337	.366	. 391	.366	. 333	.312	. 303
1.0	40	.518	.522	. 547	.566	.580	.560	. 533	. 506	.514
1.0	63	.620	.626	.638	.652	. 657	. 645	. 625	.610	.610
1.0	79	. 652	. 653	.668	. 679	. 684	.673	. 657	. 647	. 645
1.0	99	.680	.681	. 690	. 705	.708	.698	. 683	.671	.669
1.0	-1.24	.703	. 707	.717	.729	.732	.721	.708	.698	.701
1.0	-1.56	.728	.731	.739	.749	.754	.746	.734	. 725	.724
1.0	-1.95	.753	. 753	.764	.774	.774	.769	.759	. 748	. 747
1.0	-2.43	.781	.782	. 789	. 796	.800	. 793	.781	.772	.775
1.0	-3.03	. 808	.810	.814	. 824	.827	. 823	.812	.805	.802
1.0	-3.78	. 835	.834	. 840	. 848	.850	. 846	.838	. 834	.831
1.0	-4.71	. 864	.860	.866	.873	.877	. 875	.867	.859	.860
1.0	-5.86	.877	. 878	. 884	.890	. 890	.889	.884	.879	. 878
1.0	-7.02	. 906	. 905	. 909	.914	.919	.919	.912	. 906	. 906
1.0	-8.17	. 926	.929	. 932	. 938	.941	.941	. 937	.930	.928
1.0	-9.32	. 955	.955	. 957	.960	. 964	.966	. 963	.956	.956
1.0	-10.48	.996	. 997	.997			1.006	1.004	.999	.996
1.0	-11.63	1.004		1.004		1.009				
	-12.78							1.012		
1.0	-13.94	1.006	1.005	1.005	1.006	1.008	1.010	1.011	1.009	1.007
1.0	-15.09			1.004	1.005	1.006	1.008	1.009	1.008	1.006
3.0	. 58	.100	.107	.100	.118	.138	.137	.110	.086	.090

Table D.15 (cont'd).

2.0	4.0	107	111	112	126	. 141	.141	.119	.099	.100
3.0	.40		.111 .157	.113 .169	.126 .186	.192	.177	.163	.146	.145
3.0 3.0	.21 .03	.152		.262	.285	. 281	.255	.233	.214	.218
		. 228		.335	.362	.367	.326	.298	.283	.291
3.0	12	.298		. 409	.435	.444	.400	.366	.349	.358
3.0	25	.369			.535	.534	.493	.460	.447	.454
3.0	40	.464		.511		.653	.615	.581	.566	.579
3.0	63	.591	.607	.620			.666	.637	.628	.632
3.0	79	. 642	.657	.665	.687			.678	.661	.662
3.0	99	.675	.683	.687	.714	.719	.700	.704	.692	.689
3.0	-1.24	.702	.703	.714	.732	.737	.723	.704	. 720	.717
3.0	-1.56	.726	.729	.736	.751	.759	.744 .769	.758	.745	.743
3.0	-1.95	.752	. 749	.757	.771	.781		.736		.743
3.0	-2.43	.774		.783	.798	.802	.795		.771	.801
3.0	-3.03	.803	.805	.812	.817		.818	.811	. 800	
3.0	-3.78	.830	.830	.838	.844		.847	. 840	.828	.827
3.0	-4.71	. 846	. 847	.850	.858	.862	.858	.855	. 846	.841
3.0	-5.86	. 904	. 904	. 906	.914		.920	.916	.908	.902
3.0	-7.02	. 934		. 938	.939	.947	.946	.942	.938	.933
3.0	-8.17	.987		.989	.991		.998	.996	.991	.988
3.0	-9.32	1.001	.999			1.007				1.000
3.0	-10.48	1.009	1.010	1.009	1.011	1.014	1.01/	1.01/	1.015	1.012
3.0	-11.63			1.009	1.010	1.012	1.015	1.01/	1.013	1.012
3.0	-12.78	1.008							1.013	
3.0	-13.94			1.006	1.006	1.00/	1.010	1.012	1.011	1.009
3.0	-15.09								1.008	
5.0	2.00	.085	.053	.108	.130	.138	.112	.069	.039	.030
5.0	1.01	.093	.059	.107	.137	. 144	.118	.089	.066	.055
5.0	.03	. 329	. 365	. 381	. 407	.405	. 349	. 329	.319	. 333
5.0	96	. 688	. 679	.689	. 703	.715	. 707	.687	.671	. 670
5.0	-1.94	.777	. 768	.778	. 784	. 795	.799	.791	.780	.772
5.0	-2.93	.821	. 816	.823	. 828	. 834	.841	.835	. 824	.818
5.0	-3.92	. 874	. 867	. 872	. 878	. 884	.891	.885	.877	.871
5.0	-4.90	. 909	. 904	.907	.915	.920	.925	.921	.912	. 906
5.0	-5.89	. 950	. 946	.949	.952	. 956	.960	.960	.956	.950
5.0	-6.88	.976	. 973	. 974	.978	.983	.988	.989	.982	.976
5.0		1.000	. 996	. 996	.998			1.008		.998
5.0	-8.85	1.007	1.004		1.004			1.014		1.008
5.0	-9.84	1.008	1.006	1.005	1.006	1.007	1.013	1.015	1.013	1.009
5.0	-10.82	1.007	1.005	1.004	1.004	1.006	1.011	1.014	1.012	1.009
5.0	-11.81	1.006	1.005	1.003	1.003	1.005	1.009	1.012	1.011	1.008
5.0	-12.79	1.004	1.004	1.001	1.001	1.003	1.007	1.010	1.009	1.007
	-13.78				1.000	1.002	1.005	1.009	1.008	1.006
	-14.76			.999		1.000	1.003	1.006	1.006	1.004
	-15.75			.999	.998				1.006	
	-16.74			.999	. 998				1.005	
5.0	-17.72			.999	.998				1.005	
10.0	4.00		.032	.032	.043	.044	.056	.063	.048	.037
10.0	2.87	.041	.033	. 034	.048	. 048	.062	.067	. 047	.037

Table D.15 (cont'd).

10.0 1.	75 .065 .06:	2 .073	.085	. 095	.096	.091	067	.063
10.0	. ,	3 .270	. 304	.313	. 306	. 247		
10.0	51 .555 .55	3 .587	.611	. 624	.629	. 556		
10.0 -1.		7 .734	. 750	. 753	.778	.768	.752	
10.0 -2.		L .797	. 806	.812	. 834	.836		
10.0 -3.8			.860	. 864	.883	. 884		
10.0 -5.0	01 .909 .902	.899	. 904	. 909	.924	. 929		
10.0 -6.1			. 946	. 949	.960	.969		
10.0 -7.2			.977	. 980	.992	1.000		
10.0 -8.3			. 992	.994				1.003
	51 1.003 1.001		. 996					1.008
	54 1.004 1.002		.996					1.009
	77 1.002 1.002		.996				1.012	
	39 1.001 1.002		.995					1.007
	2 1.001 1.001		.994	. 995			1.008	
	.5 .999 1.001		. 994	.994			1.007	
	.998 1.000		. 993	.994	. 997	1.003	1.006	1.004
10.0 -17.4			.993	. 993			1.004	
10.0 -18.5		. 997	. 994	. 994			1.004	
15.0 6.0		.029	.026	.035	.040	.057	.067	.053
15.0 4.7		.029	.028	.039	.043	.063	.073	.053
15.0 3.4	7 .042 .038	.037	.040	.052	.055	.077	.085	.056
15.0 2.2		.088	.107	.125	.136	.123	.116	.082
15.0 .9		. 257	. 302	.331	.334	. 297	.252	.215
15.03		. 502	. 559	. 575	. 579	.563	.474	.449
15.0 -1.6		.714	.730	.753	.757	. 783	. 714	.691
15.0 -2.8		. 793	. 803	.814·	.824	.857	.832	. 804
15.0 -4.1		.852	.859	.869	.878	. 904	.891	. 865
15.0 -5.4		. 902	.906	.918	.929	. 947	.943	.921
15.0 -6.6		.949	. 949	.957	.969	. 985	.983	.967
15.0 -7.9		.979	.977	.982	.991	1.007	1.011	.999
	9 1.004 1.001	.993	.989	.992	.999	1.013	1.021	1.013
	6 1.004 1.005	. 996	.992				1.020	
	3 1.006 1.006	. 997	. 993	.994	1.000	1.011	1.018	1.015
	9 1.004 1.006	. 998	. 994	. 994	.999	1.009	1.016	1.014
	5 1.002 1.006	. 998	.993	.993	.997	1.006	1.013	1.012
	3 1.001 1.005	.998	.993	.992	.996	L.004	1.011	1.011
	9 1.001 1.005	. 998	. 994	.992	.995	L.003	1.009	1.010
15.0 -18.06		. 999	.994	.993	.995 1	L.002	1.007	1.009
	2 1.000 1.004	. 998	. 994	.992	.994 1	1.000	1.005	1.007
25.0 10.00		.063	. 044	.028	.023	.034	.053	.073
25.0 8.45		.066	.044	.027	.024	.038	.058	.081
25.0 6.91		.070	.044	.030	.032	. 045	.066	.093
25.0 5.36	·	.078	.050	.042	.051	.061	.077	.111
25.0 3.81		.095	.079	.092	.111	.125	.121	.139
25.0 2.27		.160	.175	.216	. 247	. 270	. 245	.212
25.0 .72		. 299	. 350	.415	.455	.479	.447	. 384
25.082	.572 .504	.496	. 555	.613	.666	.675	.681	.595

Table D.15 (cont'd).

25.0										
25.0										
25.0										.971
25.0								. 970		1.010
25.0			1.008						1.014	
25.0								. 993	1.014	
	-11.65								1.011	
	-13.19		1.017						1.006	
	-14.74		1.014				.982	.989	1.002	1.015
	-16.29		1.011				. 982	.988	1.000	1.011
	-17.83		1.010				. 984	.989	.998	1.009
	-19.38		1.007				.984	.988	.996	1.005
	-20.92		1.002		.990	.983	.981	.983	.990	.999
40.0	16.00	. 034	. 055	.078	.087	.081	065	. 045	.025	.027
40.0	14.03	.034	.063	.089	. 098	.089	.070	. 047	.026	.033
40.0	12.07	. 034	.077	.107	.115	. 102	.077	.051	.032	.044
40.0	10.10	.036	. 095	.129	.136	.117	.087	. 059	.044	.061
40.0	8.13	.041	. 108	. 148	.161	. 135	.101	.072	.066	.084
40.0	6.17	.060	.125	.164	. 195	.162	.122	. 104	.113	.127
40.0	4.20	.130	.212	.219	. 249	. 204	.165	.185	.213	. 240
40.0	2.24	. 264	. 374	. 343	. 334	.271	. 261	.317	.379	.432
40.0	. 27	.453	. 599	. 525	.462	. 397	.403	.490	. 574	. 626
40.0	-1.70	.661	.811	.727	.620	. 555	. 590	.662	.733	.776
40.0	-3.66	. 825	. 936	.890	. 774	.727	. 754	.787	.836	.869
40.0	-5.63	.917	. 997	1.007	.915	.855	.855	.872	. 906	.937
40.0	-7.60	. 977	1.033	1.055	. 997	. 942	.924	.930	.951	.977
40.0					1.034		.960	. 954	.965	. 987
40.0	-11.53	1.003	1.028	1.057	1.037	. 998	.972	. 964	.970	.989
		1.002	1.021	1.044	1.033	1.003	.980	.971	. 974	.989
					1.026			.973	.975	.988
	-17.42				1.020			.977	.977	.987
	-19.39	. 998			1.015	1.001	. 987	.978	.978	. 986
	-21.36	.992	.994	1.007	1.008	.998	.985	.976	.974	.981
40.0	-23.32	.994	. 997	1.007	1.007	.999	.989	.982	.981	.986
	24.00	.036	.043	.028	.028	. 048	. 065	.072	.069	.058
60.0	21.47	.035	. 044	.027	.030	.054	. 074	.081	.076	.063
60.0	18.95	.035	. 049	.031	.038	.066	.088	.094	.087	.070
60.0	16.42	.035	.058	.042	.055	. 084	.108	.113	.102	.081
60.0	13.90	.036	.073	.061	.080	. 109	.132	.138	.122	.097
60.0	11.37	.041	.097	.090	.112	.128	.157	.167	.148	.120
60.0	8.84	.061	.132	.139	.156	.134	.172	. 205	.186	.154
60.0	6.32	.118	. 200	. 233	. 245	.182	.230	. 268	. 244	. 205
60.0	3.79	. 237	.310	.377	. 396	. 339	.358	.363	.320	. 284
60.0	1.26	. 396	.452	. 548	. 597	. 551	.518	.482	.414	. 394
60.0	-1.26	. 590	.630	. 709	.779	.747	.675	.604	.531	. 529
60.0	-3.79	.781	. 774	.825	.899	. 906	.822	. 734	.671	. 702
60.0	-6.31	.922	. 872	. 904		1.030	.950	.861	.824	.839
60.0	-8.84	. 988	.911	.930	1.001	1.081	1.047	.976	.934	.914

Table D.15 (cont'd).

60 0	-11.37	.999	. 931	0/.6	1 002	1.074	1 000	1 020	. 975	. 940
	-13.89		.941			1.051				.952
	-16.42					1.031			. 985	.960
		. 994	. 949							
	-18.95	.994	. 957			1.022			.987	.966
	-21.47	.986	.957			1.006			. 985	. 966
	-24.00	. 988	.963			1.001			. 986	.972
	-26.52	.981	. 962					.992	.980	. 968
	-15.47		.977				1.015			
	-13.86		. 972				1.022			
	-12.24		. 964				1.029			
76.9	-10.63	.999	. 943				1.031			. 979
76.9	-9.01	.981	. 890				1.030		.978	.913
76.9	-7.40	. 938	. 823	. 846	.860	.901	1.010	1.000	. 923	. 854
76.9	-5.78	. 862	. 749	.776	. 825	.874	.970	. 942	. 870	. 795
76.9	-4.17	.770	. 678	. 699	.775	.835	.914	. 882	.813	. 735
76.9	-2.55	. 664	.615	.613	.702	.774	.841	. 807	.752	. 683
76.9	94	.559	. 556	. 537	.617	.701	.750	.722	. 670	.614
76.9	.68	.457	.496	.468	. 528	. 619	. 662	. 630	. 588	.547
76.9	2.30	.366	.439	.403	.438		.561	. 529	. 505	.477
76.9	3.91	.281	.377				.451	.422	.424	.410
76.9	5.53	. 203	. 321				.351	.302	.330	. 340
76.9	7.14	.149	. 270		. 245		.271	. 209	. 245	. 276
76.9	8.76	.099	.225			.213	.214	.154	.183	.227
76.9	10.37	.070	.190				.172	.138	.151	.192
76.9	11.99	.052	.165			.128	.141	.131	. 142	.167
76.9	13.60	.045	.143		.110		. 114	.123	.132	.149
76.9	15.22	.040	.125			.078	.086	.107	.124	.132
76.9	16.83	.038	.112		.077	.063	.071	.093	.112	.120
115.4	23.58	.040	.054		.063	.077	.086	.086	.079	.066
115.4	21.37	.042	.066		.071	.086	.096	.097	.092	.081
115.4	19.17	.042	.081		.083	.098	.110	.115	.111	.098
115.4	16.97	.055	.104		.094	.112	.128	.135	.134	.124
115.4		.073	.133		.113	.112	.152	.164	.168	.157
	14.77									
115.4	12.57 10.37	.101	.171		.134	.160 .208	.193	.207	.210	.199
115.4		.148	. 222	.183	.173		. 241	.252	. 257	. 250
115.4	8.17	. 205	.281	. 242	. 248	. 292	.305	.304	.309	.308
115.4	5.97	. 283	.361	. 337	.359	. 394	.387	. 374	.378	.386
115.4	3.77	.360	.451	. 464	.485	.499	.472	.444	. 442	.454
115.4	1.56	.448	.550	. 565	.567	. 556	.519	.509	.517	.542
115.4	64	. 547	.651	. 657	.653	.618	.585	. 577	. 593	. 633
115.4	-2.84	. 658	. 748	.760	.761	.713	.656	. 645	.659	.711
115.4	-5.04	.771	.830	. 826	.820	.768	.727	.720	.743	.777
115.4	-7.24	.867	. 899	. 892	.880	.827	. 792	.787	. 804	.821
115.4	-9.44	. 947	. 944	.957	.931	. 884	.852	. 847	. 845	. 854
	-11.64	. 985		1.008	.983	.944	.914	.899	.873	.880
	-13.84	.992		1.044		.993	.959	. 925	.891	.901
	-18.25	.992		1.037			.993	. 947	. 920	.930
115.4	-18.25	. 990	.980	1.037	1.059	1.037	. 993	. 947	.920	. 930

Table D.15 (cont'd).

115 /	00 /5	000	070	1 006	1 0/7	1 020	000	050	006	022
	-20.45	. 990				1.030	.992		.926 1.011	
	-28.62	.979	.982	.960	.948	. 953	.974			
	-25.51	.982	. 987	. 958	. 941	. 947			1.025	
	-22.41	.985	.990	.955	.933	.941			1.040	
	-19.30	.992	.982	. 948	.922	. 934			1.036	
153.8	-16.19	.993	. 948	.929	. 908	.919			1.002	.976
153.8	-13.09	.982	. 890	.883	.877	. 894	.959	. 966	. 947	.911
153.8	-9.98	.924	. 822	. 824	.837	. 860	.903	.893	.870	.843
153.8	-6.87	.820	. 749	.744	.768	. 802	.817		.799	.772
153.8	-3.76	.703	.688	.671	. 684	.719	. 710	.724	.727	.715
153.8	66	.576	.599	. 592	. 602	.613	. 584	. 604	.629	.626
153.8	2.45	.457	.514	.513	. 525	.521	.472	.467	.495	.516
153.8	5.56	.353	.442	.443	.446	.436	. 388	.355	.378	.420
153.8	8.66	.271	. 343	.367	. 376	.365	.316	. 272	. 273	. 310
153.8	11.77	.195	.273	. 298	.312	. 306	.271	. 228	.216	. 237
153.8	14.88	. 133	.219	.236	. 254	. 254	. 231	. 203	.190	.200
153.8	17.98	. 090	.176	. 190	. 200	. 201	.185	.168	.160	.166
153.8	21.09	.062	. 153	.158	.165	.166	.159	. 146	.143	.148
153.8	24.20	.050	.130	.132	.135	.131	.124	.117	.119	.125
153.8	27.30	. 045	.110	.110	.109	.104	.099	.097	.100	.105
153.8	30.41	.044	.091	.090	. 090	.085	.082	.081	.084	.088
153.8	33.52	.043	.077	.077	. 074	.070	.067	.067	.071	. 075
192.3	43.46	.045	.069	.070	.071	.073	.075	.075	.073	.070
192.3	39.45	.046	.083	. 084	.086	.088	.089	. 089	.088	.086
192.3	35.43	. 047	. 114	.113	.112	.113	.117	.118	.118	. 117
192.3	31.42	.051	. 146	.143	. 141	. 145	. 148	.151	.154	.151
192.3	27.41	.060	. 194	. 184	.180	.181	.187	.194	.196	.197
192.3	23.40	.082	. 221	. 209	. 203	. 208	. 215	. 226	. 232	. 230
192.3	19.38	.116	. 260	. 244	. 235	. 240	. 250	. 267	. 274	. 275
192.3	15.37	.182	. 304	. 279	. 270	.275	. 297	.322	.338	. 332
192.3	11.36	. 253	. 341	. 308	. 302	.323	.351	.386	.403	. 383
192.3	7.35	. 349	. 385	. 349	. 353	. 396	. 434	.459	.470	. 444
192.3	3.33	.460	.439	.420	. 448	.488	.513	. 532	.530	. 500
192.3	68	. 585	. 550	. 554	. 586	.599	.601	. 605	.610	. 589
192.3	-4.69	.715	. 686	.701	. 707	.710	.698	. 689	. 696	.701
192.3	-8.70	. 843	. 806	.811	.812	. 792	.772	.767	.787	.810
192.3	-12.72	. 941	. 902	. 894	.886	.863	.841	.837	.852	.886
192.3	-16.73	.982	.963	. 964	. 949	.925	. 904	. 894	. 897	.925
192.3	-20.74	.990	. 989	1.011	1.000	.979	.953	.932	.922	. 943
192.3	-24.75	.982	. 989	1.017	1.019	1.000	. 975	. 949	.937	. 952
192.3	-28.77	.979	.984	1.009	1.016	1.002	.979	. 957	. 948	. 958
192.3	-32.78	.985	.990	1.006	1.010	1.001	.984	.968	.963	.971
192.3	-36.79	.985		1.000		.997	.984	.972	.968	.974
	-44.97	.985	.981	.977	.977	.983	.991	.996	.995	.989
	-40.05	.985	.982	. 975	.975	.982		1.001		.992
	-35.13	.987	.982	.970	.969	.980		1.008		.996
	-30.21	.983	.971	.958	.957	.974		1.010		.988
	-25.29	.986	.948	.939	. 940	.966		1.004	.991	.969

Table D.15 (cont'd).

230.8	-20.37	. 987	.916	.913	.923	.952	. 975	.973	. 957	. 936
230.8	-15.46	.956	.864	.868	.888	.914	.917	.914	.895	.876
230.8	-10.54	.862	.794	.803	. 824	. 825	.826	.824	.815	.797
230.8	-5.62	.733	.715	.722	.725	.710	.698	.708	.710	.715
230.8	70	. 593	. 625	.638	. 633	. 593	.564	.574	. 592	.609
230.8	4.22	.470	. 540	.561	.558	.512	.464	.449	.473	. 508
230.8	9.14	.359	.462	.484	.488	.461	.414	. 389	.401	.432
230.8	14.06	. 257	. 396	.419	.429	.407	. 374	. 352	.351	.371
230.8	18.97	.165	. 339	. 359	. 363	. 353	. 329	. 311	. 311	.319
230.8	23.89	. 114	. 289	. 297	. 303	. 303	.288	.278	. 277	. 279
230.8	28.81	.075	. 239	. 243	. 247	. 246	.235	.232	.230	. 231
230.8	33.73	.061	.195	.199	. 200	.199	.194	.189	.188	.188
230.8	38.65	.053	.150	.151	.154	.151	.149	.146	. 147	.148
230.8	43.57	.050	.110	.112	.111	.110	.109	.109	.109	.110
230.8	48.48	.049	.089	.089	.089	.087	.088	.087	.087	.088

Table D.16 - RMS velocity straight wire results

	Unforced			Phase averaged			data (at angle ϕ)			
x/θ_0	y/θ_0							225.0		
·	v				0.506	05/5	0651	0611	0677	0660
-30.0		.0739								
-30.0	09			.1064		.1042			.1056	
-30.0	15			.1024		.1002			.0998	
-30.0	21			.0960		.0967			.0924	
-30.0	28			.0887		.0886		.0869		
-30.0	34			.0843		.0829			.0835	
-30.0	43			.0825		.0830			.0817	
-30.0	53			.0798					.0798	
-30.0	66			.0767		.0774			.0778	
-30.0	82		.0771			.0764			.0756	
-30.0	-1.02	.0770				.0746			.0766	
-30.0	-1.28		.0745			.0749			.0732	
-30.0	-1.59	.0737				.0735			.0732	
-30.0	-1.98			.0724		.0712			.0700	
-30.0	-2.46			.0707	.0708	.0675		.0670	.0680	
-30.0			.0662		.0686	.0650		.0628	.0637	
-30.0	-3.81					.0604		.0586	.0593	
-30.0 -30.0	-4.74 -5.89					.0515			.0488	
-30.0				.0510		.0373		.0367	.0388	
-30.0	-7.05 -8.20			.0388		.0226			.0210	
						.0226			.0103	
-30.0	-9.36			.0110					.0103	
	-10.51			.0061		.0082		.0078	.0060	.0078
	-11.66			.0056		.0058		.0056		.0055
	-12.82 -13.97					.0056		.0055		.0056
	-15.12					.0054		.0054		.0054
-20.0	03				.0034	.0671		.0692	.0822	
-20.0	03				.0995	.0982		.1007	.1023	
-20.0	15			.1015		.0991			.1023	
-20.0	21				.0891	.0918		.0940	.0931	
-20.0	28		.0869		.0863		.0889	.0867		.0882
-20.0	34		.0826		.0849					.0872
-20.0	43	.0829	.0826		.0823		.0822	.0812	.0830	.0818
-20.0	53			.0812			.0811	.0802	.0811	.0799
-20.0	66			.0782			.0793	.0791		.0769
-20.0	82	.0780	.0766		.0762		.0770	.0784		.0755
-20.0	-1.02		.0781		.0754		.0781	.0760	.0751	.0751
-20.0	-1.28				.0737		.0749	.0760	.0768	.0751
-20.0	-1.59				.0727		.0739	.0750	.0742	.0728
-20.0	-1.98				.0714		.0693	.0743	.0710	.0728
-20.0	-2.46		.0692		.0684			.0701	.0704	.0679
-20.0	-3.06		.0681		.0683	.0685	.0672	.0666	.0703	.0677
-20.0	-3.81				.0636		.0649	.0652	.0652	.0631
-20.0	-4.74	.0607	.0591		.0610	.0607		.0597	.0595	.0606
• •							· · · - -			

Table D.16 (cont'd).

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-5.89 .0533 .0522 .0542 .0524 .0513 .0543 .0546 .0529 .0529
-20.0
-20.0
       -7.05 .0429 .0420 .0442 .0420 .0408 .0414 .0421 .0418 .0424
-20.0
       -8.20 .0267 .0257 .0265 .0271 .0280 .0280 .0269 .0263 .0274
-20.0 -9.36 .0139 .0150 .0132 .0143 .0142 .0142 .0145 .0147 .0139
-20.0 -10.51 .0085 .0088 .0086 .0083 .0082 .0091 .0087 .0084 .0087
-20.0 -11.66 .0069 .0067 .0066 .0067 .0068 .0067 .0074 .0067 .0068
-20.0 -12.82 .0063 .0058 .0057 .0055 .0057 .0056 .0057 .0056
-20.0 -13.97 .0056 .0057 .0057 .0057 .0056 .0057 .0056 .0057
-20.0 -15.12 .0059 .0055 .0054 .0055 .0054 .0054 .0054 .0055 .0054
-10.0
        -.03 .0603 .0563 .0441 .0591 .0584 .0576 .0640 .0599 .0576
-10.0
        -.09 .1023 .1043 .0998 .1021 .1039 .1045 .1042 .1049 .1032
-10.0
        -.15 .0999 .0980 .0987 .0975 .0987 .1012 .0998 .0984 .1014
-10.0
        -.21 .0923 .0931 .0913 .0919 .0925 .0931 .0917 .0926 .0911
-10.0
        -.28 .0869 .0851 .0876 .0874 .0876 .0863 .0842 .0855 .0882
-10.0
        -.34 .0841 .0851 .0854 .0842 .0848 .0833 .0832 .0839 .0844
-10.0
        -.43 .0808 .0796 .0813 .0806 .0808 .0815 .0806 .0832 .0816
-10.0
        -.53 .0796 .0808 .0790 .0773 .0778 .0792 .0818 .0810 .0801
-10.0
        -.66 .0784 .0793 .0783 .0786 .0747 .0788 .0767 .0789 .C808
-10.0
        -.82 .0763 .0774 .0797 .0776 .0744 .0761 .0777 .0767 .0764
-10.0
       -1.02 .0758 .0751 .0759 .0744 .0766 .0751 .0766 .0772 .0766
-10.0
       -1.28 .0745 .0740 .0746 .0730 .0744 .0734 .0761 .0730 .0753
-10.0
      -1.59 .0735 .0731 .0730 .0726 .0707 .0715 .0723 .0713 .0733
-10.0
       -1.98 .0704 .0715 .0712 .0690 .0700 .0707 .0707 .0712 .0698
-10.0
       -2.46 .0694 .0716 .0693 .0677 .0681 .0679 .0689 .0702 .0702
-10.0
       -3.06 .0677 .0672 .0680 .0657 .0655 .0664 .0667 .0658 .0677
-10.0
      -3.81 .0642 .0632 .0648 .0631 .0633 .0642 .0640 .0639 .0654
-10.0
       -4.74 .0610 .0604 .0618 .0604 .0610 .0593 .0609 .0607 .0624
-10.0
      -5.89 .0541 .0539 .0559 .0534 .0542 .0528 .0527 .0547 .0543
-10.0
      -7.05 .0451 .0438 .0461 .0457 .0439 .0446 .0442 .0453 .0436
      -8.20 .0313 .0293 .0305 .0304 .0319 .0306 .0322 .0318 .0321
-10.0
-10.0 -9.36 .0174 .0174 .0177 .0175 .0168 .0173 .0157 .0163 .0173
-10.0 -10.51 .0098 .0097 .0094 .0096 .0103 .0098 .0100 .0091 .0090
-10.0 -11.66 .0070 .0070 .0071 .0069 .0071 .0070 .0068 .0066 .0071
-10.0 -12.82 .0061 .0059 .0056 .0057 .0058 .0057 .0058 .0055 .0056
-10.0 -13.97 .0056 .0055 .0057 .0056 .0055 .0056 .0055 .0056
-10.0 -15.12 .0052 .0051 .0051 .0052 .0052 .0052 .0051 .0052 .0052
-5.0
        -.03 .0648 .0477 .0465 .0557 .0595 .0570 .0587 .0566 .0642
       -.09 .0967 .0982 .0966 .0979 .1009 .1015 .0971 .0961 .1006
-5.0
       -.15 .1020 .1006 .1042 .1022 .1019 .1007 .0999 .1020 .1028
-5.0
       -.21 .0938 .0966 .0962 .0956 .0945 .0961 .0948 .0939 .0941
-5.0
-5.0
       -.28 .0875 .0868 .0864 .0881 .0887 .0863 .0884 .0889 .0874
-5.0
       -.34 .0840 .0840 .0838 .0823 .0829 .0825 .0842 .0841 .0819
-5.0
       -.43 .0806 .0808 .0798 .0797 .0793 .0820 .0799 .0801 .0828
-5.0
       -.53 .0797 .0780 .0783 .0783 .0788 .0761 .0777 .0794 .0808
-5.0
       -.66 .0786 .0763 .0783 .0756 .0762 .0785 .0779 .0790 .0749
-5.0 -.82 .0763 .0773 .0757 .0754 .0762 .0747 .0748 .0762 .0769
-5.0 -1.02 .0753 .0760 .0763 .0757 .0738 .0743 .0761 .0740 .0756
-5.0
      -1.28 .0734 .0738 .0728 .0717 .0727 .0737 .0709 .0742 .0742
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-1.59 .0729 .0720 .0711 .0707 .0714 .0721 .0725 .0731 .0728
      -1.98 .0702 .0700 .0706 .0676 .0717 .0697 .0689 .0714 .0709
      -2.46 .0685 .0684 .0689 .0679 .0694 .0665 .0681 .0673 .0684
-5.0
      -3.06 .0671 .0671 .0674 .0662 .0659 .0671 .0659 .0647 .0649
      -3.81 .0637 .0663 .0634 .0653 .0658 .0625 .0633 .0633 .0649
-5.0
      -4.74 .0600 .0586 .0602 .0602 .0601 .0604 .0597 .0615 .0611
-5.0
      -5.89 .0547 .0532 .0525 .0530 .0533 .0545 .0523 .0551 .0541
      -7.05 .0453 .0442 .0459 .0439 .0447 .0434 .0441 .0459 .0459
-5.0
      -8.20 .0312 .0310 .0311 .0318 .0297 .0307 .0299 .0316 .0308
-5.0
     -9.36 .0175 .0171 .0187 .0172 .0190 .0156 .0167 .0178 .0173
-5.0
-5.0 -10.51 .0095 .0084 .0087 .0086 .0090 .0088 .0093 .0089 .0091
-5.0 -11.66 .0068 .0066 .0066 .0068 .0072 .0066 .0068 .0068
-5.0 -12.82 .0060 .0058 .0058 .0059 .0059 .0059 .0058 .0063 .0059
-5.0 -13.97 .0054 .0057 .0057 .0057 .0058 .0057 .0056 .0058 .0056
-5.0 -15.12 .0055 .0055 .0055 .0054 .0055 .0054 .0055 .0056
       -.03 .0512 .0471 .0416 .0553 .0601 .0566 .0527 .0556 .0550
-1.0
       -.09 .0921 .0925 .0899 .0949 .0966 .0978 .0975 .0933 .0948
-1.0
-1.0
       -.15 .0999 .1006 .1007 .0997 .C982 .1006 .0986 .1014 .0994
-1.0
       -.21 .0916 .0896 .0914 .0914 .0891 .0909 .0913 .0925 .0922
       -.28 .0851 .0845 .0868 .0835 .0807 .0827 .0857 .0853 .0872
-1.0
       -.34 .0820 .0827 .0810 .0795 .0798 .0798 .0807 .0816 .0823
-1.0
       -.43 .0779 .0795 .0776 .0790 .0789 .0772 .0787 .0793 .0781
-1.0
-1.0
       -.53 .0784 .0747 .0766 .0765 .0759 .0767 .0791 .0774 .0797
       -.66 .0762 .0769 .0735 .0758 .0755 .0752 .0744 .0772 .0780
-1.0
-1.0
      -.82 .0752 .0770 .0755 .0735 .0735 .0730 .0741 .0783 .0753
     -1.02 .0734 .0747 .0722 .0722 .0738 .0730 .0729 .0761 .0739
-1.0
     -1.28 .0733 .0727 .0721 .0725 .0700 .0724 .0718 .0750 .0724
-1.0
     -1.59 .0704 .0733 .0719 .0703 .0696 .0699 .0714 .0707 .0706
-1.0
     -1.98 .0696 .0701 .0697 .0674 .0695 .0695 .0705 .0690 .0714
     -2.46 .0683 .0660 .0674 .0678 .0664 .0672 .0668 .0660 .0677
-1.0
     -3.06 .0661 .0669 .0668 .0651 .0659 .0648 .0661 .0662 .0661
-1.0
     -3.81 .0635 .0629 .0646 .0634 .0622 .0644 .0644 .0635 .0641
-1.0
     -4.74 .0595 .0604 .0597 .0579 .0603 .0576 .0596 .0601 .0602
-1.0
     -5.89 .0538 .0531 .0529 .0525 .0524 .0527 .0542 .0514 .0521
-1.0
     -7.05 .0449 .0451 .0454 .0438 .0428 .0439 .0441 .0433 .0442
-1.0
     -8.20 .0318 .0304 .0305 .0297 .0298 .0305 .0320 .0324 .0317
-1.0
-1.0 -9.36 .0179 .0175 .0174 .0163 .0178 .0174 .0175 .0196 .0182
-1.0 -10.51 .0096 .0103 .0090 .0087 .0092 .0098 .0083 .0101 .0094
-1.0 -11.66 .0065 .0070 .0066 .0067 .0064 .0069 .0067 .0067 .0066
-1.0 -12.82 .0060 .0054 .0054 .0053 .0054 .0055 .0055 .0054 .0056
-1.0 -13.97 .0058 .0055 .0055 .0055 .0057 .0056 .0056 .0055
-1.0 -15.12 .0059 .0051 .0053 .0053 .0053 .0054 .0052 .0053
       -.03 .0731 .0631 .0572 .0640 .0739 .0762 .0679 .0683 .0745
  .0
      -.09 .1018 .0973 .0972 .1001 .1017 .1063 .1042 .1068 .1033
  .0
      -.15 .0972 .0979 .0962 .0970 .0961 .0994 .1005 .0993 .0959
  .0
       -.21 .0927 .0909 .0890 .0898 .0876 .0921 .0935 .0927 .0928
  .0
       -.28 .0864 .0854 .0855 .0832 .0834 .0896 .0887 .0916 .0883
       -.34 .0828 .0830 .0824 .0810 .0805 .0809 .0849 .0839 .0840
```

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-.43 .0807 .0797 .0775 .0774 .0793 .0803 .0818 .0799 .0808
 .0
      -.53 .0791 .0792 .0780 .0773 .0785 .0787 .0785 .0808 .0796
 .0
      -.66 .0779 .0780 .0763 .0780 .0772 .0769 .0786 .0769 .0772
 .0
      -.82 .0781 .0774 .0762 .0773 .0750 .0763 .0756 .0787 .0754
 .0
     -1.02 .0755 .0753 .0760 .0752 .0743 .0749 .0764 .0760 .0753
 .0
     -1.28 .0748 .0749 .0733 .0753 .0717 .0730 .0756 .0751 .0755
     -1.59 .0738 .0731 .0742 .0728 .0708 .0715 .0749 .0726 .0745
 .0
     -1.98 .0715 .0734 .0720 .0725 .0718 .0692 .0731 .0707 .0730
 .0
     -2.46 .0705 .0679 .0690 .0697 .0692 .0701 .0683 .0700 .0696
 .0
     -3.06 .0674 .0701 .0679 .0656 .0662 .0668 .0685 .0688 .0687
 .0
     -3.81 .0646 .0652 .0675 .0655 .0646 .0642 .0667 .0629 .0661
 .0
    -4.74 .0617 .0611 .0627 .0616 .0606 .0613 .0621 .0611 .0615
 .0
     -5.89 .0559 .0546 .0568 .0544 .0546 .0546 .0547 .0547 .0566
 .0
    -7.05 .0464 .0467 .0455 .0442 .0444 .0453 .0433 .0463 .0449
    -8.20 .0323 .0338 .0322 .0316 .0299 .0296 .0305 .0309 .0321
 .0
    -9.36 .0177 .0172 .0180 .0171 .0172 .0161 .0168 .0176 .0188
 .0
 .0 -10.51 .0102 .0100 .0098 .0101 .0092 .0093 .0096 .0093 .0096
 .0 -11.66 .6070 .0065 .0069 .0067 .0067 .0070 .0065 .0078 .0064
 .0 -12.82 .0059 .0065 .0062 .0063 .0064 .0062 .0063 .0062 .0065
 .0 -13.97 .0057 .0057 .0055 .0056 .0055 .0055 .0056 .0055 .0055
 .0 -15.12 .0059 .0053 .0052 .0052 .0053 .0051 .0051 .0052 .0052
       .58 .0197 .0182 .0223 .0192 .0370 .0392 .0317 .0235 .0180
1.0
       .40 .0224 .0206 .0240 .0185 .0323 .0365 .0323 .0243 .0201
1.0
       .21 .0220 .0234 .0264 .0219 .0245 .0309 .0302 .0258 .0225
1.0
      .03 .0324 .0349 .0362 .0376 .0346 .0394 .0404 .0345 .0368
1.0
      -.12 .0753 .0795 .0824 .0875 .0871 .0799 .0791 .0758 .0761
1.0
     -.25 .1158 .1212 .1223 .1255 .1192 .1252 .1202 .1164 .1178
1.0
      -.40 .1107 .1120 .1059 .1049 .0996 .1051 .1098 .1140 .1109
1.0
      -.63 .0841 .0826 .0817 .0805 .0805 .0814 .0841 .0844 .0857
1.0
      -.79 .0792 .0787 .0787 .0755 .0779 .0792 .0808 .0794 .0800
1.0
      -.99 .0776 .0794 .0759 .0773 .0766 .0794 .0770 .0785 .0792
1.0
     -1.24 .0772 .0779 .0771 .0730 .0744 .0760 .0766 .0790 .0768
1.0
     -1.56 .0750 .0761 .0738 .0745 .0738 .0742 .0776 .0752 .0768
1.0
     -1.95 .0727 .0735 .0726 .0715 .0694 .0718 .0731 .0736 .0769
1.0
     -2.43 .0706 .0732 .0710 .0717 .0716 .0708 .0705 .0722 .0728
1.0
     -3.03 .0691 .0694 .0672 .0692 .0666 .0672 .0696 .0698 .0691
1.0
     -3.78 .0660 .0673 .0667 .0649 .0659 .0642 .0649 .0662 .0648
1.0
     -4.71 .0632 .0642 .0641 .0625 .0624 .0651 .0633 .0640 .0638
1.0
     -5.86 .0625 .0616 .0612 .0600 .0616 .0608 .0603 .0621 .0601
1.0
     -7.02 .0580 .0579 .0577 .0581 .0566 .0564 .0592 .0573 .0569
1.0
    -8.17 .0556 .0538 .0545 .0527 .0520 .0526 .0530 .0536 .0537
1.0
    -9.32 .0477 .0470 .0480 .0461 .0468 .0461 .0461 .0483 .0466
1.0 -10.48 .0264 .0247 .0271 .0265 .0254 .0239 .0251 .0269 .0262
1.0 -11.63 .0176 .0178 .0183 .0170 .0168 .0179 .0162 .0164 .0178
1.0 -12.78 .0082 .0077 .0073 .0077 .0079 .0073 .0076 .0079 .0078
1.0 -13.94 .0067 .0064 .0065 .0065 .0064 .0063 .0063 .0064 .0064
1.0 -15.09 .0058 .0059 .0060 .0059 .0059 .0059 .0059 .0060
      .58 .0403 .0385 .0375 .0572 .0655 .0604 .0452 .0334 .0325
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Table D.16 (cont'd).

2 2		0/00	04.00	05/0	0617	0000	0600	OEC.	0506	04.50
3.0				.0543						
3.0		.0772		.0876						
3.0		.1010		.1078				.1104		
3.0		.1167		.1202				.1217		
3.0		.1238		.1296						.1259
3.0		.1267		.1253						
3.0		.1083		.1017						
3.0		.0895		.0844						
3.0		.0816		.0809						
3.0		.0787		.0761						
3.0	-1.56	.0762	.0770	.0760	.0752	.0726	.0739	.0762	.0751	.0773
3.0				.0720						
3.0	-2.43	.0702		.0721						
3.0		.0693		.0689						
3.0				.0660						
3.0				.0666						
3.0	-5.86	.0587	.0588	.0585	.0571	.0569	.0586	.0580	.0582	.0583
3.0				.0515						
3.0	-8.17	.0355	.0336	.0331	.0336	.0336	.0337	.0339	.0358	.0341
3.0	-9.32	.0252	.0248	.0249	.0235	.0223	.0251	.0254	.0225	.0273
3.0	-10.48									
	-11.63									
				.0061						
3.0				.0056						
				.0059						
5.0				.0108						
5.0				.0342						
5.0				.1334						
5.0				.0836						
5.0				.0712						
5.0	-2.93			.0673				.0678		
5.0				.0615						
5.0				.0581						
5.0		.0498		.0489						
5.0		.0399		.0385						
5.0	-7.86	.0249						.0240		.0266
5.0	-8.85		.0151	.0162						.0147
5.0	-9.84	.0088	.0094	.0087	.0084	.0086	.0089	.0088	.0088	.0096
5.0	-10.82	.0073	.0067	.0073	.0068	.0066	.0064	.0067	.0070	.0066
5.0	-10.82	.0073	.0062	.0063	.0064	.0063	.0062	.0063	.0062	.0063
	-12.79	.0060	.0058	.0057	.0057	.0057	.0056	.0057	.0058	.0057
							.0058	.0056	.0057	.0057
5.0	-13.78	.0062	.0057	.0057	.0057	.0057	.0059	.0059	.0058	.0058
5.0	-14.76	.0062	.0057	.0057	.0057	.0056			.0054	.0055
5.0	-15.75	.0058	.0053	.0053	.0052	.0053	.0055	.0054	.0054	
5.0	-16.74	.0055	.0052	.0050	.0051	.0051	.0051	.0053		.0052
5.0	-17.72	.0054	.0051	.0051	.0051	.0051	.0051	.0051	.0052	.0052
10.0	4.00	.0067	.0062	.0064	.0081	.0091	.0103	.0094	.0079	.0064
10.0	2.87	.0108	.0097	.0107	.0142	.0159	.0187	.0157	.0109	.0101

						0570	0/07	0207	0222	0260
10.0								.0387	.0332	
10.0		.1062		.1162			.1240	.1004	.1053	.1038
10.0	51	.1271	.1220	.1172			.1245	.1355		.1271
10.0	-1.63	.0766	.0765	.0769		.0729	.0742	.0832		.0807
10.0	-2.76	.0680	.0686	.0695	.0679	.0657	.0653	.0657	.0670	.0680
10.0		.0621		.0621	.0617	.0620	.0595	.0620	.0627	.0632
10.0		.0560		.0552			.0533	.0547	.0549	.0576
10.0		.0473		.0476			.0457	.0462	.0464	.0491
10.0		.0334		.0328		-	.0288	.0304		.0333
		.0208		.0189			.0176		.0187	.0204
10.0					.0100		.0096		.0099	.0113
10.0		.0112					.0071	.0068		.0076
	-10.64			.0070		•				.0064
	-11.77		.0061		.0062		.0063	.0062		
	-12.89				.0057		.0059	.0058	.0057	.0057
	-14.02		.0058	.0058		.0058	.0058	.0058	.0058	.0059
10.0	-15.15	.0063	.0057			.0058	.0057		.0059	.0057
10.0	-16.27	.0053	.0052	.0051	.0053	.0052	.0051	.0053		.0052
10.0	-17.40	.0052	.0052	.0051	.0052	.0053	.0052	.0053	.0053	.0053
10.0	-18.52	.0053	.0050	.0052	.0052	.0053	.0052	.0052	.0054	.0053
15.0		.0061					.0087	.0088	.0079	.0067
15.0		.0089			.0086		,0137		.0120	.0097
15.0		.0164			.0211	-	.0266		.0215	.0159
15.0		.0503			.0698		.0832			.0433
15.0		.1091		.1129			.1241		.0999	.1054
		.1326		.1330			.1258			.1383
15.0				.0906			.0774			.1095
15.0		.0922								
15.0		.0687		.0691						
15.0		.0619	.0626		.0621		.0610		.0598	
15.0	-5.40	-	.0558	.0547			.0513		.0541	
15.0	-6.66	.0430	.0448		.0421		.0384	.0403		.0436
15.0	-7.93	.0273	.0294	.0285		.0259	.0233			.0281
15.0	-9.19	.0142	.0147	.0147	.0139	.0117	.0125			.0136
15.0	-10.46	.0087	.0081	.0082	.0079	.0077	.0076	.0080		.0094
15.0	-11.73	.0070	.0067	.0068	.0067	.0067	.0068	.0065	.0068	.0068
15.0	-12.99	.0062	.0057	.0056	.0057	.0059	.0059	.0057	.0058	.0059
15.0	-14.26	.0059	.0057	.0059	.0057	.0059	.0059	.0058	.0060	.0061
15.0	-15.53	.0065	.0057	.0058	.0056	.0056	.0057	.0058	.0058	.0058
15.0	-16.79	.0057	.0055	.0056	.0054	.0056	.0055	.0056	.0056	.0055
15.0	-18.06	.0059	.0053	.0053	.0052	.0055	.0055	.0055	.0053	.0052
15.0	-19.32	.0054	.0054	.0054	.0053	.0054	.0053	.0054	.0054	.0053
		.0053	.0071	.0067	.0058	.0047	.0056	.0084	.0091	.0076
25.0	10.00				.0058	.0052	.0064	.0103	.0124	.0102
25.0	8.45	.0071	.0076	.0069				.0163	.0188	.0156
25.0	6.91	.0103	.0112	.0097	.0087	.0076	.0120			
25.0	5.36	.0164	.0162	.0133	.0138	.0217	.0305	.0314	.0317	.0264
25.0	3.81	.0421	.0278	.0253	.0463	.0665	.0741	.0746	.0688	.0454
25.0	2.27	.0888	.0551	.0724	.0983	.1130	.1148	.1150	.1094	.0736
25.0	. 72	.1253	.0987	.1204	.1303	.1350	.1305	.1337	.1343	.1175
25.0	82	.1318	.1258	.1440	.1318	.1189	.1136	.1143	.1181	.1320

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-2.37 .0911 .1189 .1059 .0882 .0800 .0748 .0740 .0779 .1128
25.0
      -3.92 .0658 .0766 .0712 .0659 .0657 .0617 .0603 .0629 .0703
25.0
      -5.46 .0554 .0563 .0588 .0558 .0550 .0527 .0504 .0519 .0544
25.0
     -7.01 .0420 .0432 .0451 .0413 .0382 .0352 .0342 .0379 .0417
25.0
     -8.55 .0230 .0276 .0252 .0231 .0202 .0180 .0171 .0171 .0237
25.0
25.0 -10.10 .0108 .0117 .0123 .0106 .0101 .0095 .0096 .0093 .0100
25.0 -11.65 .0073 .0077 .0078 .0076 .0073 .0076 .0072 .0071 .0070
25.0 -13.19 .0063 .0066 .0065 .0061 .0061 .0062 .0062 .0062 .0062
25.0 -14.74 .0062 .0059 .0061 ,0060 .0059 .0063 .0062 .0063 .0060
25.0 -16.29 .0054 .0054 .0055 .0055 .0057 .0056 .0057 .0057 .0055
25.0 -17.83 .0054 .0052 .0053 .0051 .0053 .0055 .0055 .0052
25.0 -19.38 .0054 .0056 .0056 .0054 .0055 .0056 .0055 .0057
25.0 -20.92 .0050 .0053 .0052 .0051 .0052 .0055 .0055 .0055
     16.00 .0043 .0085 .0081 .0069 .0062 .0058 .0054 .0046 .0067
40.0
      14.03 .0056 .0113 .0110 .0090 .0077 .0069 .0064 .0057 .0100
40.0
      12.07 .0076 .0160 .0148 .0116 .0088 .0078 .0078 .0084 .0144
40.0
      10.10 .0100 .0230 .0216 .0158 .0112 .0099 .0105 .0160 .0236
40.0
       8.13 .0150 .0385 .0368 .0248 .0149 .0131 .0163 .0365 .0446
40.0
       6.17 .0325 .0610 .0539 .0362 .0203 .0199 .0498 .0754 .0800
40.0
       4.20 .0746 .0994 .0730 .0527 .0325 .0506 .1006 .1176 .1207
40.0
       2.24 .1146 .1254 .1020 .0680 .0559 .1010 .1360 .1393 .1366
40.0
       .27 .1360 .1304 .1181 .0901 .1021 .1344 .1401 .1312 .1268
40.0
     -1.70 .1274 .1069 .1304 .1128 .1269 .1298 .1157 .0940 .0845
40.0
      -3.66 .0858 .0714 .1109 .1191 .1133 .0888 .0754 .0666 .0628
40.0
      -5.63 .0581 .0520 .0688 .0814 .0728 .0615 .0548 .0480 .0455
40.0
     -7.60 .0387 .0313 .0436 .0487 .0471 .0429 .0333 .0275 .0262
40.0
     -9.56 .0172 .0153 .0194 .0243 .0233 .0188 .0147 .0138 .0118
40.0
40.0 -11.53 .0097 .0092 .0095 .0113 .0115 .0102 .0094 .0091 .0084
40.0 -13.49 .0072 .0081 .0075 .0078 .0083 .0080 .0078 .0079 .0079
40.0 -15.46 .0067 .0071 .0066 .0070 .0071 .0070 .0068 .0071 .0069
40.0 -17.42 .0059 .0061 .0058 .0061 .0061 .0061 .0061 .0064 .0062
40.0 -19.39 .0055 .0059 .0058 .0059 .0056 .0055 .0057 .0061 .0061
40.0 -21.36 .0060 .0065 .0061 .0059 .0058 .0057 .0060 .0063 .0064
40.0 -23.32 .0054 .0058 .0054 .0053 .0054 .0053 .0054 .0056 .0057
     24.00 .0038 .0056 .0058 .0062 .0059 .0051 .0046 .0047 .0051
60.0
     21.47 .0048 .0062 .0058 .0078 .0074 .0066 .0057 .0058 .0059
      18.95 .0061 .0070 .0078 .0123 .0106 .0095 .0083 .0079 .0074
60.0
      16.42 .0081 .0085 .0120 .0185 .0166 .0145 .0120 .0100 .0088
60.0
     13.90 .0104 .0118 .0205 .0319 .0275 .0259 .0191 .0137 .0112
60.0
      11.37 .0159 .0173 .0397 .0516 .0427 .0430 .0312 .0210 .0160
60.0
       8.84 .0333 .0364 .0789 .0819 .0565 .0586 .0449 .0309 .0234
60.0
       6.32 .0689 .0855 .1220 .1158 .0870 .0776 .0599 .0456 .0377
60.0
       3.79 .1078 .1248 .1434 .1277 .1216 .0935 .0721 .0578 .0753
60.0
       1.26 .1314 .1387 .1261 .1146 .1228 .1025 .0873 .0751 .1111
60.0
      -1.26 .1379 .1115 .0847 .0877 .1213 .1115 .0937 .0968 .1253
60.0
      -3.79 .1097 .0728 .0580 .0643 .1091 .1136 .1024 .1120 .1099
60.0
      -6.31 ..0618 .0445 .0328 .0423 .0762 .0986 .1047 .0963 .0641
60.0
     -8.84 .0326 .0220 .0188 .0215 .0369 .0632 .0661 .0504 .0319
60.0
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Table D.16 (cont'd).

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60.0 -11.37 .0153 .0157 .0150 .0147 .0183 .0228 .0238 .0202 .0155
 60.0 -13.89 .0108 .0135 .0134 .0120 .0118 .0123 .0133 .0128 .0120
 60.0 -16.42 .0084 .0092 .0093 .0096 .0090 .0079 .0088 .0094 .0091
 60.0 -18.95 .0069 .0077 .0077 .0079 .0075 .0064 .0069 .0074 .0075 60.0 -21.47 .0065 .0081 .0085 .0078 .0074 .0069 .0068 .0068 .0070
 60.0 -24.00 .0061 .0068 .0069 .0069 .0067 .0060 .0057 .0060 .0063
 60.0 -26.52 .0056 .0062 .0064 .0064 .0062 .0058 .0057 .0056 .0058
 76.9 -15.47 .0125 .0147 .0145 .0145 .0139 .0150 .0144 .0146 .0149
 76.9 -13.86 .0150 .0172 .0170 .0169 .0158 .0171 .0175 .0231 .0198
 76.9 -12.24 .0184 .0252 .0201 .0199 .0189 .0198 .0255 .0436 .0392
 76.9 -10.63 .0254 .0416 .0240 .0194 .0175 .0233 .0461 .0726 .0737
       -9.01 .0407 .0786 .0345 .0267 .0228 .0318 .0724 .0923 .0937
 76.9
       -7.40 .0628 .0955 .0607 .0308 .0255 .0457 .0888 .0965 .1001
 76.9
       -5.78 .0894 .1042 .0886 .0424 .0322 .0593 .0995 .1028 .0984
 76.9
       -4.17 .1150 .1029 .1052 .0607 .0440 .0766 .1072 .1008 .0960
 76.9
       -2.55 .1317 .0968 .1159 .0858 .0566 .0910 .1107 .1052 .0946
 76.9
 76.9
        -.94 .1367 .0940 .1148 .1106 .0740 .0968 .1148 .1080 .0980
 76.9
         .68 .1351 .0896 .1043 .1200 .0874 .1065 .1179 .1048 .0936
        2.30 .1281 .0853 .0900 .1248 .1102 .1097 .1200 .1073 .0920
 76.9
        3.91 .1180 .0749 .0767 .1181 .1221 .1130 .1254 .1052 .0842
 76.9
 76.9
        5.53 .0983 .0729 .0708 .1027 .1246 .1112 .1203 .1016 .0810
        7.14 .0831 .0620 .0583 .0855 .1229 .1061 .0986 .0912 .0715
 76.9
        8.76 .0576 .0533 .0501 .0578 .1059 .0973 .0756 .0743 .0626
 76.9
       10.37 .0392 .0445 .0416 .0445 .0834 .0890 .0570 .0603 .0541
 76.9
       11.99 .0244 .0389 .0325 .0340 .0611 .0812 .0521 .0533 .0470
 76.9
       13.60 .0187 .0319 .0282 .0286 .0428 .0632 .0471 .0431 .0382
 76.9
 76.9
       15.22 .0131 .0225 .0202 .0214 .0303 .0430 .0360 .0315 .0286
 76.9
       16.83 .0112 .0188 .0159 .0169 .0223 .0296 .0267 .0240 .0227
       23.58 .0124 .0264 .0283 .0283 .0281 .0280 .0264 .0267 .0250
115.4
       21.37 .0140 .0376 .0362 .0344 .0340 .0339 .0347 .0348 .0358
115.4
       19.17 .0183 .0471 .0473 .0459 .0430 .0425 .0442 .0456 .0455
       16.97 .0251 .0613 .0583 .0525 .0519 .0534 .0537 .0543 .0608
115.4
       14.77 .0414 .0772 .0725 .0600 .0586 .0619 .0655 .0693 .0728
115.4
       12.57 .0597 .0904 .0855 .0756 .0826 .0868 .0852 .0844 .0867
115.4
       10.37 .0834 .1082 .0984 .0976 .1057 .1021 .0990 .0985 .1044
115.4
115.4
        8.17 .0994 .1140 .1131 .1339 .1328 .1183 .1075 .1074 .1156
        5.97 .1204 .1171 .1297 .1471 .1458 .1332 .1194 .1174 .1238
115.4
        3.77 .1308 .1113 .1365 .1515 .1462 .1314 ,1206 .1224 .1271
115.4
        1.56 .1422 .1012 .1216 .1395 .1357 .1291 .1265 .1270 .1205
115.4
        -.64 .1447 .0911 .1210 .1375 .1348 .1280 .1282 .1290 .1007
115.4
115.4
       -2.84 .1405 .0804 .1151 .1291 .1320 .1297 .1266 .1252 .0750
       -5.04 .1278 .0696 .1059 .1218 .1288 .1268 .1245 .1064 .0508
115.4
      -7.24 .1042 .0574 .0960 .1091 .1189 .1174 .1159 .0821 .0388
115.4
      -9.44 .0687 .0436 .0860 .1036 .1080 .1130 .1005 .0528 .0322
115.4
115.4 -11.64 .0428 .0350 .0686 .0961 .0996 .0981 .0743 .0368 .0291
115.4 -13.84 .0258 .0312 .0442 .0746 .0831 .0728 .0433 .0273 .0248
115.4 -18.25 .0206 .0231 .0270 .0280 .0275 .0230 .0193 .0187 .0199
115.4 -18.25 .0174 .0231 .0270 .0280 .0275 .0230 .0193 .0187 .0199
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Table D.16 (cont'd).

115.4	-20.45	.0148	.0216	.0225	.0204	.0168	.0140	.0154	.0161	.0175
	-28.62									
	-25.51								.0269	
	-22.41			.0187			.0292		.0335	.0333
	-19.30			.0373		.0289	.0344	.0402	.0556	.0634
153.8	-16.19	.0339	.0932	.0647	.0350	.0323	.0398	.0639	.0875	.0989
	-13.09			.1068		.0396	.0507	.0881	.1115	.1246
153.8		.0929	.1431	.1302	.0908	.0516	.0699	.1077	.1305	.1392
153.8	-6.87	.1290	.1524	.1535	.1294	.0785	.0887	.1210	.1445	. 1474
153.8	-3.76		.1592	.1545	.1534	.1089	.1028	.1269	.1541	.1522
153.8	66	.1495	.1608	.1579	.1591	.1366	.1213	.1433	.1681	.1669
153.8	2.45	. 1443					.1302		.1680	.1671
153.8	5.56						.1257		.1663	
153.8	8.66	.1209	.1480	.1482	.1446	.1404	.1208	.1128	.1276	.1429
153.8	11.77						.1137		.1016	
153.8	14.88						.1102		.0912	
153.8	17.98						.1011		.0831	.0859
153.8	21.09	.0321	.0789	.0807	.0897	.0929	.0949	.0838	.0783	.0791
153.8	24.20	.0201	.0682	.0694	.0725	.0759	.0738	.0647	.0660	.0660
153.8	27.30	.0152	.0575	.0566	.0594	.0594	.0576	.0583	.0551	. 0545
153.8	30.41	.0126	.0456	.0448	.0487	.0489	.0486	.0485	.0463	. 0454
153.8	33.52	.0113	.0368	.0362	.0363	.0374	.0365	.0363	.0371	.0376
192.3	43.46	.0109	.0433	.0433	.0431	.0456	.0456	.0455	.0445	.0444
192.3	39.45	.0127	.0540	.0537	.0553		.0544		.0552	
192.3	35.43	.0155	.0737	.0729	.0701	.0703	.0701	.0722	.0736	.0740
192.3	31.42	.0197	.0885	.0896	.0849	.0814	.0852	.0860	.0889	.0895
192.3	27.41	.0297	.1114	.1028	.0963	.0966	.0982	.1044	.1047	
192.3	23.40	.0505	.1169	.1072	.0990		.1039		.1150	
192.3	19.38	.0688		.1105			.1113		.1280	
192.3	15.37	.0952	.1261	.1155	.1112	.1150	.1280	.1425	.1455	. 1405
192.3	11.36	.1198	.1272	.1136			.1427		.1562	.1426
192.3	7.35	.1395	.1240	.1252	.1430	.1561	.1633		.1608	
192.3	3.33	.1536	.1329	. 1497			.1726		.1623	
192.3	68	.1532	.1424				.1701			
192.3	-4.69	.1496					.1643		.1542	
192.3	-8.70	.1298	.1111	.1346			.1574			.0969
192.3	-12.72	.0910	.0913	.1229	.1366	.1404	.1465	.1361	.0971	.0682
192.3	-16.73	.0541	.0637	.0968	.1145	.1224	.1232	.1030	.0627	.0479
192.3	-20.74	.0345	.0453	.0642	.0823	.0887	.0857	.0618	.0352	.0365
192.3	-24.75	. 0245	.0364	.0447	.0518	.0542	.0455	.0339	.0219	.0281
192.3	-28.77	.0184	.0283	.0312	.0305	.0280	.0241	.0172	.0176	.0223
192.3	-32.78	.0138	.0237	.0242	.0218	.0186	.0148	.0124	.0150	.0198
192.3	-36.79	.0126	.0205	.0214	.0192	.0153	.0114	.0100	.0126	.0168
230.8	-44.97	.0125	.0109	.0105	.0137	.0176	.0200	.0200	.0177	.0141
230.8	-40.05	.0147	.0151	.0131	.0163	.0206	.0237	.0238	.0215	.0170
230.8	-35.13	.0177	.0174	.0170	.0181	.0233	.0276	.0279	.0263	.0236
230.8	-30.21	.0227	.0405	.0252	.0232	.0289	.0351	.0386	.0454	.0498
230.8	-25.29	.0320	.0762	.0523	.0355	.0377	.0491	.0620	.0760	.0811

Table D.16 (cont'd).

230.8	-20.37	.0485	.1086	.0825	.0546	.0497	.0746	.0931	.1084	.1135
230.8	-15.46				.0810			.1223	.1356	.1394
230.8	-10.54				.1128			.1467		.1608
230.8	-5.62	.1570	.1646	.1589	.1440	.1359	.1531	.1703	.1712	.1639
230.8								.1741		.1751
230.8	4.22	.1582	.1659	.1627	.1591	.1435	.1395	.1506	.1616	.1652
230.8	9.14	.1418	.1601	.1633	.1585	.1466	.1327	.1296	.1430	. 1.552
230.8	14.06	.1221	.1454	.1516	.1551	.1437	.1266	.1249	.1284	.1376
230.8	18.97								.1201	
230.8	23.89								.1182	.1204
230.8	28.81	.0390	.1162	.1157	.1186	.1202	.1173	.1144	.1137	.1100
230.8	33.73	.0237	.1027	.1056	.1054	.1068	.1051	.1035	.1014	.0993
230.8	38.65	.0179	.0890	.0910	.0926	.0931	.0889	.0874	.0859	.0868
230.8	43.57	.0150	.0683					.0722		.0697
230.8	48.48	.0131	.0581	.0578	.0576	.0571	.0580	.0568	.0572	.0576

Table D.17 - Entrainment Field \overline{u} (θ =-60°)

	Unforced			Pha	se ave	eraged	data	(at ang	$gle \phi$))			
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0			
. 0	0												
107.7	17.54	.027	.033	.035	.038	. 052	.079	.095	.078	.046			
107.7	25.31	.012	.015	.017	.015	.016	.026	.035	.031	.019			
107.7	33.07	.010	.008	.008	.007	. 007	.011	.015	.015	.010			
107.7	40.83	.010	.005	.004	.004	.005	.006	.007	.008	.006			
107.7	48.59	.006	.003	.003	.004	.003	.004	.003	.003	.003			
123.1	20.79	.021	.052	.033	.027	.027	.032	.042	.058	.064			
123.1	30.00	.011	.021	.015	.013	.013	.012	.015	.021	.024			
123.1	39.21	.011	.010	.008	.006	. 005	.006	.007	.009	.010			
123.1	48.42	.008	.004	.004	. 004	.003	. 004	.005	.005	.005			
123.1	57.63	.003	.006	.005	.005	.005	.005	.005	.005	.006			
138.5	24.04	.019	.052	.052	. 045	.034	.029	.029	.034	. 044			
138.5	34.70	.012	.018	.019	.017	.014	.013	.012	.013	.015			
138.5	45.36	.011	.006	.007	.007	.006	.005	.005	.005	.006			
138.5	56.01	.007	.005	.005	.004	.004	. 004	.004	.005	.005			
138.5	66.67	.002	.005	.005	.005	.005	.005	.005	.005	.005			
153.8	27.29	.019	.037	.042	.044	.046	.040	.036	.032	.034			
153.8	39.40	.013	.014	.015	.017	.017	.016	.015	.014	.014			
153.8	51.50	.011	.005	.005	.006	.006	.006	.005	.005	.004			
153.8	63.61	.005	.005	.005	. 004	.005	. 004	.005	.004	.004			
153.8	75.71	.003	.005	.006	.005	.005	.005	. 005	.005	.005			
169.2	30.54	.018	.036	.041	.043	. 047	. 047	.045	.044	.040			
169.2	44.09	.013	.014	.014	.015	.015	.016	.016	.015	.015			
169.2	57.65	.010	.004	.004	.004	.005	.005	.005	.005	.004			
169.2	71.20	.005	.005	.004	.004	.005	.005	.005	.005	.005			
169.2	84.75	. 004	.006	.006	.006	.005	.005	.005	.006	.006			
184.6	33.79	.019	. 045	. 042	. 040	.045	.048	.051	.051	. 048			
184.6	48.79	.014	.014	.013	.013	.013	.013	.014	.015	.014			
184.6	63.79	.010	.004	.004	.004	.004	.004	.004	.005	.005			
184.6	78.80	.005	.005	.005	.005	.005	.005	.006	.005	.005			
184.6	93.80	.006	.006	.005	.005	.005	.006	.005	.005	.005			
200.0	37.04	.019	.055	.053	.049	.049	.050	.053	.055	.056			
200.0	53.49	.014	.014	.014	.014	.013	.013	.013	.014	.014			
200.0	69.94	.010	.004	. 004	.004	.004	.004	.004	.004	.004			
200.0	86.39	.004	.005	.005	.005	.005	. 005	. 005	. 005	.006			

Table D.18 - Entrainment Field $\tilde{\mathbf{u}}$ (θ =-60°)

		Unforce	ed	Pha	ase av	eraged	data	(at ang	gle φ)	
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
U	U									
107.7	17.54	.0243	.0351	.0356	.0427	.0538	.0569	.0546	.0511	.0433
107.7	25.31	.0081	.0143	.0161	.0166	.0162	.0180	.0194	.0195	.0160
107.7	33.07	.0038	.0079	.0102	.0109	.0105	.0101	.0107	.0100	.0071
107.7	40.83	.0029	.0059	.0076	.0082	.0078	.0074	.0068	.0063	.0055
107.7	48.59	.0023	.0054	.0065	.0081	.0072	.0062	.0059	.0049	.0045
123.1	20.79	.0176	.0434	.0362	.0316	.0337	.0379	.0408	.0471	.0478
123.1	30.00	.0070	.0169	.0148	.0129	.0144	.0159	.0156	.0167	.0178
123.1	39.21	.0037	.0080	.0071	.0082	.0090	.0092	.0086	.0083	.0085
123.1	48.42	.0030	.0062	.0064	.0068	.0080	.0086	.0079	.0071	.0065
123.1	57.63	.0031	.0060	.0061	.0068	.0075	.0073	.0070	.0061	.0060
138.5	24.04	.0162	.0446	.0464	.0425	.0381	.0356	.0360	.0377	.0435
138.5	34.70	.0064	.0156	.0156	.0154	.0142	.0140	.0149	.0149	.0154
138.5	45.36	.0036	.0081	.0076	.0076	.0077	.0082	.0088	.0089	.0085
138.5	56.01	.0034	.0078	.0075	.0071	.0073	.0077	.0084	.0089	.0084
138.5	66.67	.0034	.0075	.0076	.0074	.0077	.0077	.0079	.0083	.0081
153.8	27.29	.0136	.0435	.0459	.0459	.0466	.0439	.0422	.0399	.0402
153.8	39.40	.0058	.0154	.0163	.0166	.0158	.0156	.0152	.0154	.0161
153.8	51.50	.0040	.0093	.0091	.0087	.0082	.0079	.0082	.0085	.0090
153.8	63.61	.0040	.0096	.0091	.0084	.0080	.0077	.0083	.0087	.0090
153.8	75.71	.0044	.0093	.0094	.0089	.0083	.0078	.0083	.0087	.0089
169.2	30.54	.0129	.0466	.0495	.0500	.0524	.0510	.0507	.0508	.0485
169.2	44.09	.0061	.0162	.0172	.0171	.0166	.0159	.0164	.0156	.0166
169.2	57.65	.0047	.0092	.0100	.0100	.0094	.0087	.0083	.0086	.0089
169.2	71.20	.0044	.0090	.0092	.0092	.0088	.0081	.0077	.0076	.0083
169.2	84.75	.0054	.0099	.0106	.0106	.0099	.0093	.0089	.0089	.0090
184.6	33.79	.0132	.0492	.0504	.0486	.0512	.0533	.0539	.0535	.0529
184.6	48.79	.0068	.0162	.0155	.0164	.0162	.0163	.0164	.0160	.0163
184.6	63.79	.0051	.0092	.0096	.0093	.0095	.0096	.0086	.0085	.0087
184.6	78.80	.0047	.0086	.0091	.0092	.0091	.0086	.0084	.0081	.0083
184.6	93.80	.0065	.0096	.0101	.0102	.0100	.0097	.0093	.0090	.0091
200.0	37.04	.0132	.0571	.0563	.0557	.0548	.0532	.0538	.0557	.0566
200.0	53.49	.0070	.0164	.0155	.0164	.0170	.0167			.0161
200.0	69.94	.0057	.0085	.0089	.0087	.0089	.0089	.0089	.0086	.0084
200.0	86.39	.0046	.0087	.0091	.0092	.0095	.0090	.0088	.0087	.0087

Table D.19 - Entrainment Field \overline{v} (θ =-60°)

	Unforced		Phase	hase averaged data (at angle ϕ)				
x/θ_0	y/θ_0	data 0.	0 45.0 9	0.0 135.0	180.0	225.0	270.0	315.0
107.7	17.54	04709	4088	099120	120	099	085	094
107.7	25.31	02303	20380	054066	065	053	037	031
107.7	33.07	02002	L0270	035042	043	037	028	022
107.7	40.83	02202	40280	033036	036	033	028	024
107.7	48.59	02402	30300	032035	035	033	030	028
123.1	20.79	03607	50720	068073	085	095	095	085
123.1		02103						
123.1		022028						
123.1		02403						
123.1		02803						
138.5		033083						
138.5		021044						
138.5		023035						
138.5		027034						
138.5		030039						
153.8		030084						
153.8		023045						
153.8		025034						
153.8		029034						
153.8		032035						
169.2		028088						
169.2		023039						
169.2		027032						
169.2		031032						
169.2 184.6		033035						
184.6		027089 025037						
184.6		025037						
184.6		032032						
184.6		034034						
200.0		028095						
200.0		026038						
200.0		030030						
200.0		033033						
	50.57	.000 .000	.000 .0				. 002	

Table D.20 - Entrainment Field $\tilde{\mathbf{v}}$ (θ =-60°)

	Unforced		Pha	ise ave	eraged	data (at angle ϕ)				
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225 <i>:</i> 0	270.0	315.0
107.7	17.54	.0308	.0648	.0535	.0545	.0554	.0500	.0461	.0448	.0601
107.7	25.31	.0113	.0203	.0214	.0235	.0222	.0199	.0184	.0188	.0202
107.7	33.07		.0121	.0144	.0151	.0149	.0134	.0122	.0113	.0106
107.7	40.83	.0044	.0091	.0100	.0105	.0105	.0098	.0089	.0082	.0081
107.7	48.59	.0030	.0062	.0067	.0073	.0073	.0069	.0063	.0058	.0056
123.1	20.79	.0232	.0452	.0490	.0448	.0432	.0432	.0435	.0465	.0452
123.1	30.00	.0097	.0207	.0202	.0213	.0226	.0226	.0215	.0198	.0190
123.1	39.21	.0059	.0110	.0110	.0122	.0133	.0139	.0136	.0127	.0118
123.1	48.42	.0039	.0079	.0078	.0083	.0090	.0095	.0094	.0091	.0085
123.1	57.63	.0032	.0049	.0048	.0052	.0056	.0060	.0061	.0058	.0052
138.5	24.04	.0222	.0404	.0477	.0496	.0501	. 0447	.0421	.0401	.0385
138.5	34.70	.0091	.0197	.0194	.0188	.0188	.0209	.0219	.0223	.0213
138.5	45.36	.0053	.0126	.0119	.0112	.0112	.0118	.0125	.0131	.0131
138.5	56.01	.0039	.0081	.0078	.0072	.0070	.0073	.0079	.0083	.0083
138.5	66.67	.0028	.0054	.0054	.0050	.0050	.0050	.0052	.0056	.0056
153.8	27.29	.0183	.0435	.0444	.0476	.0488	.0521	.0491	.0469	.0439
153.8	39.40	.0080	.0238	.0225	.0228	.0220	.0211	.0223	.0227	.0233
153.8	51.50	.0050	.0124	.0124	.0120	.0113	.0108	.0108	.0113	.0120
153.8	63.61	.0038	.0076	.0076	.0075	.0071	.0069	.0069	.0071	.0075
153.8	75.71	.0029	.0057	.0059	.0057	.0054	.0051	.0052	.0052	.0054
169.2	30.54	.0167	.0531	.0506	.0509	.0493	.0513	.0554	.0587	.0577
169.2	44.09	.0079	.0219	.0228	.0224	.0233	.0236	.0219	.0226	.0226
169.2	57.65	.0052	.0123	.0126	.0127	.0127	.0122	.0118	.0115	.0123
169.2	71.20	.0040	.0068	.0070	.0070	.0070	.0069	.0066	.0064	.0065
169.2	84.75	.0029	.0056	.0059	.0057	.0057	.0056	.0054	.0053	.0053
184.6	33.79	.0168	.0612	.0611	.0567	.0550	.0561	.0564	.0578	.0595
184.6	48.79	.0083	.0242	.0238	.0242	.0244	.0242	.0228	.0235	.0235
184.6	63.79	.0055	.0110	.0111	.0113	.0115	.0116	.0115	.0113	.0111
184.6	78.80	.0042	.0064	.0065	.0066	.0067	.0067	.0066	.0066	.0065
184.6	93.80	.0029	.0054	.0055	.0055	.0057	.0056	.0054	.0053	.0053
200.0	37.04	.0160	.0605	.0606	.0636	.0618	.0624	.0586	.0572	.0585
200.0	53.49	.0080	.0241		.0249	.0250	.0256	.0250	.0256	.0259
200.0	69.94	.0057	.0108		.0105	.0105	.0106	.0108	.0109	.0108
200.0	86.39	.0038	.0065	.0065	.0065	.0067	.0066	.0065	.0066	.0065

Table D.21 - Entrainment Field $\overline{u'v'}$ (θ =-60°)

	Unforced	Phase averaged data (at angle ϕ)
x/θ_0	y/θ_0 data 0.0	Phase averaged data (at angle φ)) 45.0 90.0 135.0 180.0 225.0 270.0 315.0
107.7	17.5400340088	30063008500860083008000870131
107.7	25.3100000001	.0013 .0012 .00030003000200010003
107.7	33.070001 .0005	5 .0009 .0011 .0006 .0001 .0000 .0002 .0001
107.7	40,83 .0000 .0003	3 .0004 .0004 .0002 .0001 .0001 .0001 .0001
107.7	48.59 .0000 .0001	.0001 .0002 .000100010000 .0000
123.1	20.7900140060	00060005100420054005000820063
123.1	30.0000010005	50003 .0000 .0007 .0004000200070008
123.1	39.210000 .0001	.0002 .0006 .0007 .0006 .0004 .0000 .0000
123.1	48.42 .0000 .0000	.0001 .0002 .0003 .0003 .00010001
123.1	57.63 .0000 .0000	0 .0001 .0002 .0002 .0002 .0001 .0000
138.5	24.0400100045	50058006600590040003500450052
138.5	34.7000010009	00008000700030003 .0001 .00010004
138.5		2 .0001 .0002 .0004 .0005 .0005 .0003
138.5	56.01 .0000 .0001	.0001 .0001 .0002 .0002 .0003 .0003 .0001
138.5		2 .0002 .0002 .0002 .0003 .0003 .0003 .0002
153.8		'0064006300780086008200490052
153.8		0006001000090008000800020001
153.8		.0003 .0003 .0002 .0003 .0004 .0005 .0005
153.8	63.61 .0000 .0004	.0003 .0003 .0002 .0002 .0003 .0003 .0003
153.8		.0004 .0003 .0003 .0002 .0003 .0003 .0003
169.2	30.5400010059	0075007300830091008701240113
169.2	44.0900010005	5000200070010001200090009
169.2	57.65 .0000 .0005	0.0005 .0004 .0004 .0003 .0004 .0004 .0004
169.2	71.20 .0000 .0004	0004 .0004 .0003 .0003 .0002 .0002 .0003
169.2	84.750001 .0005	0005 .0005 .0004 .0004 .0004 .0004 .0004
184.6	33.7900020124	0122010301010124013001290147
184.6	48.7900000010	00005000900060006000800060009
184.6	63.79 .0001 .0005	0006 .0006 .0006 .0005 .0005 .0004 .0005
184.6	/8.80 .0000 .0003	0004 .0004 .0004 .0003 .0003 .0003 .0003
184.6	93.800001 .0004	0005 .0005 .0005 .0004 .0004 .0004 .0004
200.0	57.0400000150	00165013701430127012201330145 00004001100050007000700100010
200.0	55.4900000010	.0005 .0005 .0005 .0005 .0005 .0005 .0004
	09.94 .UUUI .UUU3	.0004 .0004 .0005 .0004 .0004 .0003 .0003
200.0	86.39 .0000 .0003	COOO. COOO. POOO. POOO. COOO. POOO. POOO.

Table D.22 - Entrainment Field \overline{u} (θ =-45°)

	Unforced			Pha	se ave	eraged	data (at angle ϕ)			
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
107.7	17.54	.028	.050	.053	.058	.062	.076	.092	.088	.060
107.7	33.07	.012	.015	.018	.016	.014	.015	.017	.016	.013
107.7	48.59	.013	.012	.012	.010	.008	.007	.007	.009	.010
138.5	24.04	.020	.059	.061	.055	.047	.045	. 047	.049	.054
138.5	45.36	.015	.011	.012	.012	.013	.013	.013	.012	.011
138.5	66.67	.010	.007	.007	.007	.007	.008	.007	.007	.007
169.2	30.54	.019	.058	.060	.064	.067	.068	.064	.061	.058
169.2	57.65	.015	.013	.012	.012	.012	.012	.012	.012	.013
169.2	84.75	.009	.007	.007	.007	.007	.007	.007	.007	.007
200.0	37.04	.020	.073	.070	.067	.068	.068	.071	.073	.074
200.0	69.94	.014	.012	.012	.013	.012	.012	.012	.012	.012

Table D.23 - Entrainment Field \tilde{u} (θ =-45°)

	Unforced			Pha	se ave	eraged	data (at angle ϕ)			
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
107.7	17.54	.0208	.0380	.0325	.0348	.0379	.0432	.0441	.0451	.0443
107.7	33.07	.0048	.0069	.0084	.0091	.0085	.0090	.0090	.0078	.0057
107.7	48.59	.0039	.0056	.0060	.0059	.0051	.0043	.0041	.0048	.0053
138.5									.0364	
138.5	45.36	.0062	.0071	.0071	.0067	.0070	.0074	.0077	.0072	.0072
138.5									.0041	
169.2									.0506	
169.2									.0074	
169.2									.0043	
200.0									.0629	
200.0									.0070	

Table D.24 - Entrainment Field \overline{v} (θ =-45°)

	Unfor			data (at angle ϕ)			
x/θ_0	y/θ_0 dat	a 0.0 45.0	90.0 135.0	180.0 225.0 270.0	315.0		
107.7	17.54029	9053056	067086	091071046	047		
107.7	33.0701	8013017	027035	038033024	016		
107.7	48.5902	4021022	025029	031030027	023		
138.5	24.04023	3062054	048045	047053060	065		
138.5	45.36024	4031028	024022	023026030	032		
138.5	66.67028	3031031	030029	029030030	031		
169.2	30.54024	4061064	064063	061058058	059		
169.2	57.65027	7025026	027027	026025024	024		
169.2	84.75030	030030	029030	030029030	030		
200.0	37.04026	5061059	061062	064065064	063		
200.0	69.94030	0023022	022023	024024024	024		

Table D.25 - Entrainment Field $\tilde{\mathbf{v}}$ (θ =-45°)

					ase averaged data (at angle ϕ)					
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
107.7	17.54	.0218	.0421	.0377	.0397	.0404	.0373	.0339	.0327	.0349
107.7	33.07	.0083	.0117	.0148	.0163	.0163	.0149	.0130	.0112	.0098
107.7	48.59	.0048	.0084	.0093	.0093	.0083	.0074	.0068	.0066	.0071
138.5	24.04	.0164	.0351	.0348	.0359	.0352	.0343	.0369	.0375	.0364
138.5	45.36	.0073	.0136	.0128	.0122	.0120	.0128	.0137	.0141	.0141
138.5	66.67	.0038	.0059	.0058	.0057	.0058	.0060	.0062	.0062	.0061
169.2	30.54	.0168	.0441	.0446	.0435	.0407	.0413	.0413	.0428	.0425
169.2	57.65	.0073	.0127	.0130	.0131	.0130	.0126	.0123	.0122	.0124
169.2	84.75	.0036	.0052	.0053	.0055	.0055	.0055	.0054	.0052	.0052
200.0	37.04	.0162	.0459	.0435	. 0446	.0456	.0458	.0452	.0435	.0449
200.0	69.94	.0074	.0119	.0118	.0118	.0119	.0121	.0123	.0123	.0121

Table D.26 - Entrainment Field $\overline{\mathbf{u'v'}}$ (θ --45°)

	Unforced	Phase averaged data (at angle ϕ)
x/θ_0	y/θ_0 data 0.0	45.0 90.0 135.0 180.0 225.0 270.0 315.0
107.7	17.5400190096	004600280006 .0005 .001300070054
107.7	33.07 .0001 .0004	.0008 .0010 .0007 .00010001 .0001 .0002
107.7	48.59 .0002 .0005	.0006 .0006 .0004 .0003 .0003 .0003 .0004
138.5	24.0400040022	0031005000500048003800250033
138.5	45.36 .0002 .0004	.0004 .0005 .0006 .0007 .0007 .0007 .0006
138.5	66.67 .0001 .0002	.0002 .0003 .0003 .0003 .0003 .0002
169.2	30.5400040052	0052003400400058005800700065
169.2	57.65 .0003 .0007	.0007 .0007 .0007 .0007 .0007 .0007 .0007
169.2	84.75 .0001 .0002	.0002 .0003 .0003 .0003 .0002 .0002
200.0	37.0400010073	0068010700690069006900670086
200.0	69.94 .0004 .0007	.0007 .0007 .0007 .0007 .0007 .0007 .0007

Table D.27 - Entrainment Field \overline{u} (θ =-90°)

	U	nforced	Phase	averaged	data (at angle ϕ)			
x/θ_0	y/θ_0	data 0.0	45.0 90	0.0 135.0	180.0	225.0	270.0	315.0
107.7 107.7 107.7 138.5 138.5 138.5 169.2 169.2	17.54 33.07 48.59 24.04 45.36 66.67 30.54 57.65 84.75	.012 .007 .007001 .004 .006 .011 .006 .007006 .008011 .009006	.006 .0	.005 .005 .002001 .005011 .005 .002 .006006 .006007 .006004	.001 007 009 004 009	.001 008 011 004 009	.002 007 012 005 009	.010 .001 .003 .004 006 010 006
200.0 200.0	69.94		0060					

Table D.28 - Entrainment Field \tilde{u} (θ =-90°)

	Unforced			Phase averaged			data (at angle ϕ)			
x/θ_0	y/θ_0	data	0.0	45.0	90.0	135.0	180.0	225.0	270.0	315.0
107.7								.0704		
107.7								.0174		.0156
107.7								.0053		.0044
138.5								.0407		
138.5								.0106		.0116
138.5								.0050		.0048
169.2	30.54	.0208	.0475	.0491	.0486	.0493	.0501	.0512	.0494	.0471
169.2								.0096		
169.2								.0052		
200.0								.0500		.0519
200.0	69.94	.0029	.0087	.0088	.0088	.0089	.0086	.0087	.0087	.0088

Table D.29 - Entrainment Field \bar{v} (θ =-90°)

					data (at angle ϕ)				
x/θ 0	y/θ_0 d	ata 0.0	45.0	90.0 1	135.0	180.0	225.0	270.0	315.0
107.7	17.54	097135	131	150 -	177	186	171	156	150
107.7	33.07	024 037	034	036 -	041	047	050	047	042
107.7	48.59	023025	026	029 -	031	031	029	027	025
138.5	24.04	061116	117	112 -	103	095	093	099	109
138.5	45.36	024039	036	034 -	034	036	039	041	042
138.5	66.67	027033	032	031 -	031	032	032	033	033
169.2	30.54	045113	115	116 -	119	120	120	118	114
169.2	57.65	029033	034	034 -	033	032	032	032	032
169.2	84.75	029032	032	032 -	032	032	032	032	032
200.0	37.04	036127	124	122 -	120	119	122	125	127
200.0	69.94	031027	027	027 -	028	028	029	029	028

Table D.30 - Entrainment Field \tilde{v} (θ =-90°)

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Unforced Phase averaged data (at angle \phi) x/\theta_0 data 0.0 45.0 90.0 135.0 180.0 225.0 270.0 315.0 107.7 17.54 .0596 .0786 .0812 .0941 .0925 .0832 .0771 .0713 .0750 107.7 33.07 .0094 .0190 .0203 .0200 .0196 .0182 .0181 .0179 .0181 107.7 48.59 .0028 .0063 .0068 .0068 .0064 .0057 .0053 .0053 .0058 138.5 24.04 .0413 .0667 .0707 .0738 .0682 .0628 .0579 .0579 .0610 138.5 45.36 .0061 .0142 .0142 .0138 .0143 .0144 .0148 .0148 .0144 138.5 66.67 .0027 .0044 .0041 .0039 .0040 .0043 .0046 .0047 .0046 169.2 30.54 .0275 .0683 .0693 .0674 .0709 .0749 .0797 .0780 .0728 169.2 57.65 .0053 .0118 .0122 .0124 .0118 .0118 .0120 .0123 .0119 169.2 84.75 .0027 .0043 .0043 .0043 .0043 .0042 .0041 .0041 .0042 200.0 37.04 .0186 .0798 .0808 .0783 .0753 .0742 .0763 .0761 .0783 200.0 69.94 .0050 .0100 .0097 .0098 .0102 .0109 .0111 .0102 .0103
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Table D.31 - Entrainment Field $\overline{\mathbf{u'v'}}$ (θ =-90°)

	Unforced	Phase averaged data (at angle ϕ)
x/θ_0	y/θ_0 data 0.0	45.0 90.0 135.0 180.0 225.0 270.0 315.0
107.7	17.54 .0105 .0202	.0189 .0265 .0257 .0181 .0125 .0151 .0226
107.7	33.070002 .0002	0001 .0001000300030001 .0004 .0002
107.7	48.590000 .0001	.0001 .0001 .000000010001 .0000 .0001
138.5	24.04 .0036 .0100	.0133 .0157 .0132 .0073 .0020 .0013 .0034
138.5	45.36 .0000 .0000	.0001 .0001 .0002 .0002 .0002 .00000000
138.5	66.6700000000	0000 .0000 .0000 .0001 .0001 .00000000
169.2	30.54 .0012 .0081	.0093 .0073 .0109 .0167 .0176 .0149 .0118
169.2	57.650001 .0005	.0004 .0004 .0002 .0003 .0002 .0003 .0004
169.2	84.75 .0000 .0000	.0000 .0000 .0000 .0000 .0000 .0000
200.0	37 04- 0004 .0209	.0219 .0191 .0145 .0156 .0147 .0159 .0200
200.0	69 94- 0001 .0003	.0003 .0004 .0004 .0004 .0003 .0003 .0003

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End date June 21,1990

